

# 星形成銀河における円盤不安定性と 星形成クランプの形成プロセス

Disc instability in star-forming galaxies and  
formation mechanisms of their giant clumps

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I am going to talk about “giant clumps” in galaxies

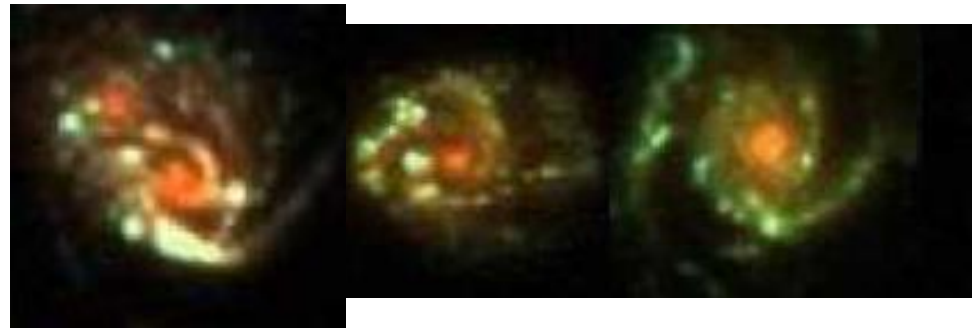
- “clump”

- is a very ambiguous word.
  - e.g. gas clouds, star cluster, dwarf galaxies etc.

- In this talk, “clump” I refer to as is

- “giant clumps”

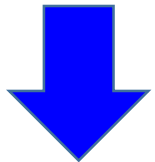
- found in gas-rich galaxies (mainly in high-z galaxies)
- massive star clusters containing much gas
- $\sim 10^8 M_{\odot}$  at the largest,  $\sim 1$  kpc in size.
- actively star-forming



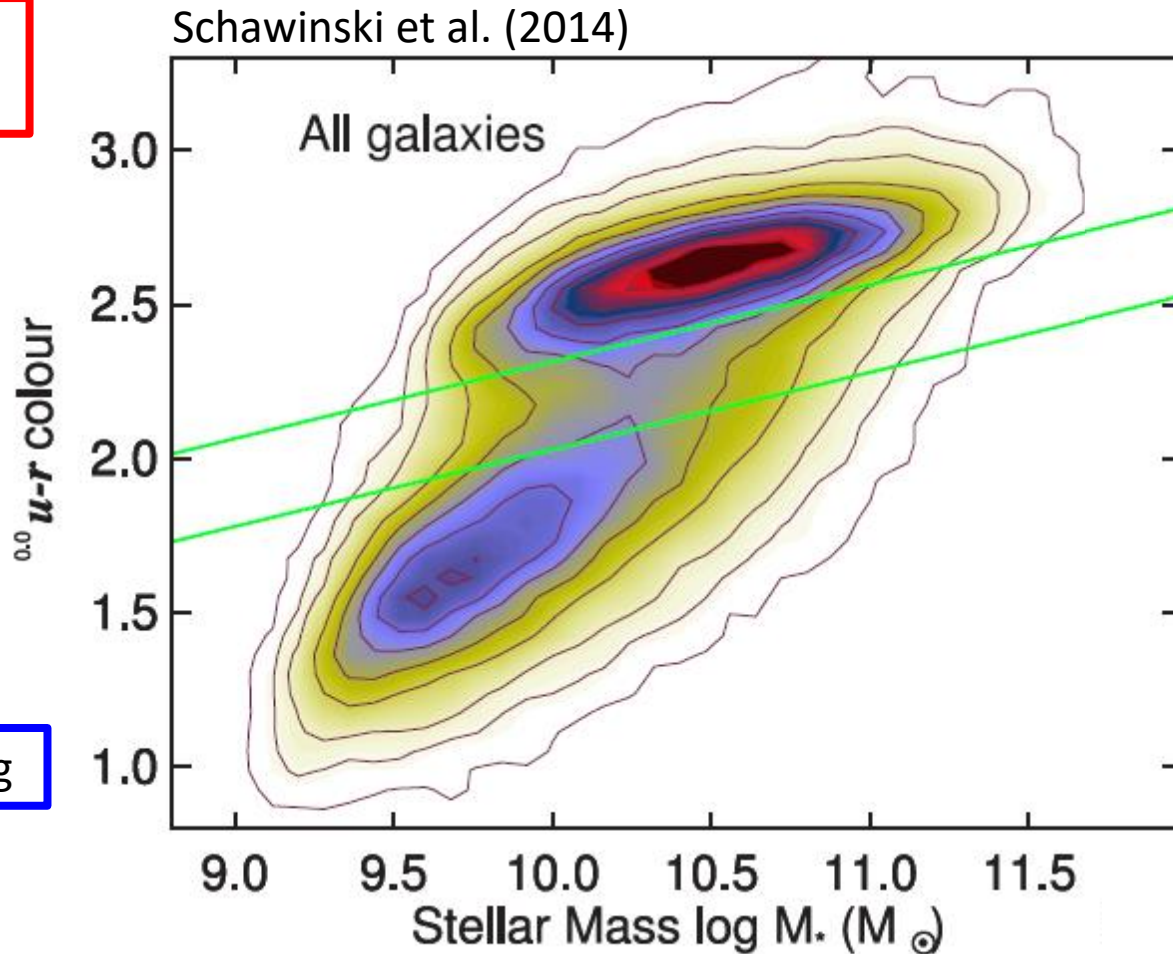
# Star formation in galaxies

- Colour – stellar mass relation

Quiescent/  
Quenched

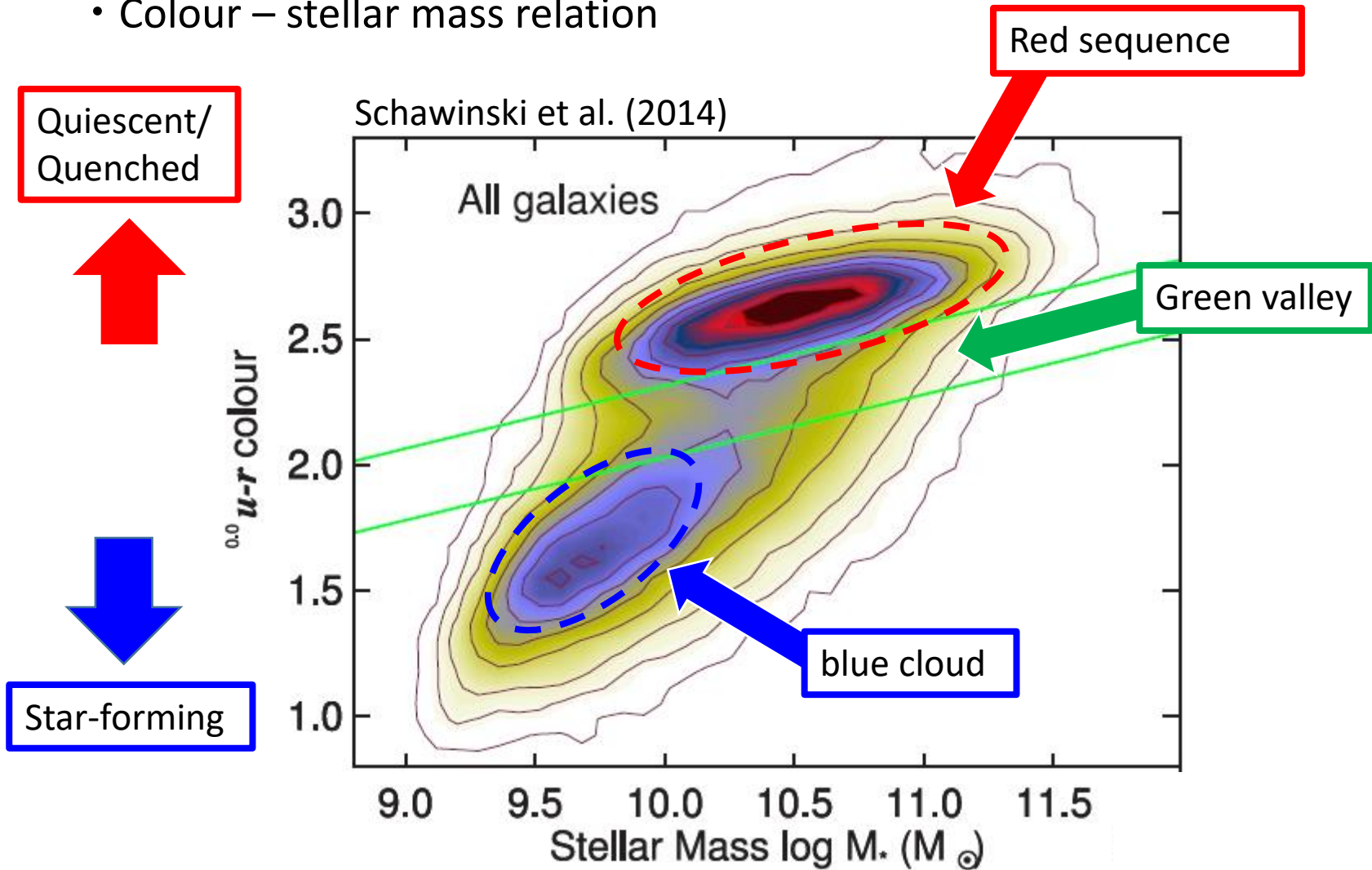


Star-forming



# Star formation in galaxies

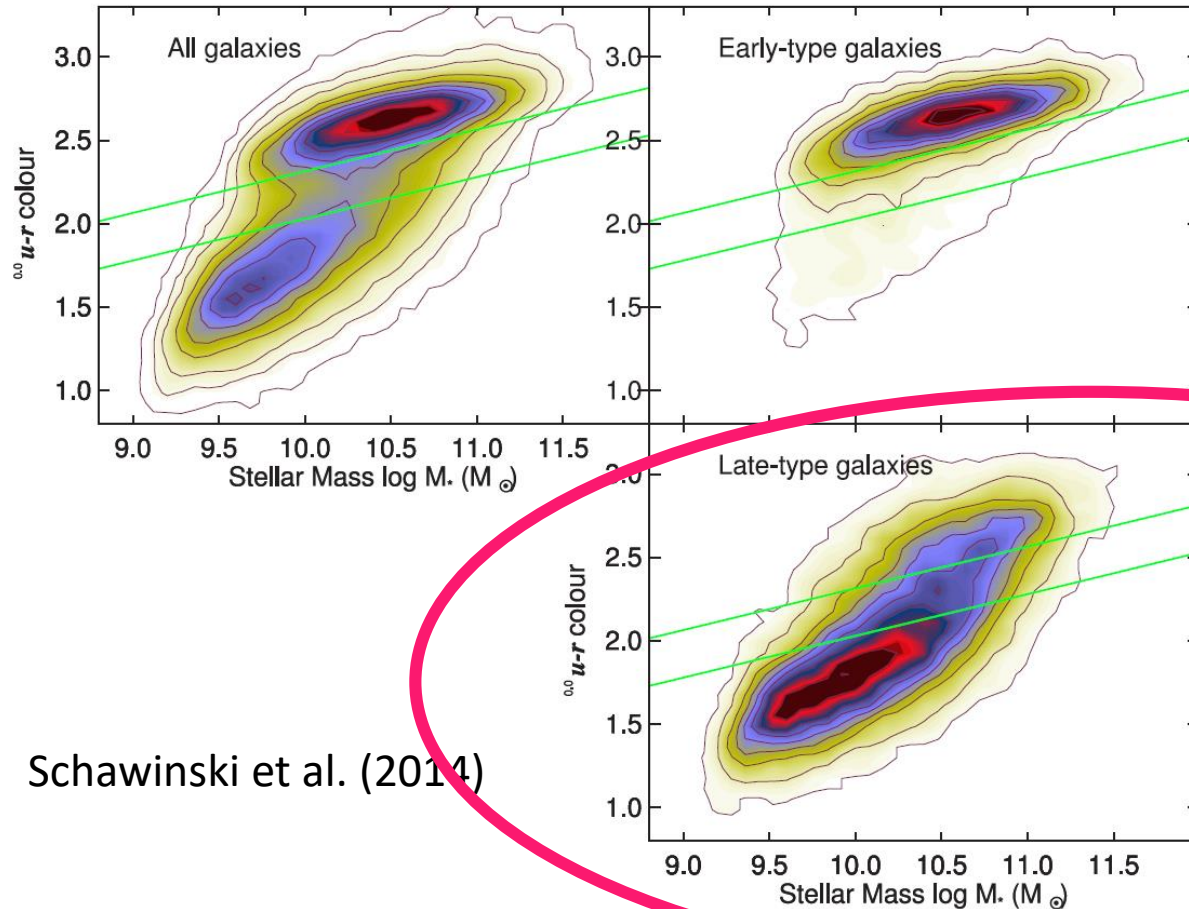
- Colour – stellar mass relation





# Star formation in galaxies

- Colour – stellar mass relation



Ellipticals



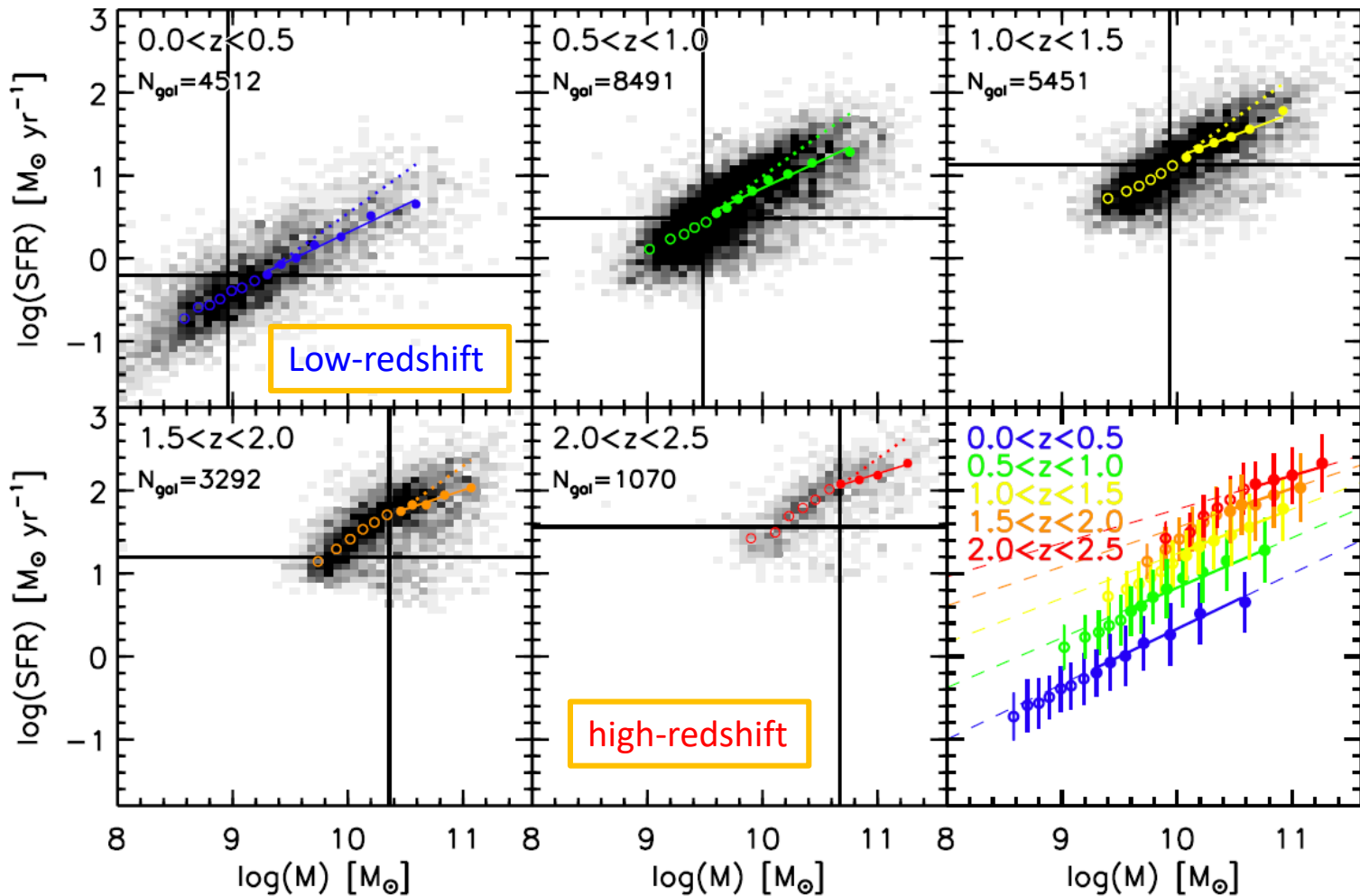
Discs

Schawinski et al. (2014)

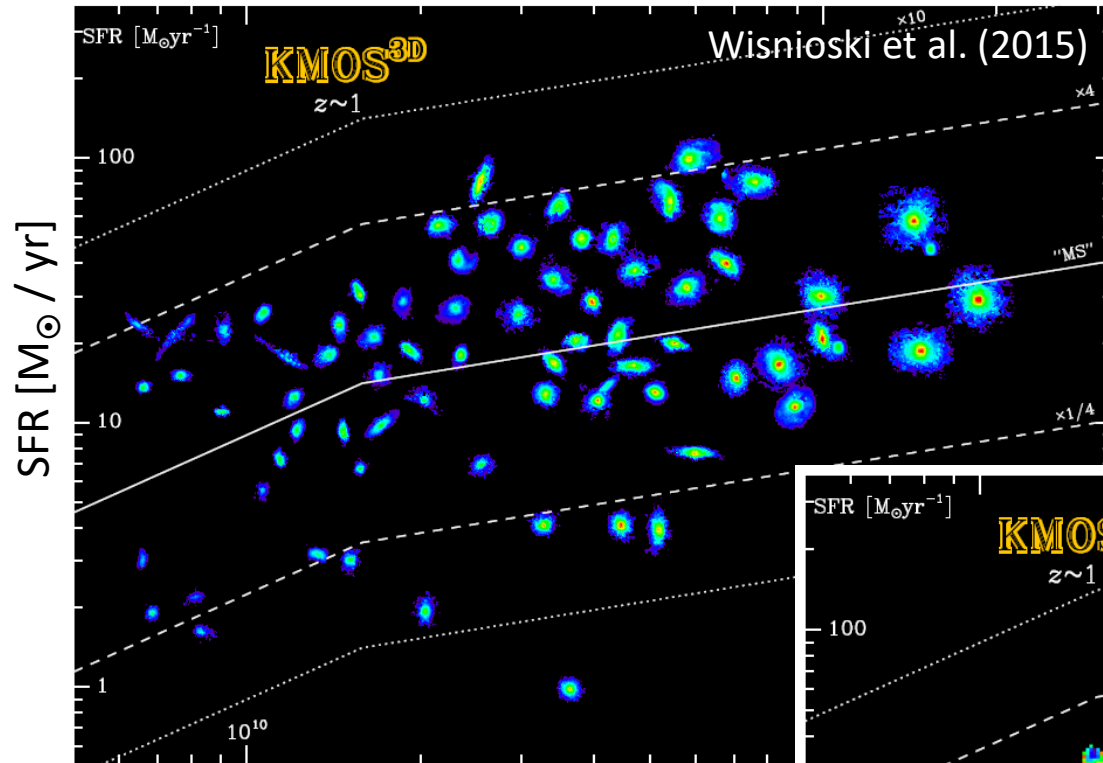
# Star-formation “main sequence”

- Tight correlations between stellar mass and SFR
  - Evolving with redshifts
  - The origin is still a mystery

Whitaker et al. (2012)



# What do the “main-sequence” galaxies look like?



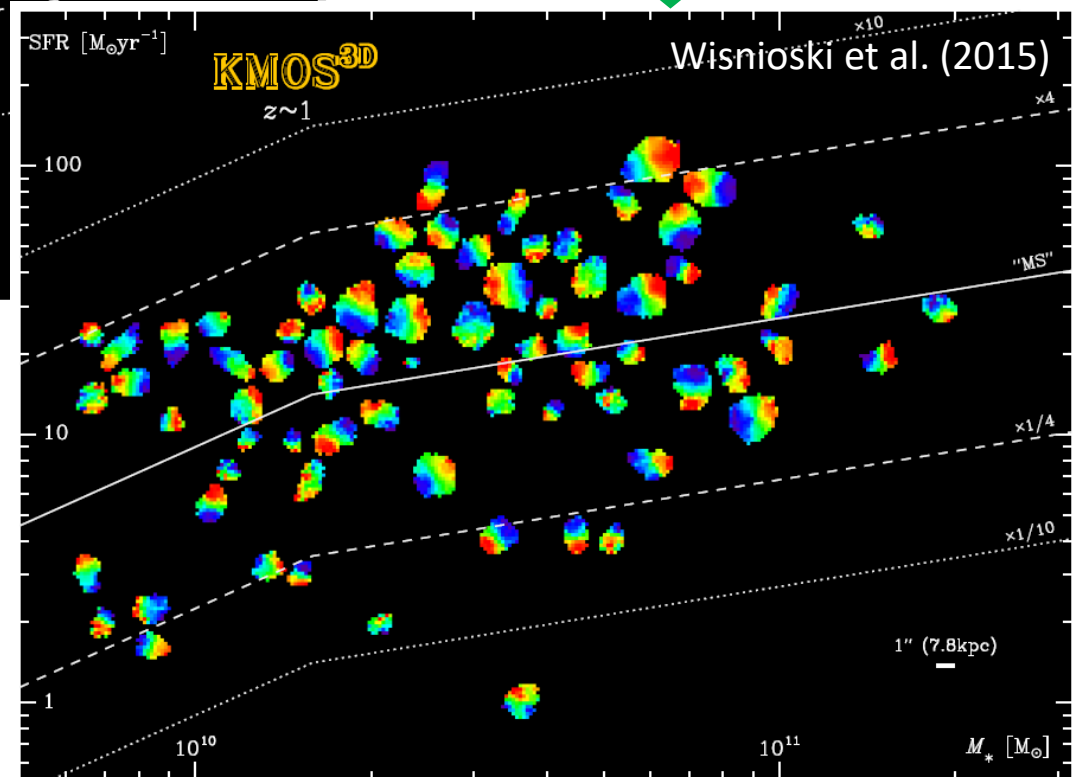
Stellar mass [ $M_{\odot}$ ]

Most of star-forming galaxies are rotating discs.

Most of star formation takes place in disc galaxies.

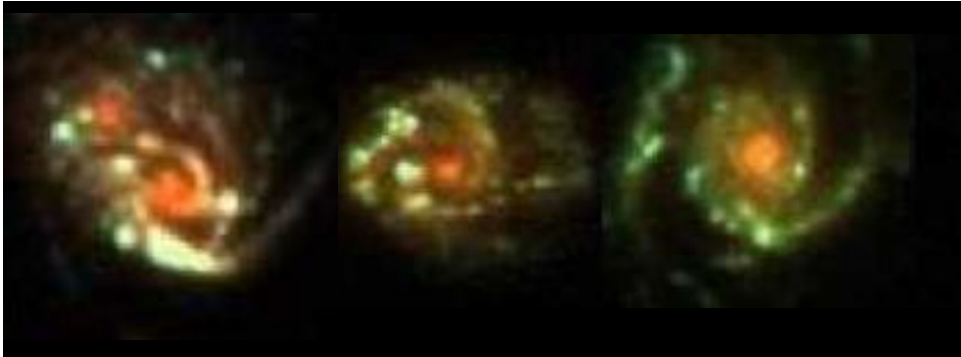
Stellar mass distributions

Line-of-sight velocity distributions



# Many of SF galaxies are clumpy

- Clumpy galaxies



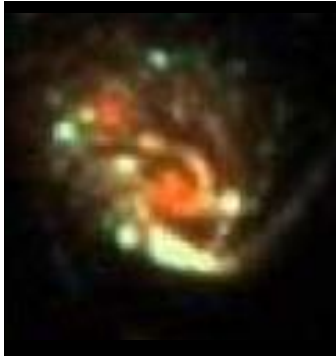
Guo et al. (2014)

- observed mainly at high redshifts  $z \sim 2$ .
- Quite rare at low-redshifts.

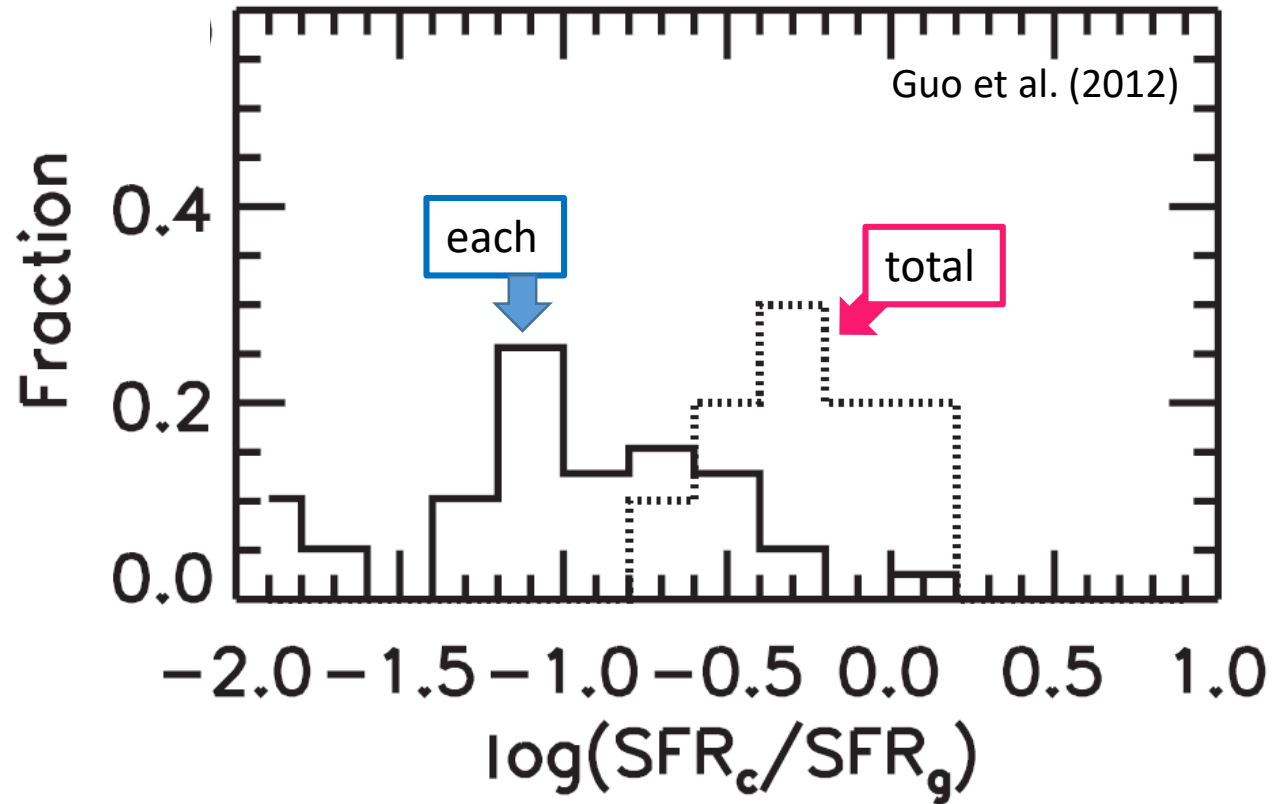
- The clumpy structures are detected with H $\alpha$  and UV light.
  - They are star-forming clumps
  - $\sim 10^8 M_{\odot}$  at the largest,  $\sim 1$  kpc in size

# Many of SF galaxies are clumpy

- Clumpy galaxies



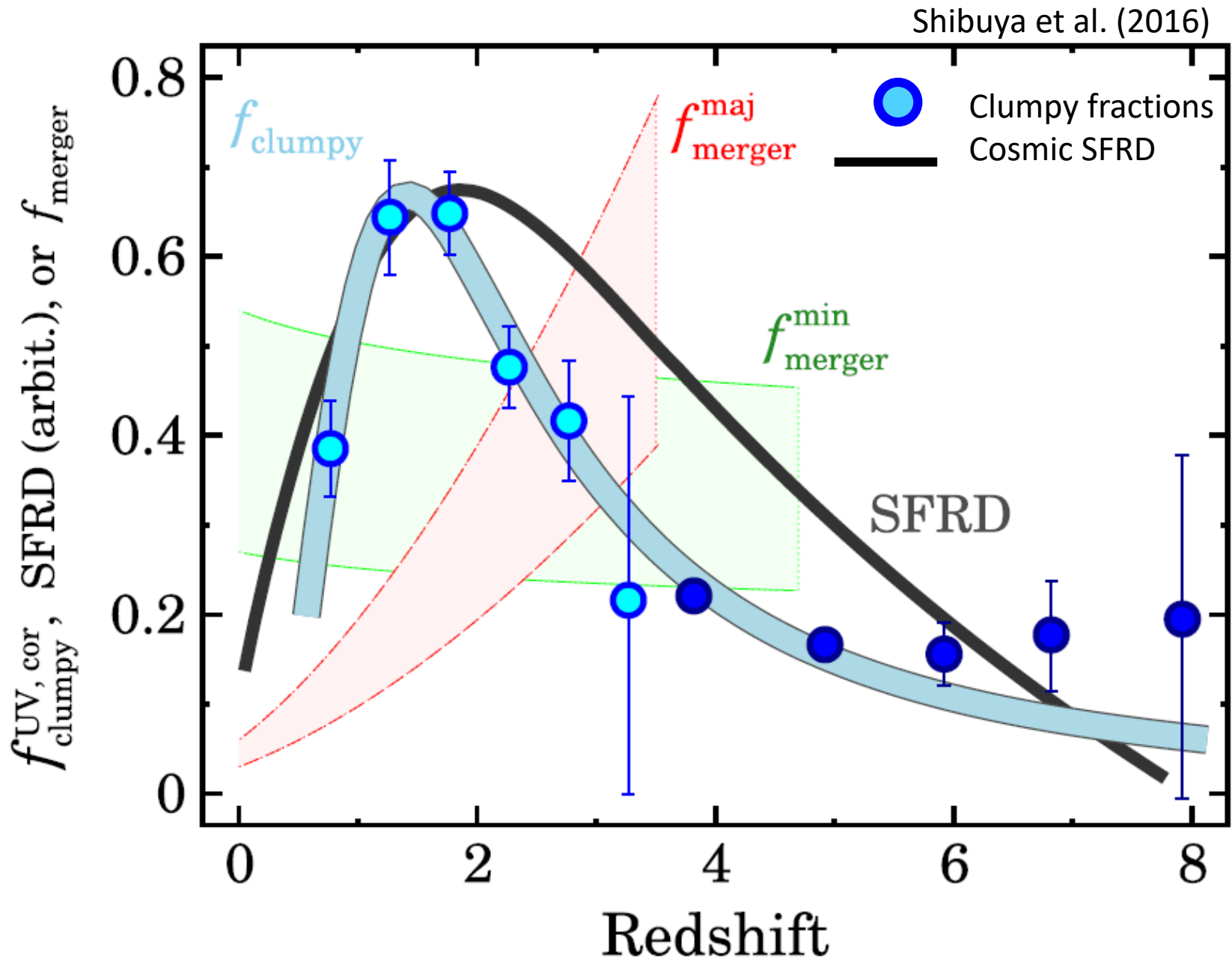
Guo et al. (2014)



- Each clump accounts for  $\sim 10\%$  of the galactic total SFR.
- **The total SFR in the clumps accounts for  $\sim 50\%$  of the galactic SFR.**
  - although the SFR fraction depends on spatial resolutions
    - see Dessauges-Zavadsky et al. 2016, Cava et al. 2017

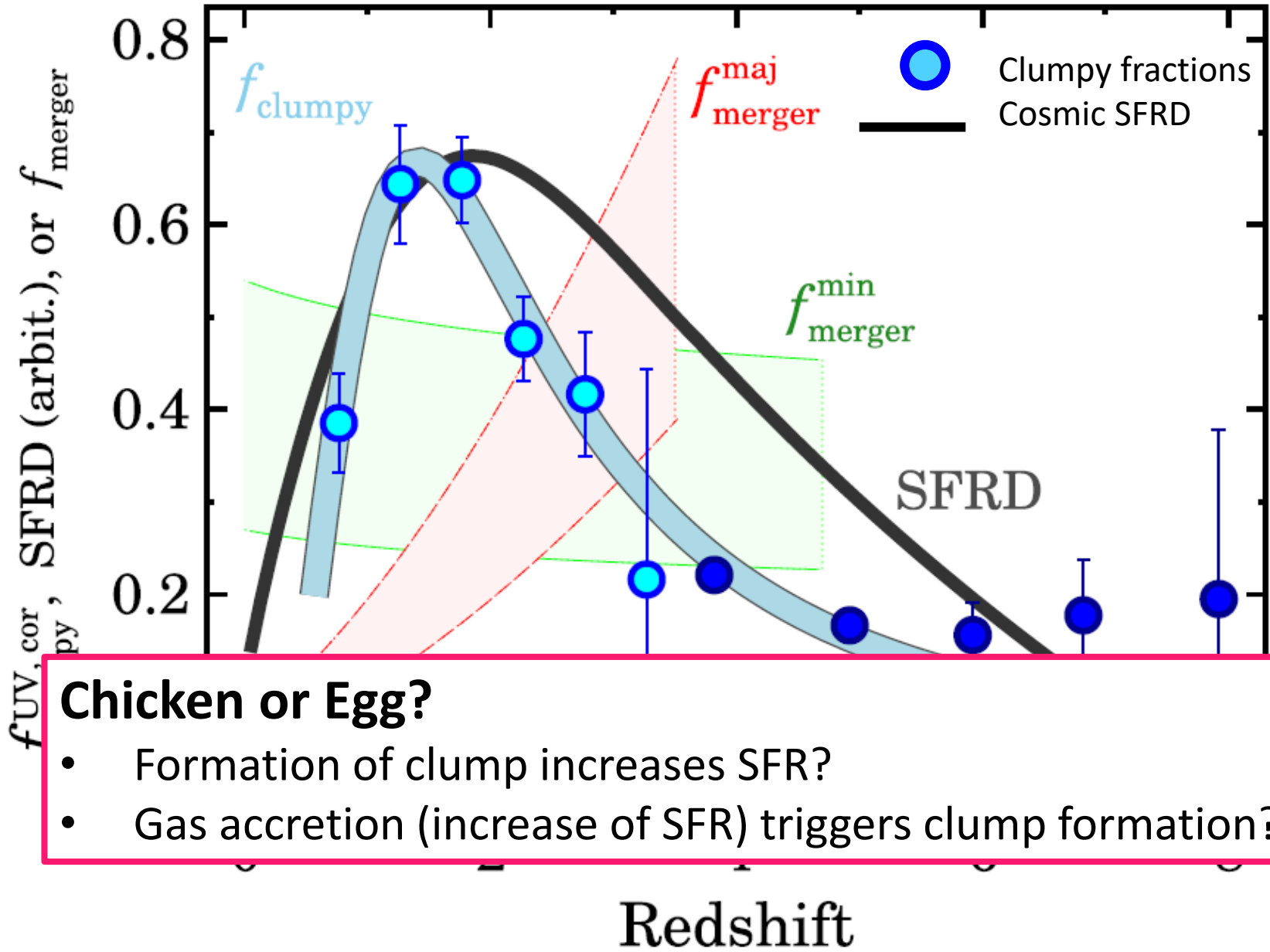
**Giant clumps are the main SF sites in gas-rich clumpy galaxies.**

# Clumpy fraction and cosmic SFR



# Clumpy fraction and cosmic SFR

Shibuya et al. (2016)



## Chicken or Egg?

- Formation of clump increases SFR?
- Gas accretion (increase of SFR) triggers clump formation?

# Fate of giant clumps: longevity or ephemerality?

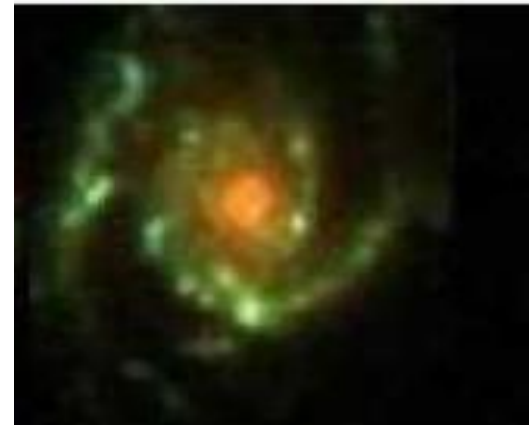
## • The long-lived scenario

- Noguchi 98, 99; Immeli+ 04; Bournaud+ 06, 08, 14; Ceverino+ 10, 12; Inoue+ 11, 12, 14; Forbs+ 13; Moody+ 14
- Observed giant clumps are gravitationally bound structures.
  - migrate to the galactic centres by dynamical friction and finally form bulges.
- Possible if feedback processes are weak and/or clump masses are large.

## • The short-lived scenario

- Genel+ 12; Hopkins+ 11; Buck+ 17; Oklopčić+ 17.
- Observed giant clumps are less-bound and/or tidally disrupted soon.
  - cannot migrate to the galactic centres and are transient structures.
- Possible if feedback processes are strong and/or clump masses are small.

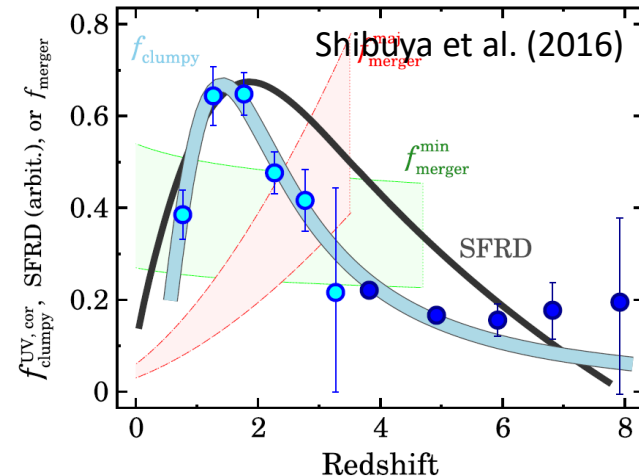
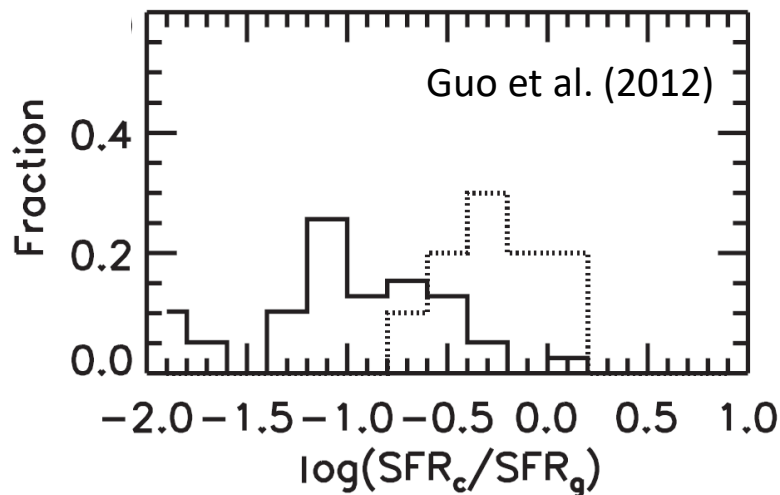
**Still under debate**





# Clump formation and star formation

- Thus, formation mechanisms of giant clumps are closely related to (global) physics of star formation in galaxies.
  - What drives giant-clump formation?
    - Gravitational instability (GI)
    - Cosmological gas accretion
    - Galactic mergers
  - What suppress giant-clump formation? (why clumps disappear?)
    - Disc stabilization by gas consumption and/or heating
    - Growth of a massive bulge
    - Cessation of galactic mergers





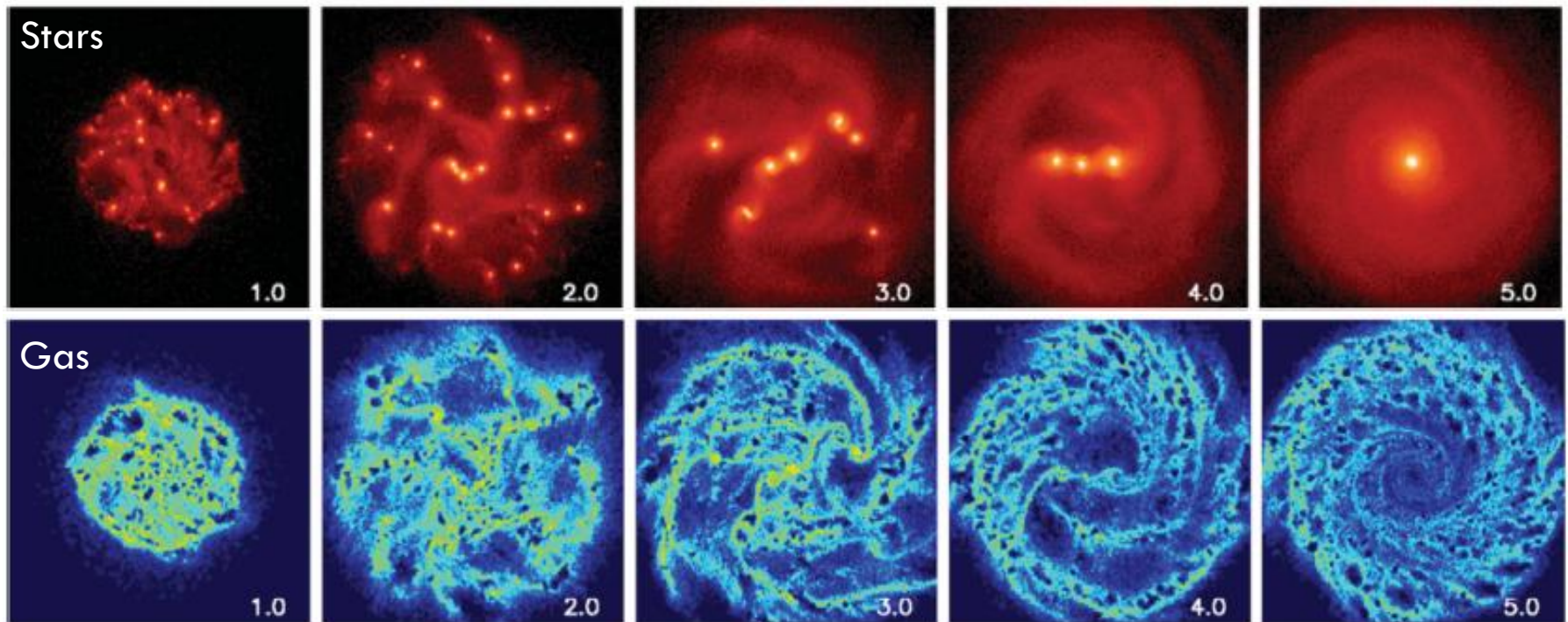
“Non-linear violent disc instability with high Toomre’s  $Q$  in high-redshift clumpy disc galaxies”

MNRAS, 456, 2052 (2016)

SI, Avishai Dekel, Nir Mandelker, Daniel Ceverino,  
Frederic Bournaud, Joel Primack

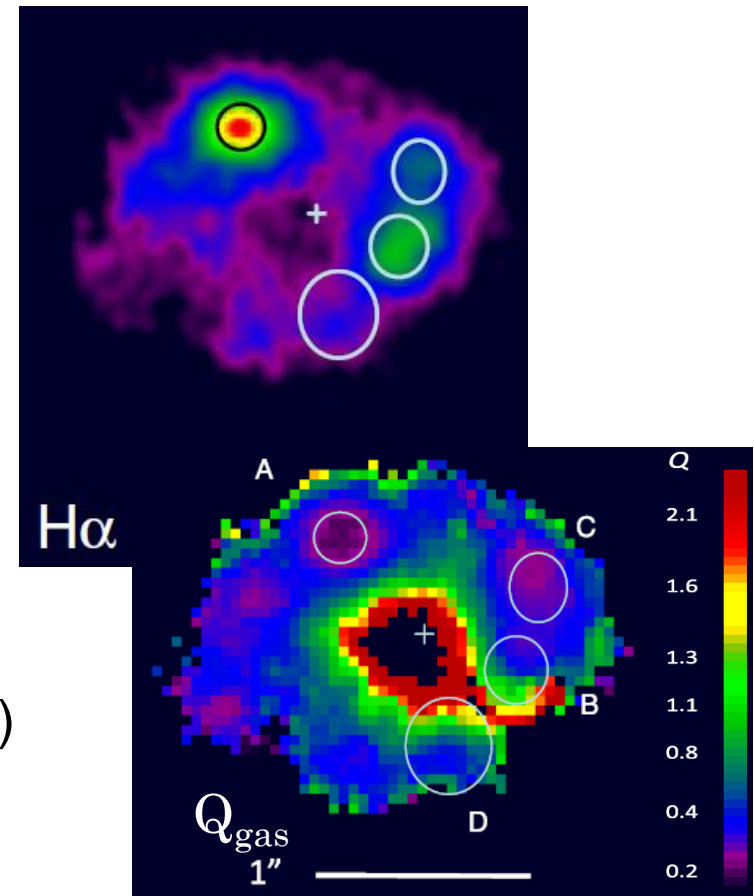
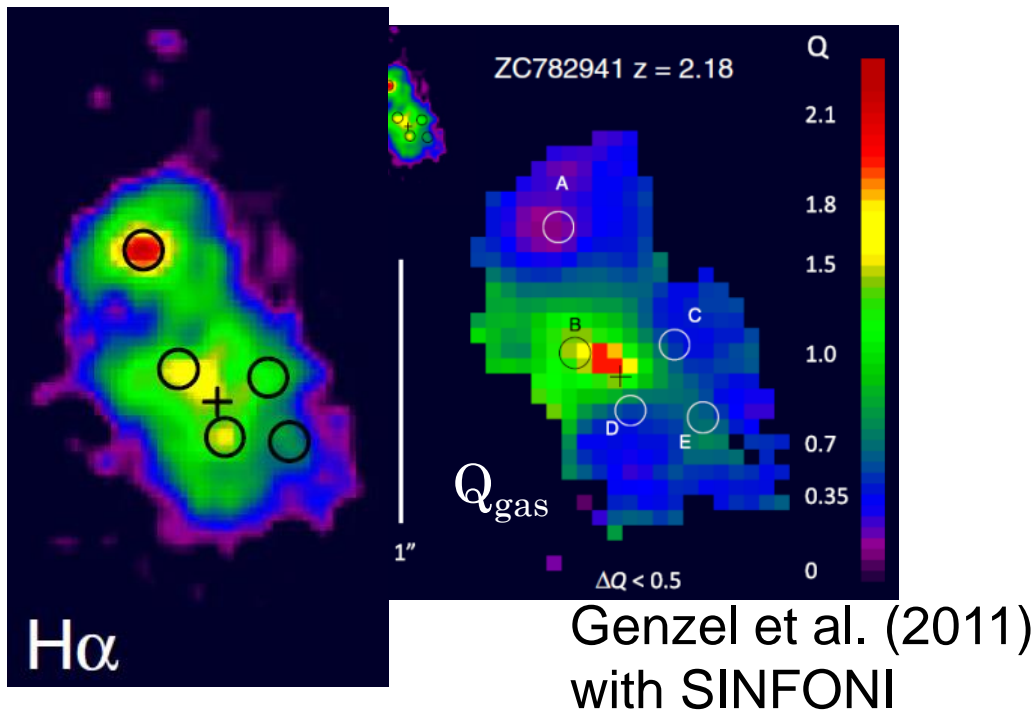
# Why are they clumpy?

- It has been proposed;
  - Galaxies are highly gas-rich (stream-fed) in their early formation stages.
  - Cold gas discs in the galaxies are **Toomre unstable** (Noguchi 1998, 1999).
  - **Clump formation is caused by ‘Toomre instability’**



# Toomre instability

- From a **local** and **linear** perturbation theory for **axisymmetric** perturbations,
- In observations,

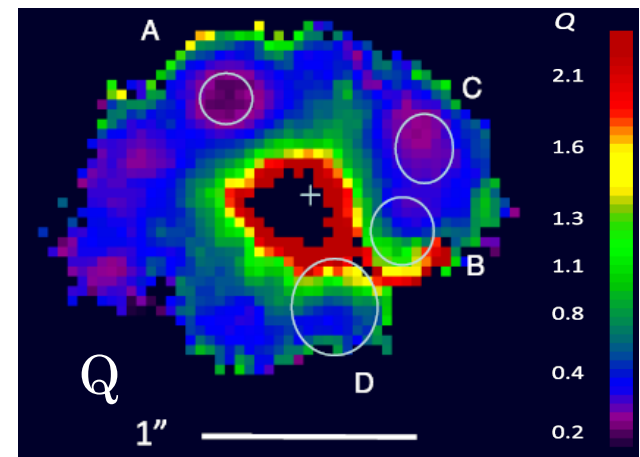


**$Q \leq 1$  in observed clumpy discs.**

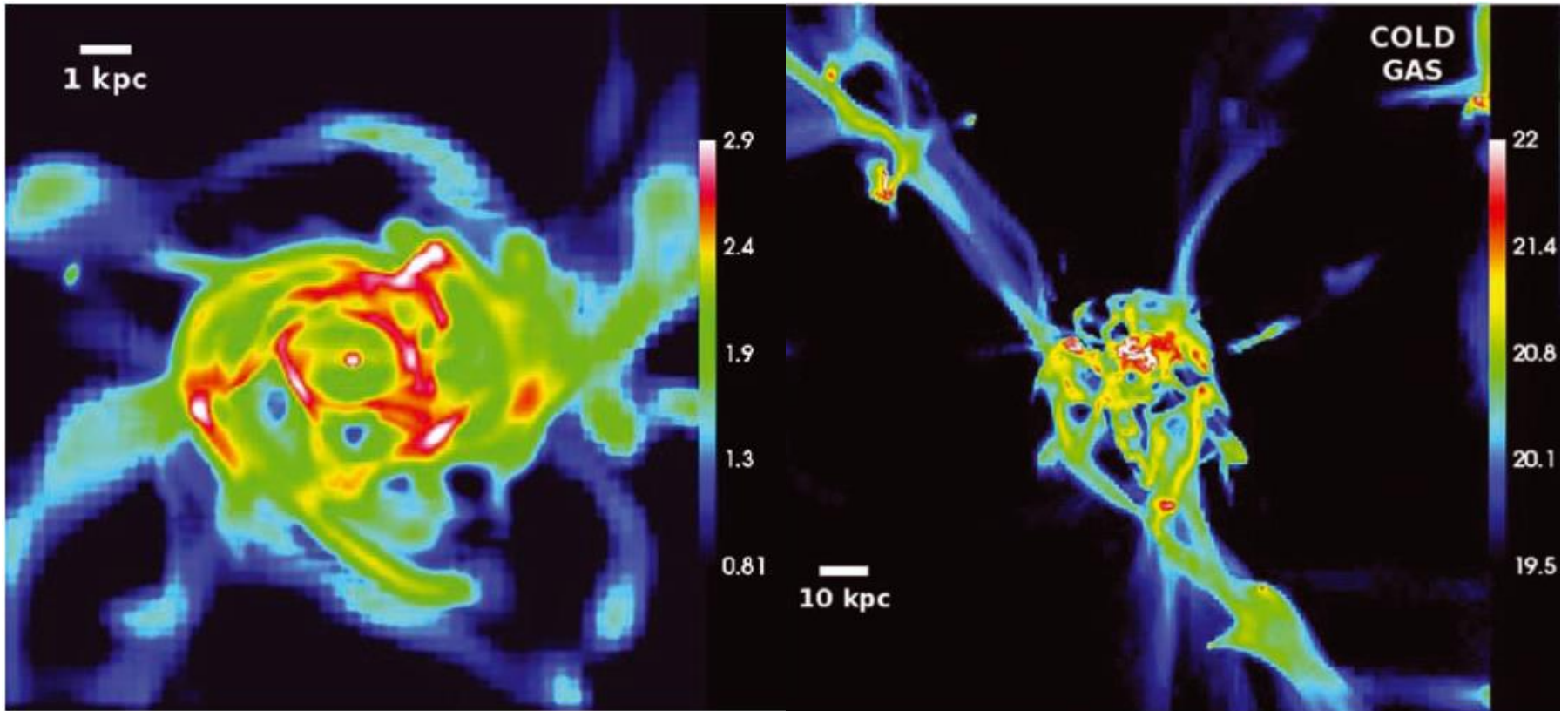
# Toomre instability

- However, dynamically unstable states cannot be long-lasting.
- The unstable regions will collapse soon, then their disc (inter-clump) regions turn over to stable states within the local dynamical time-scales.

The observation might be underestimating Toomre  $Q$ ...



# Toomre analysis in cosmological sims.



- Cosmological simulations
  - Ceverino et al. (2010, 2013) using ART code
    - 10pc-order resolution with radiation pressure.



# How to measure $Q_{2comp}$

- 2-component model (Romeo & Wiegert 2011)

- $Q_{gas} = \frac{\kappa_{gas}\sigma_{gas}}{\pi G \Sigma_{gas}}$  ,  $Q_{star} = \frac{\kappa_{star}\sigma_{star}}{3.36 G \Sigma_{star}}$

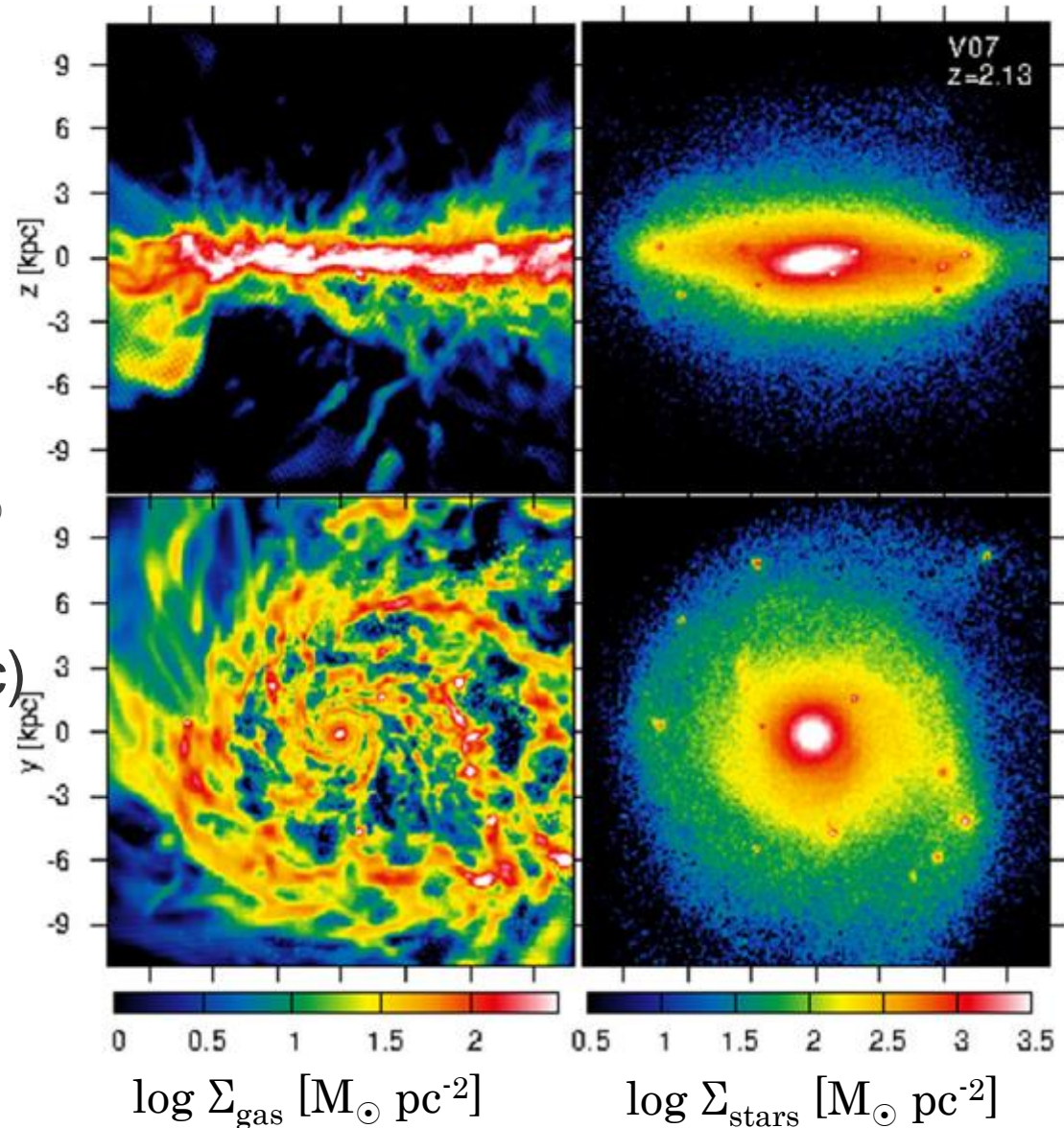
- $$\begin{cases} Q_{2comp}^{-1} = W Q_{gas}^{-1} + Q_{star}^{-1} & (if \ Q_{gas} > Q_{star}) \\ Q_{2comp}^{-1} = Q_{gas}^{-1} + W Q_{star}^{-1} & (if \ Q_{gas} < Q_{star}) \end{cases}$$

- $W \equiv \frac{\sigma_{gas}\sigma_{star}}{\sigma_{gas}^2 + \sigma_{star}^2}$

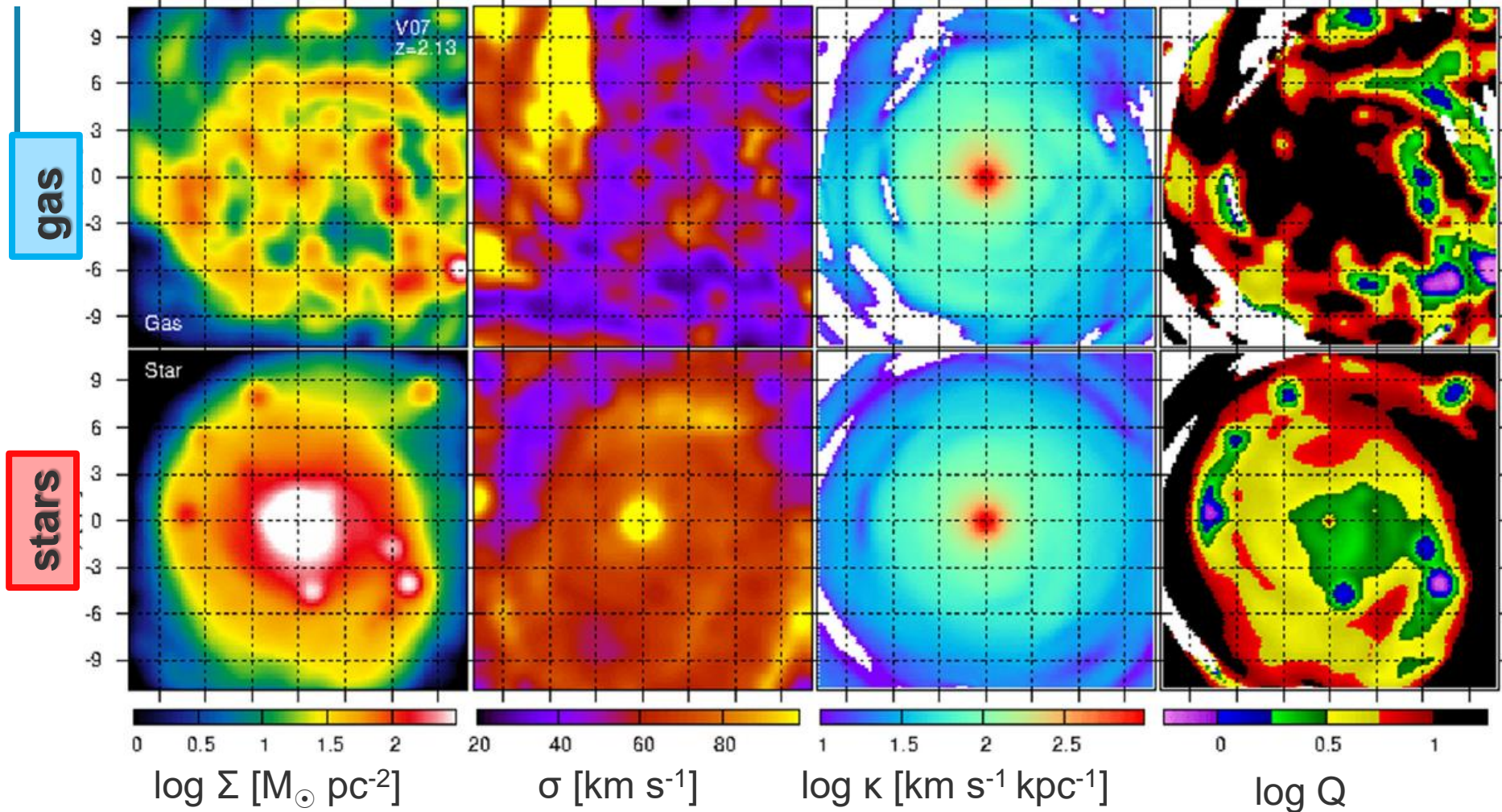
- $\sigma$  is velocity dispersion (not sound speed).
- $\kappa$  is calculated from mean velocity fields of gas/star.
  - $\kappa \equiv \sqrt{2 \frac{\langle v_\phi \rangle}{R} \left( \frac{d\langle v_\phi \rangle}{dR} + \frac{\langle v_\phi \rangle}{R} \right)}$
- Young stars (age < 100 Myr) are considered to be “gas”
- Bulge stars are removed ;  $j_z/j_{max} < 0.7$
- **Gaussian smoothing with FWHM=1.2 kpc**
  - to focus on  $M_{clump} = 10^{8-9} M_\odot$
- A razor-thin disc model (which gives lower limits)

# Cosmological simulations

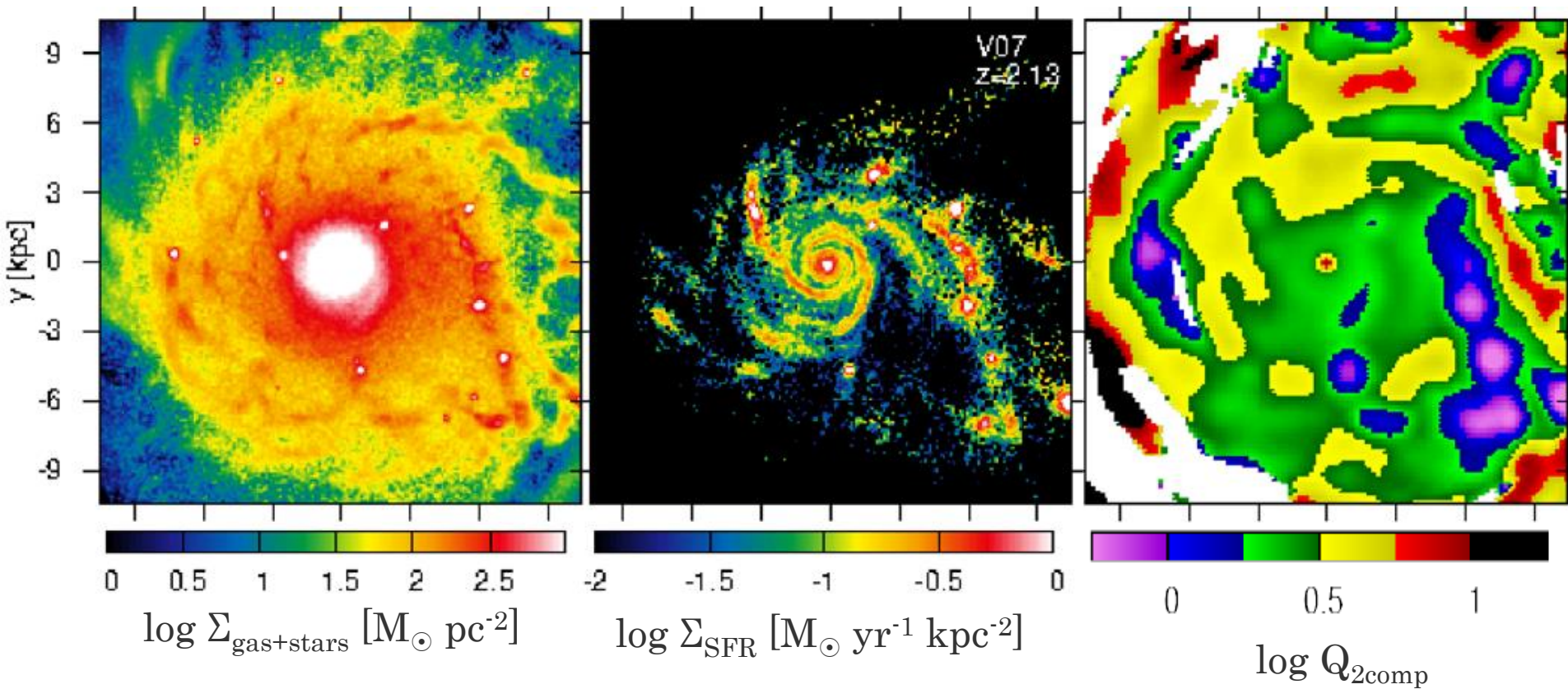
- V07
- $z = 2.13$
- $M_{vir} = 8.8 \times 10^{11} M_{\odot}$
- $M_{star} = 5.6 \times 10^{10} M_{\odot}$
- $f_{gas} = 0.18$
- $B/T = 0.37$  (kinematic)
- $SFR = 27.5 M_{\odot} \text{ yr}^{-1}$



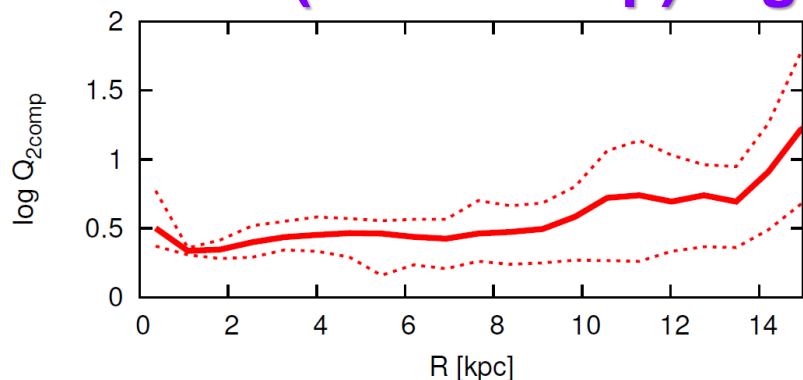




**Purple**  $Q < 1$ : linear instability  
**Blue**  $Q = 1 - 1.8$ : non-linear instability  
**Green**  $Q = 1.8 - 3$ : dissipative instability  
**Yellow, Red, Black**:  $Q > 3$ : stable state  
**White**: imaginary  $\kappa$  ( $Q$  cannot be defined)



- **Instability ( $Q < 1$ ) can only be seen in/around the clumps.**
- **Disc (inter-clump) regions seem to be stable ( $Q > 2$ ).**



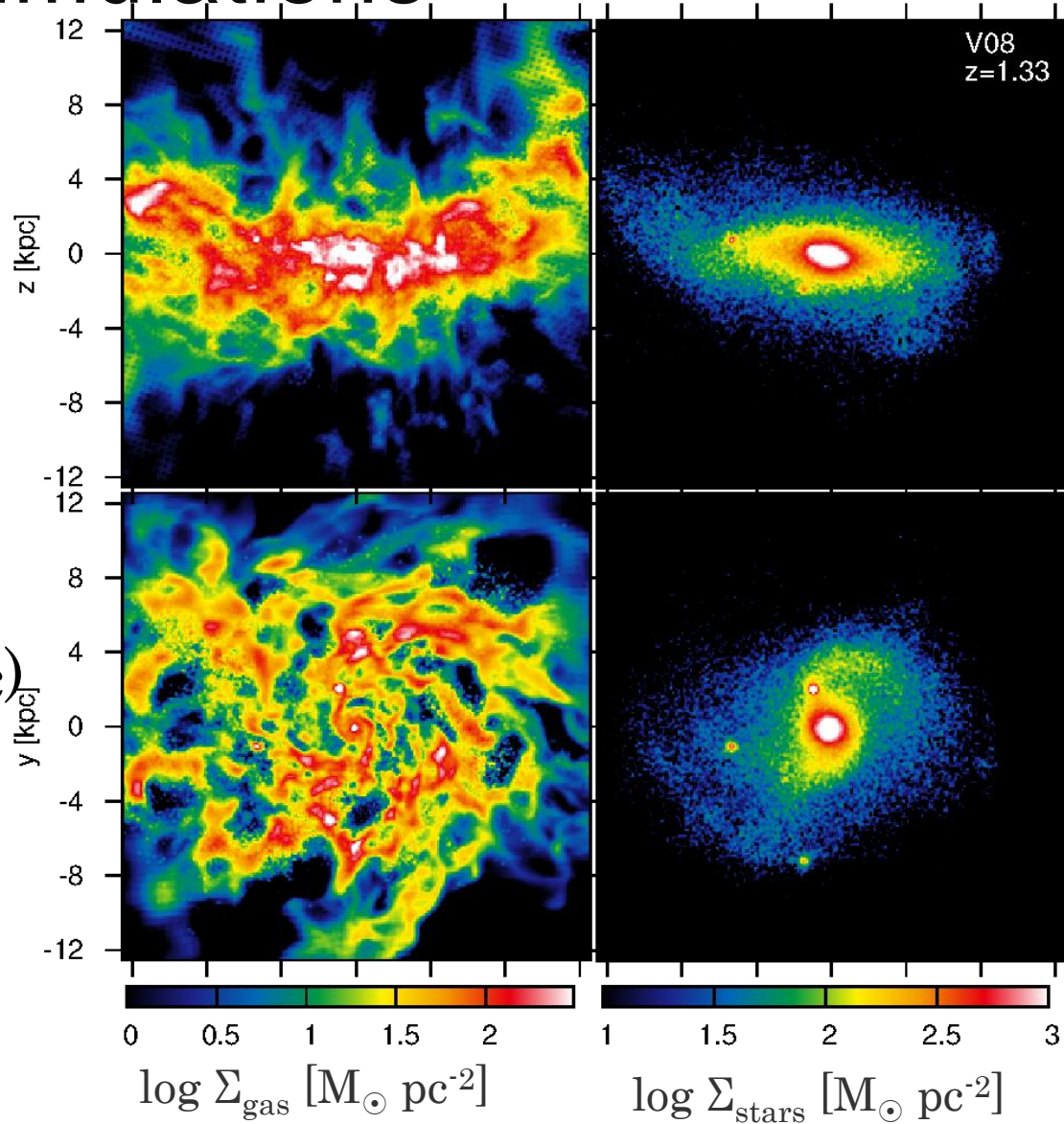
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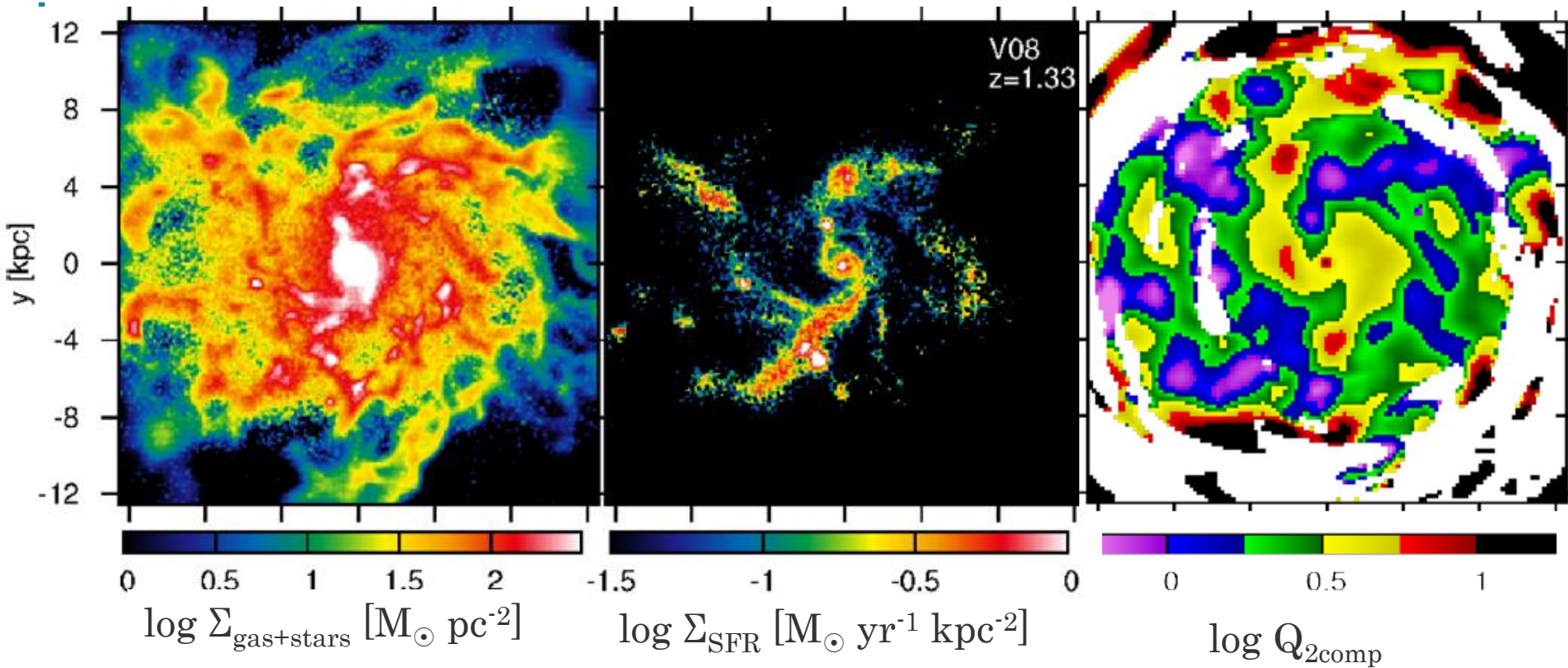


# Cosmological simulations

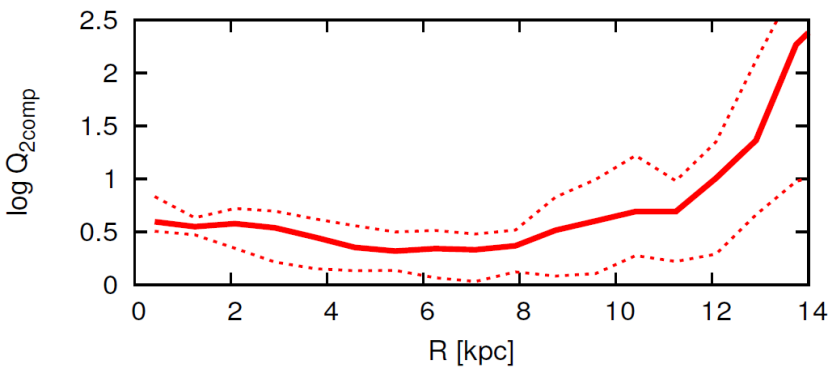
- V08

- $z = 1.33$
- $M_{vir} = 6.0 \times 10^{11} M_{\odot}$
- $M_{star} = 1.9 \times 10^{10} M_{\odot}$
- $f_{gas} = 0.42$
- $B/T = 0.45$  (kinematic)
- $SFR = 33.1 M_{\odot} \text{ yr}^{-1}$





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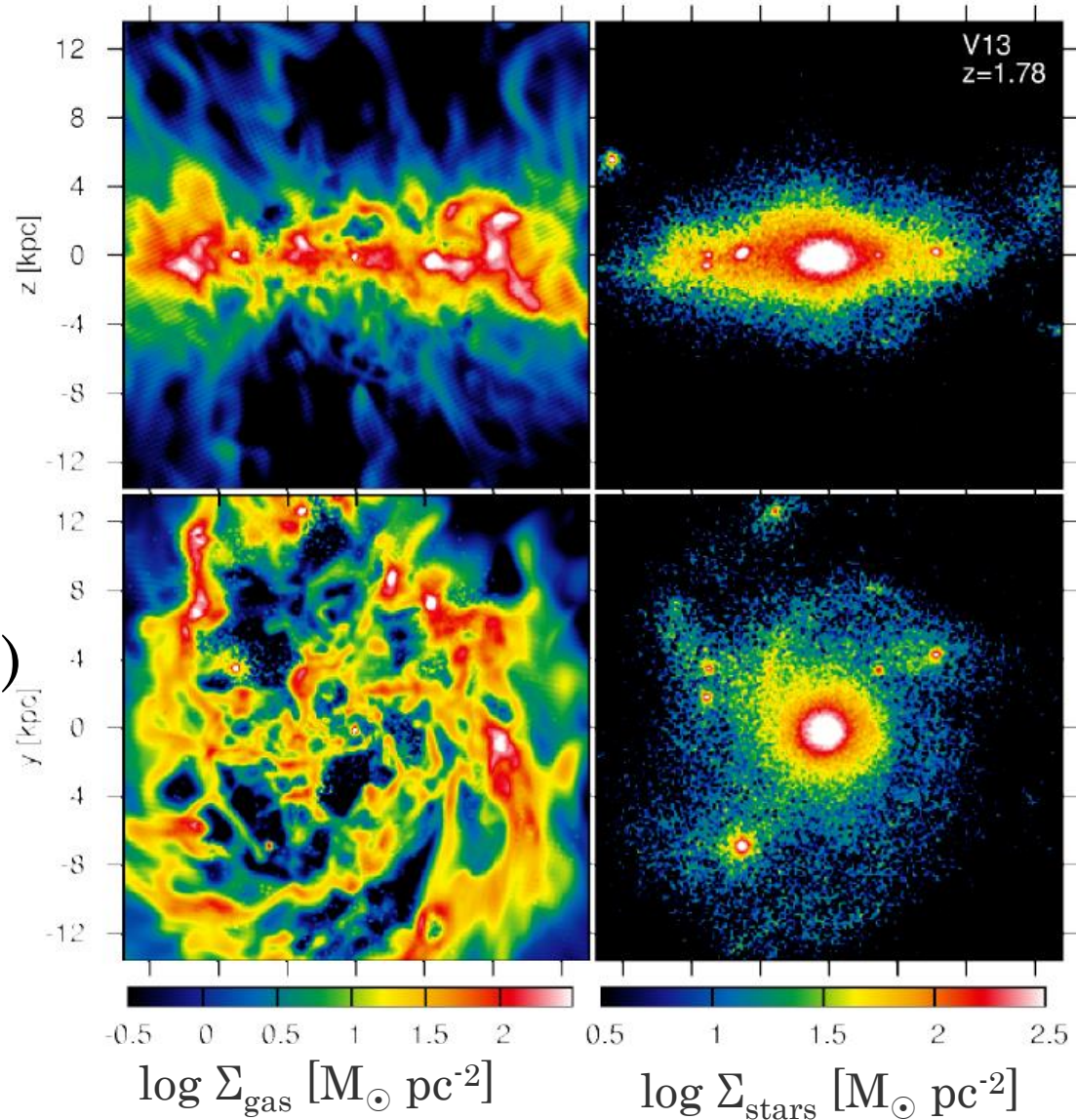
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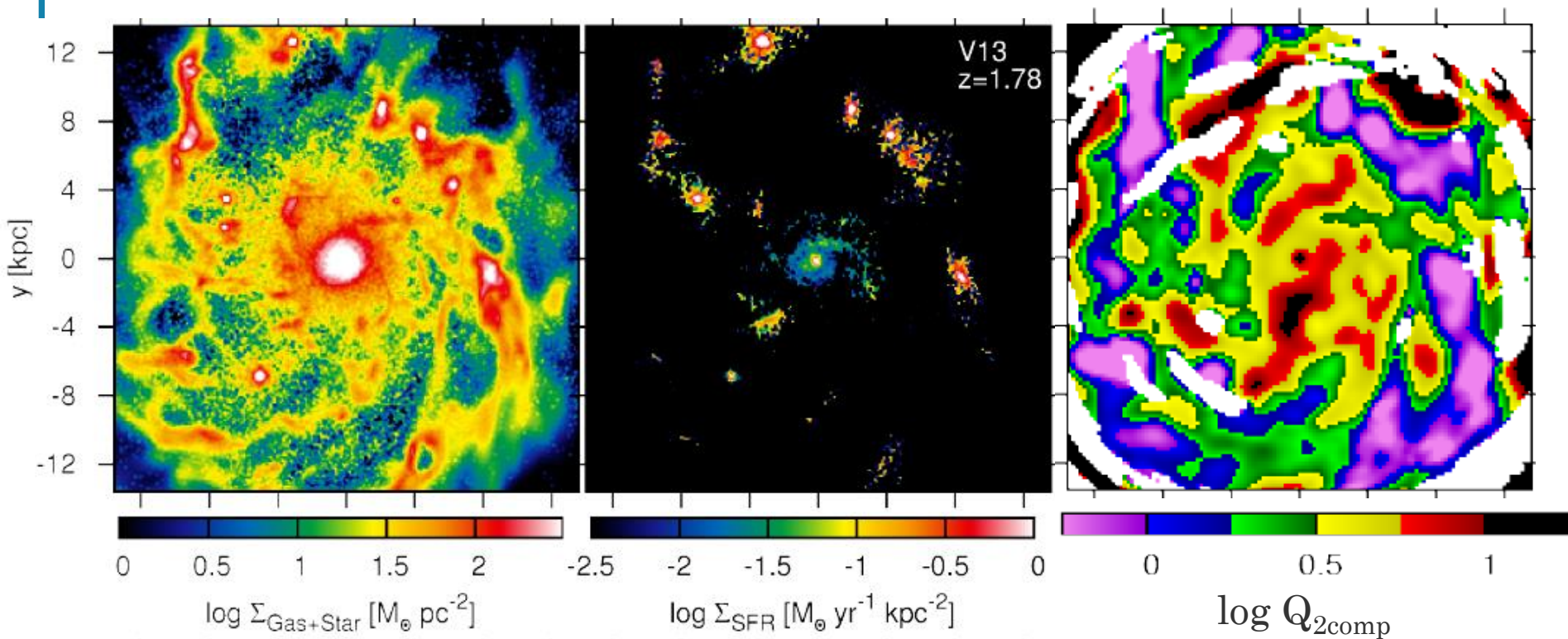


# Cosmological simulations

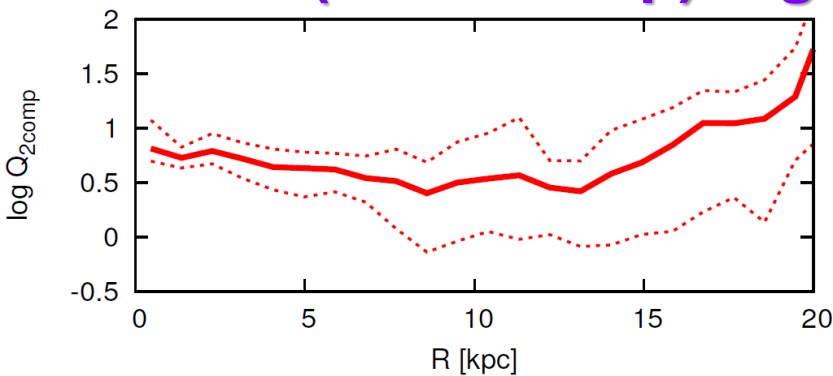
- V13

- $z = 1.78$
- $M_{vir} = 3.4 \times 10^{11} M_{\odot}$
- $M_{star} = 1.2 \times 10^{10} M_{\odot}$
- $f_{gas} = 0.40$
- $B/T = 0.46$  (kinematic)
- $SFR = 11.2 M_{\odot} \text{ yr}^{-1}$





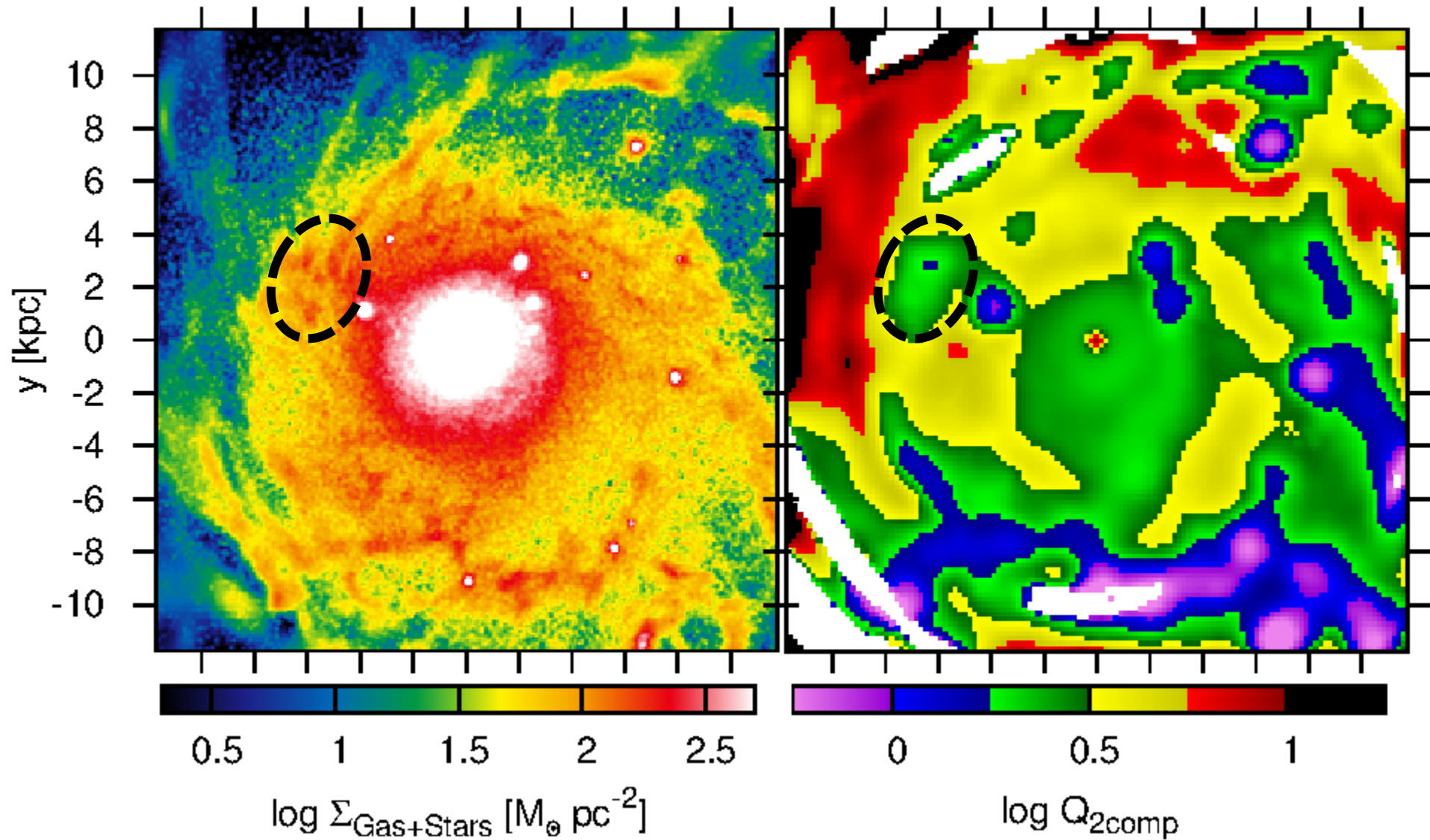
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# Non-linear formation of clumps

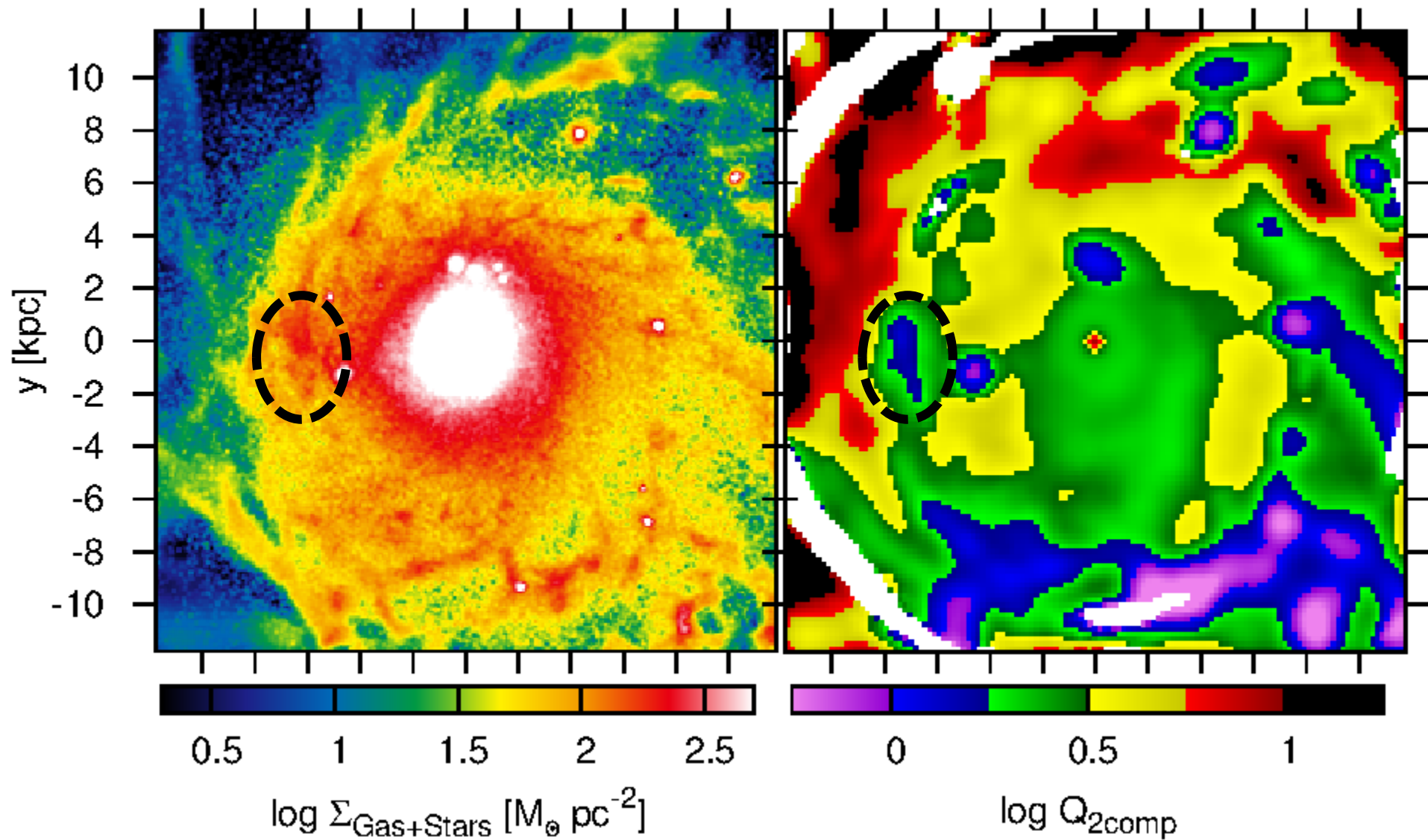
V07  $a=0.3384$





# Non-linear formation of clumps

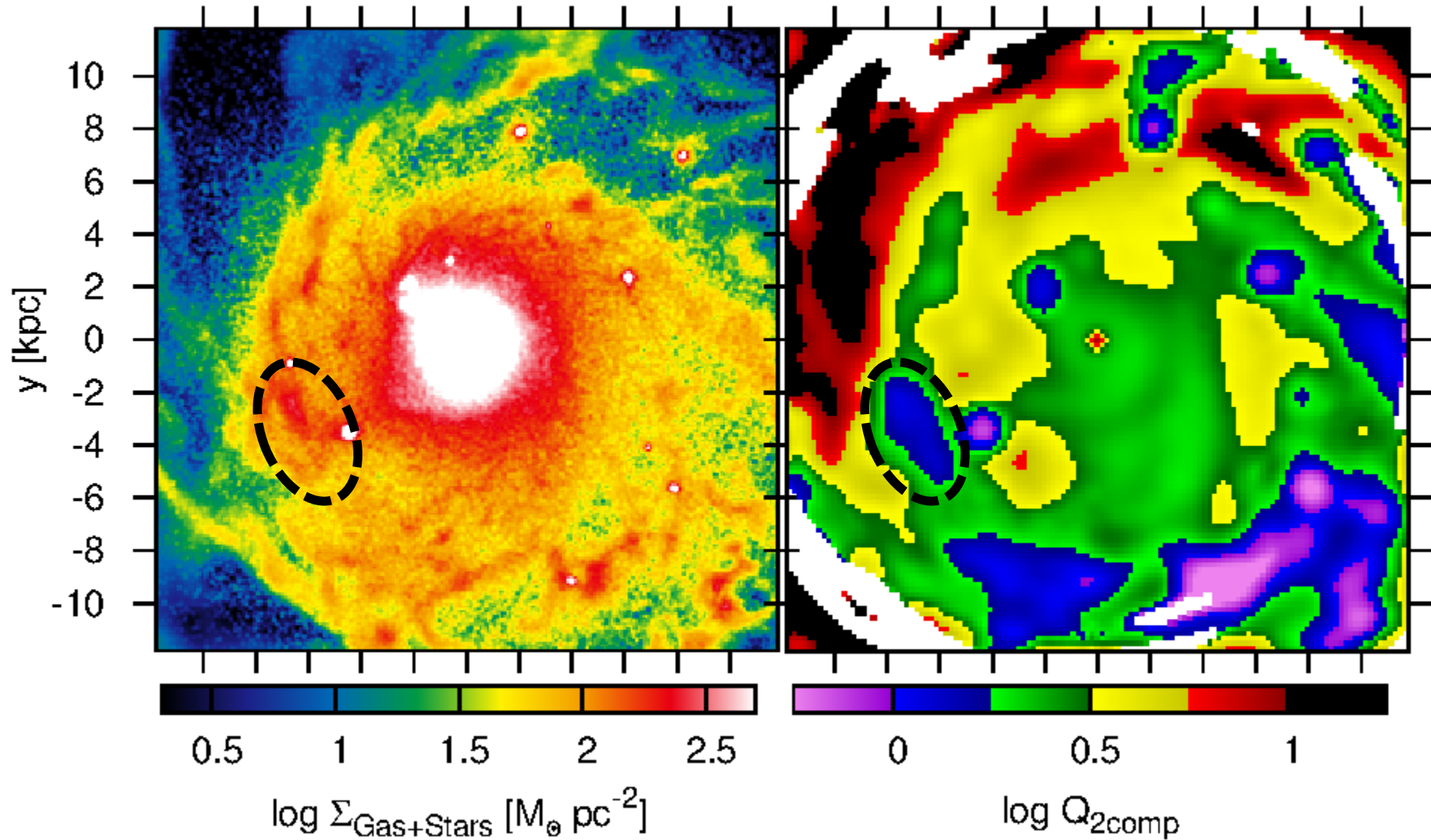
V07 a=0.3389





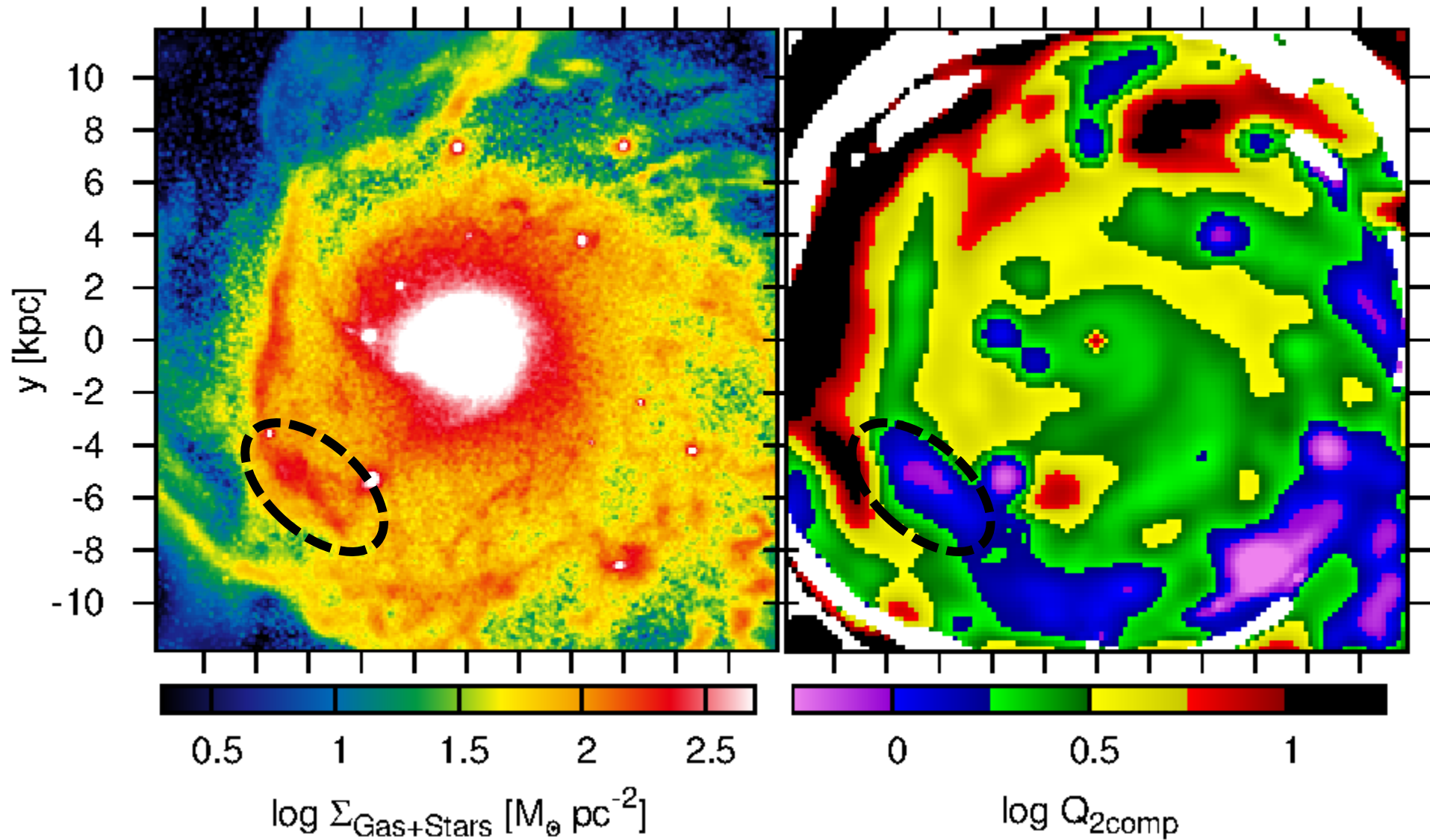
# Non-linear formation of clumps

V07 a=0.3394



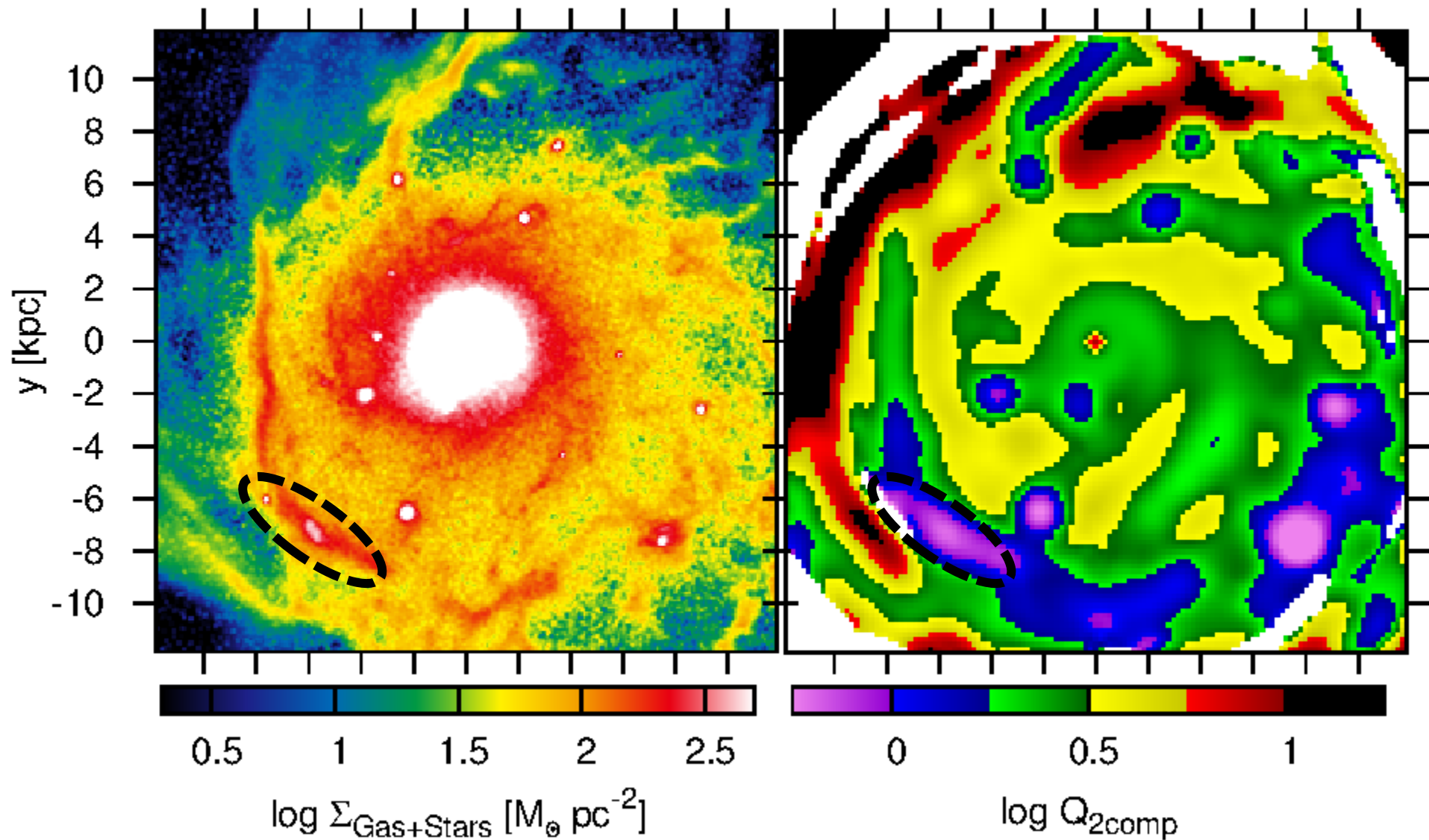
# Non-linear formation of clumps

V07 a=0.3400



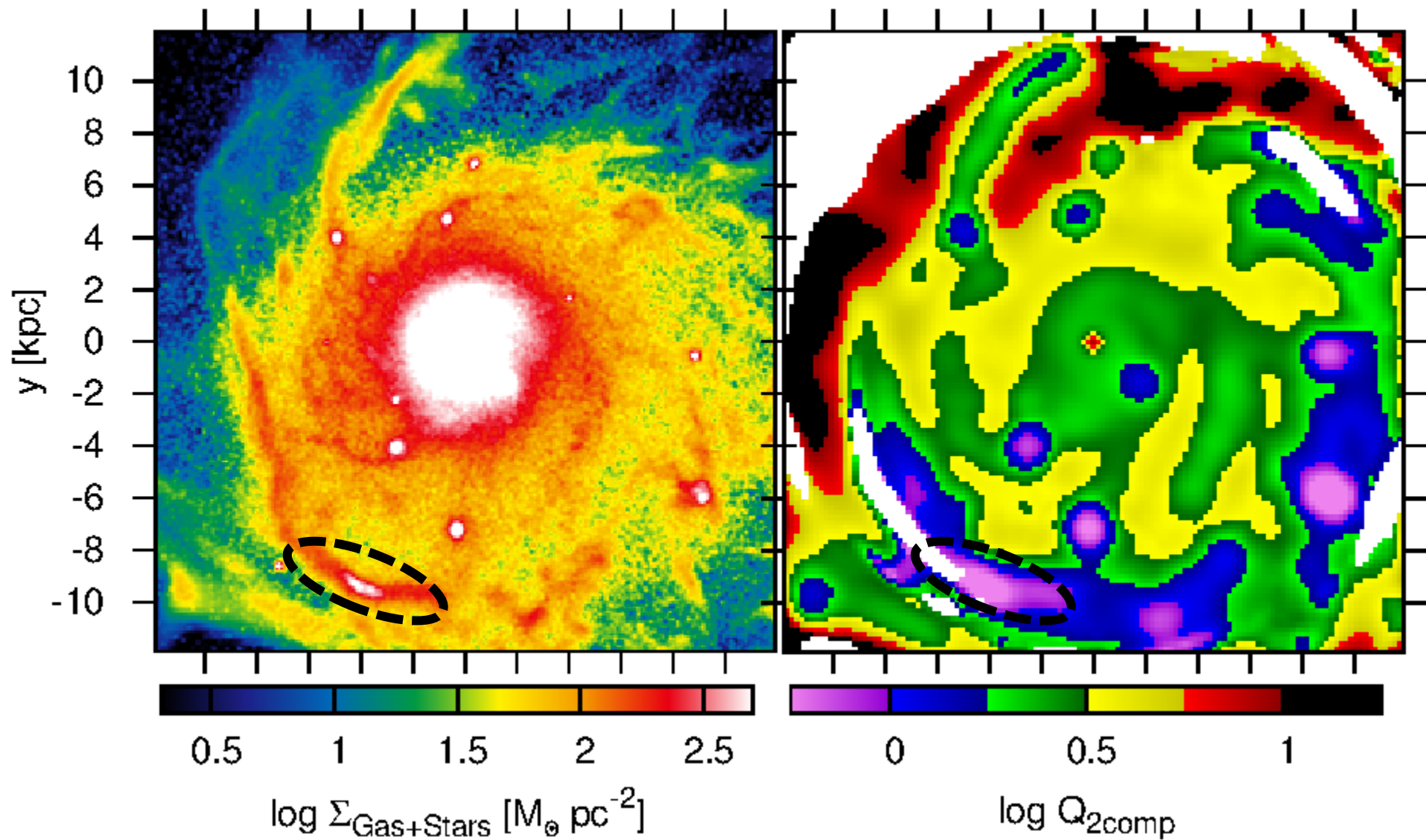
# Non-linear formation of clumps

V07 a=0.3405



# Non-linear formation of clumps

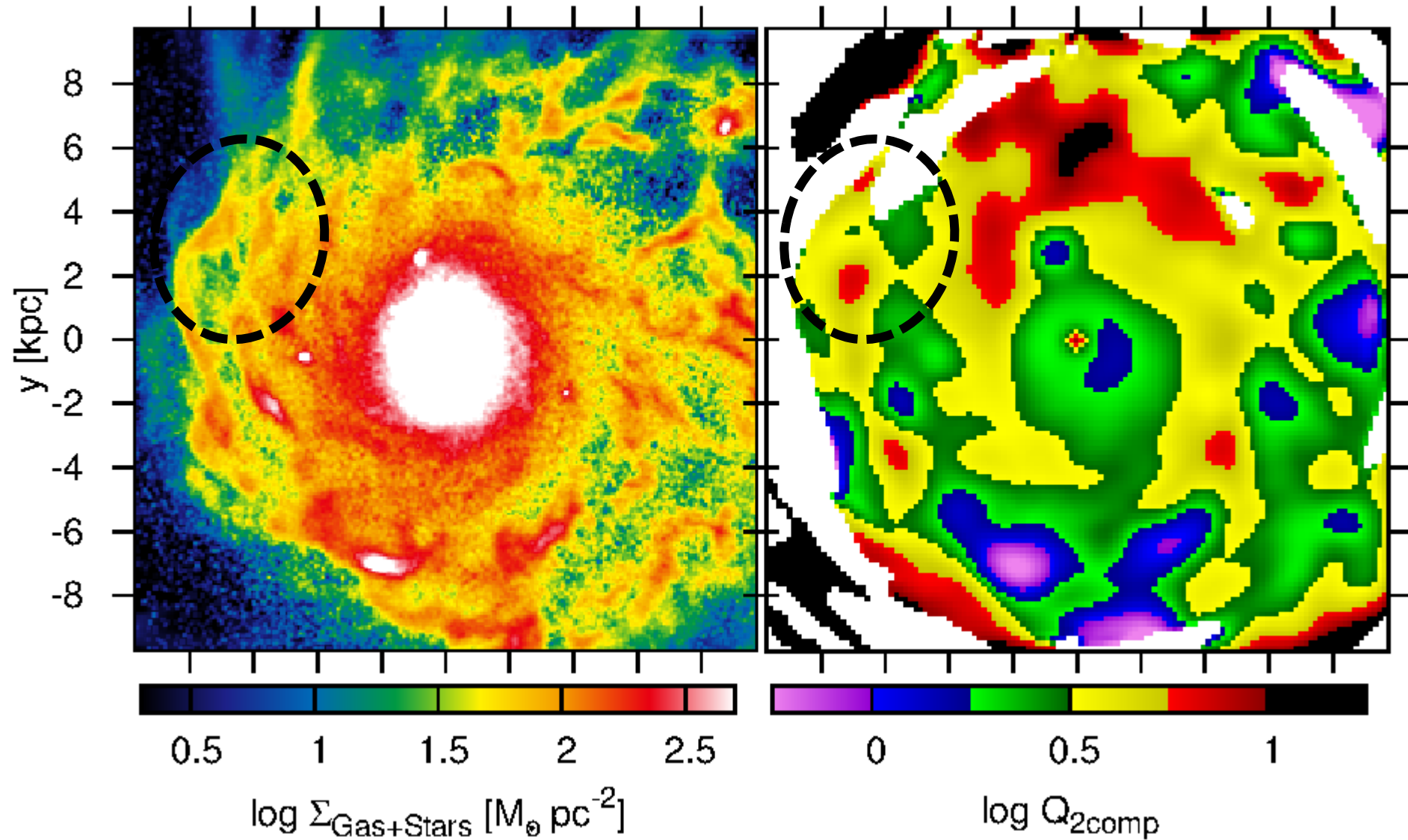
V07 a=0.3411





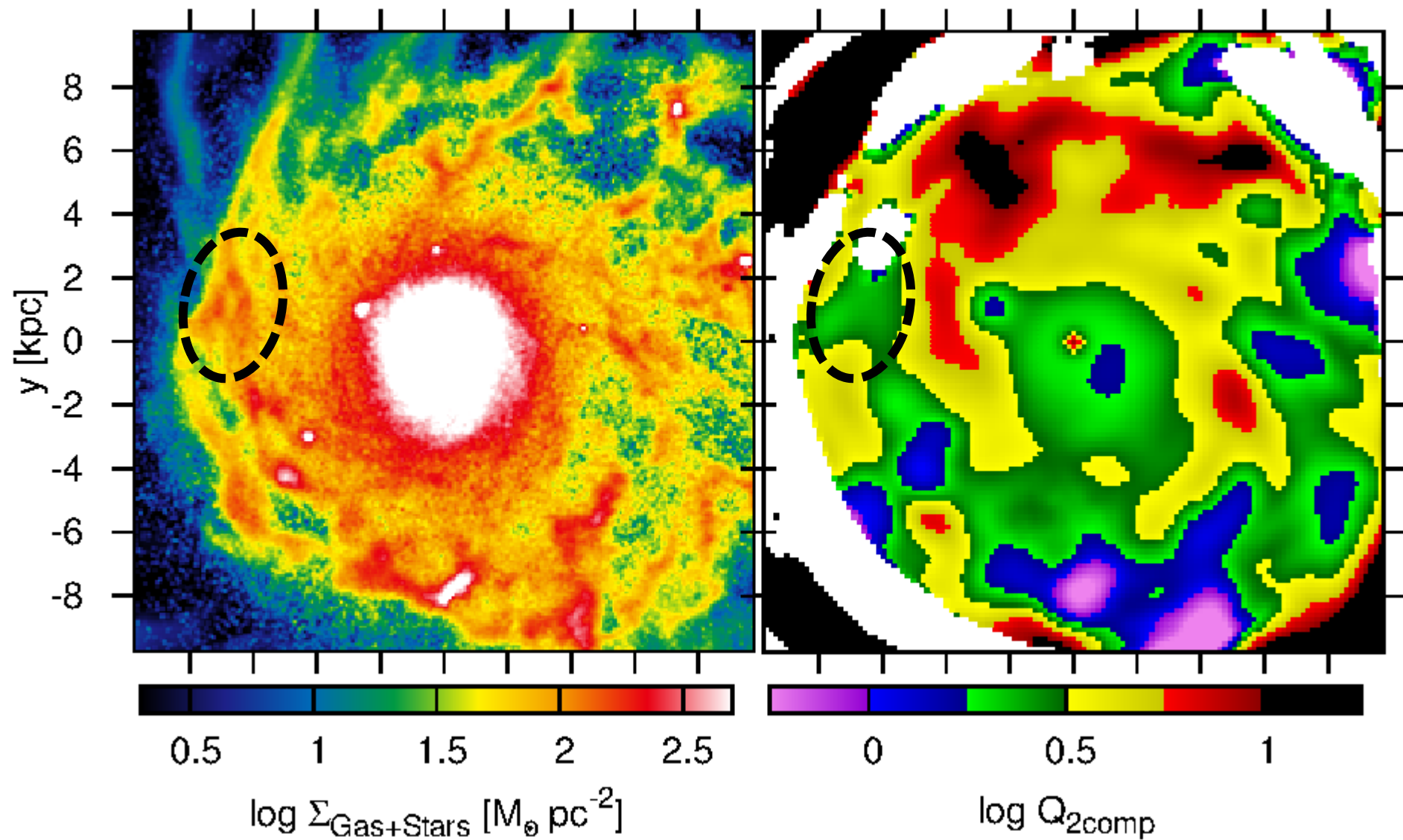
# Non-linear formation of clumps

V07 a=0.2866



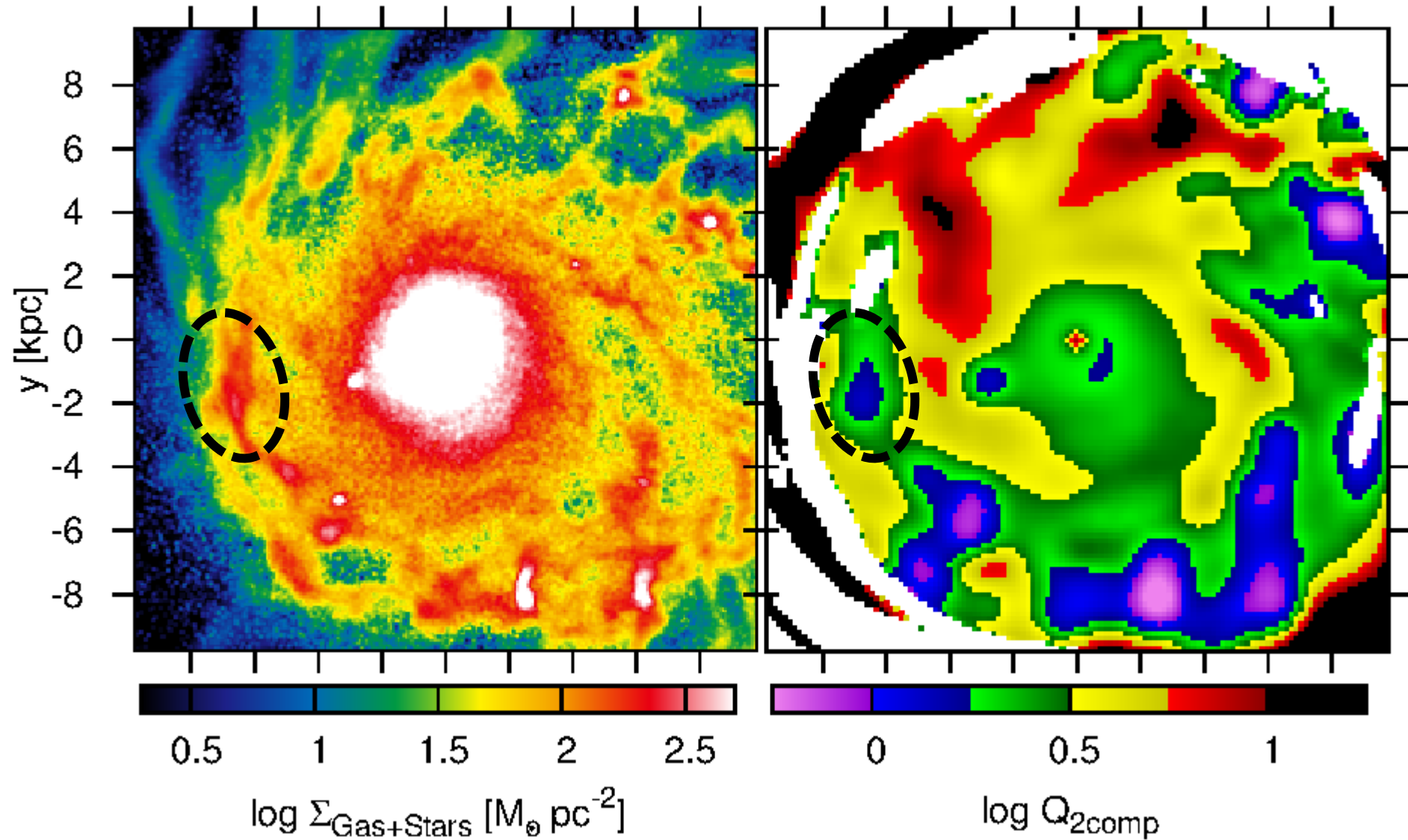
# Non-linear formation of clumps

V07 a=0.2872



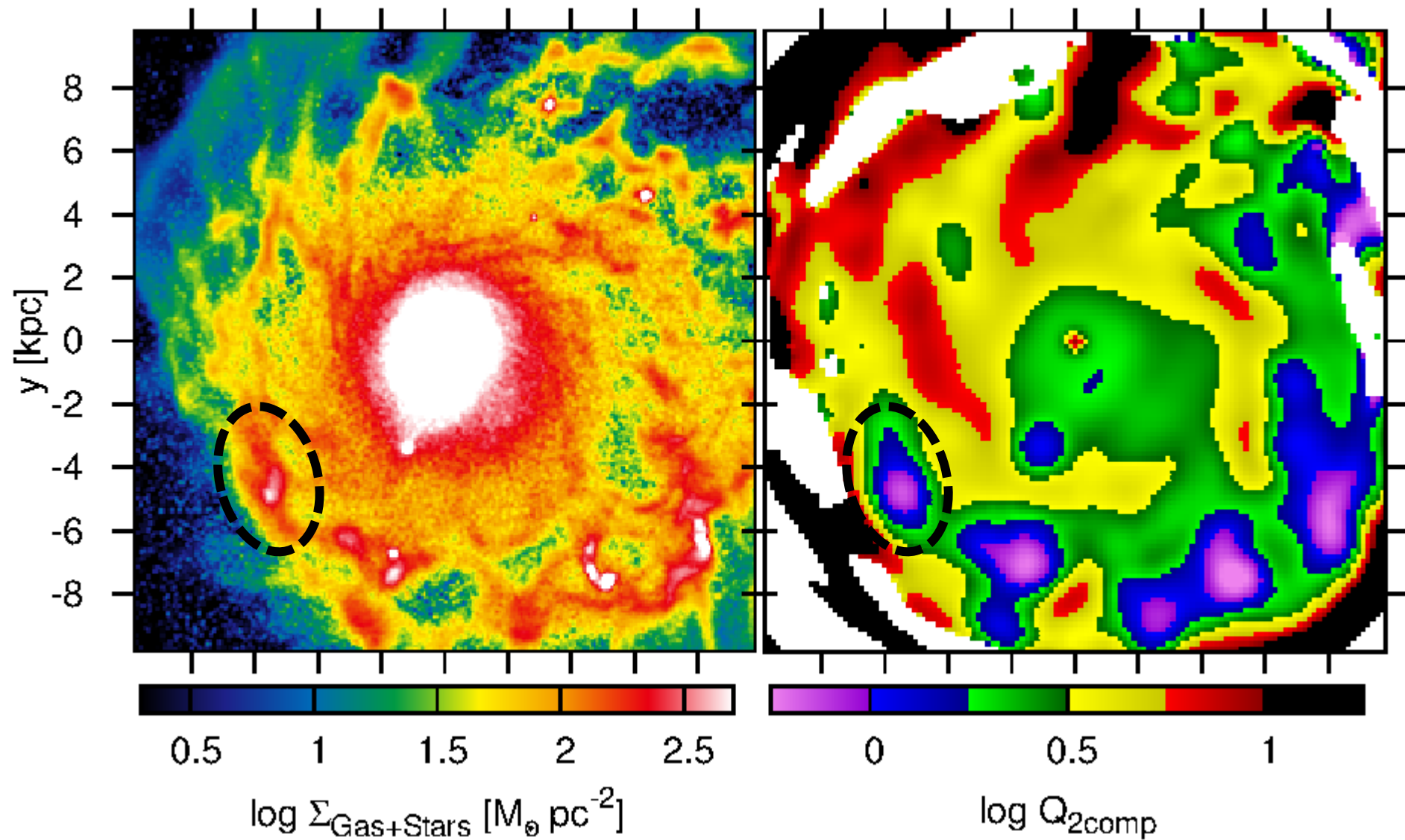
# Non-linear formation of clumps

V07 a=0.2878



# Non-linear formation of clumps

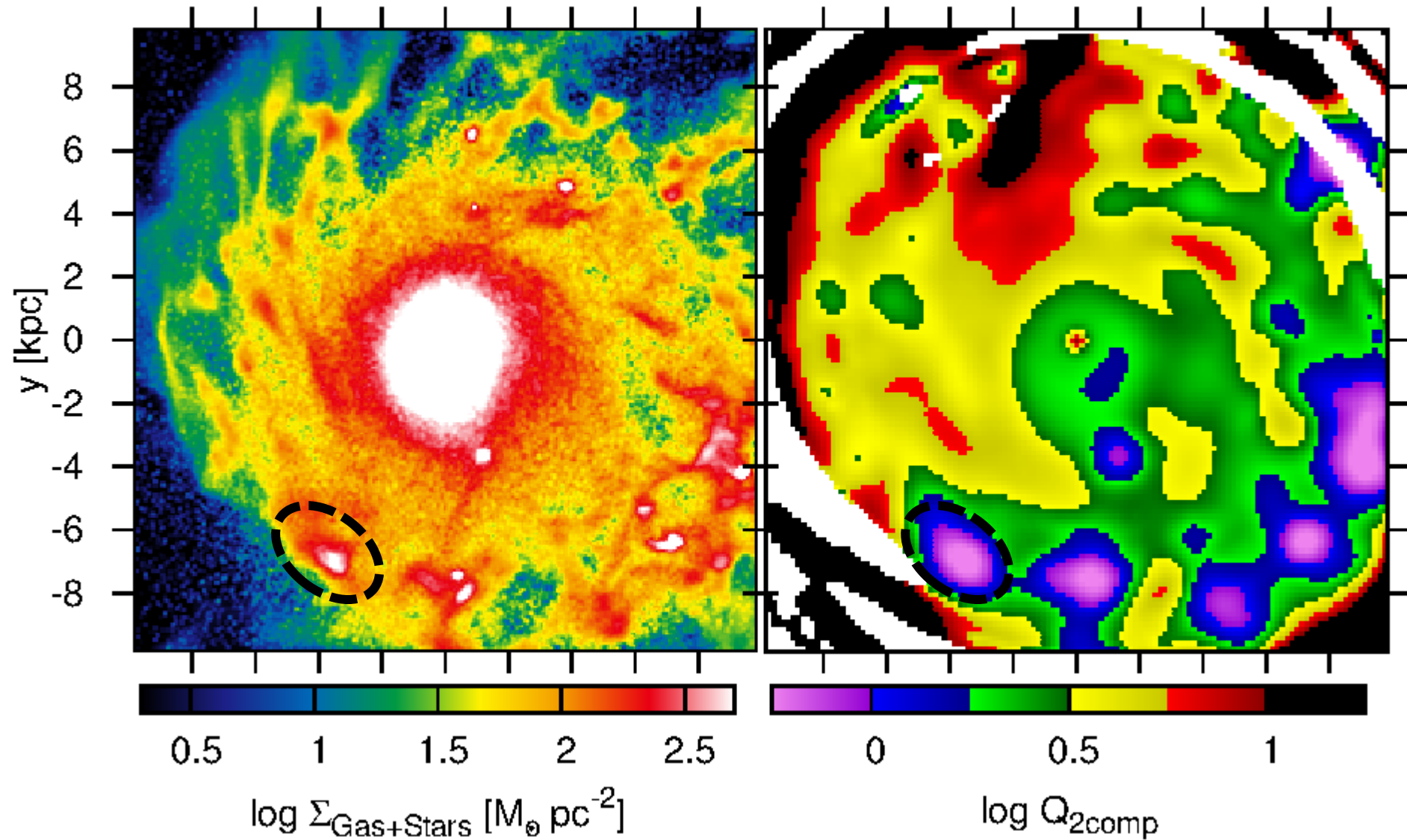
V07 a=0.2885





# Non-linear formation of clumps

V07 a=0.2892

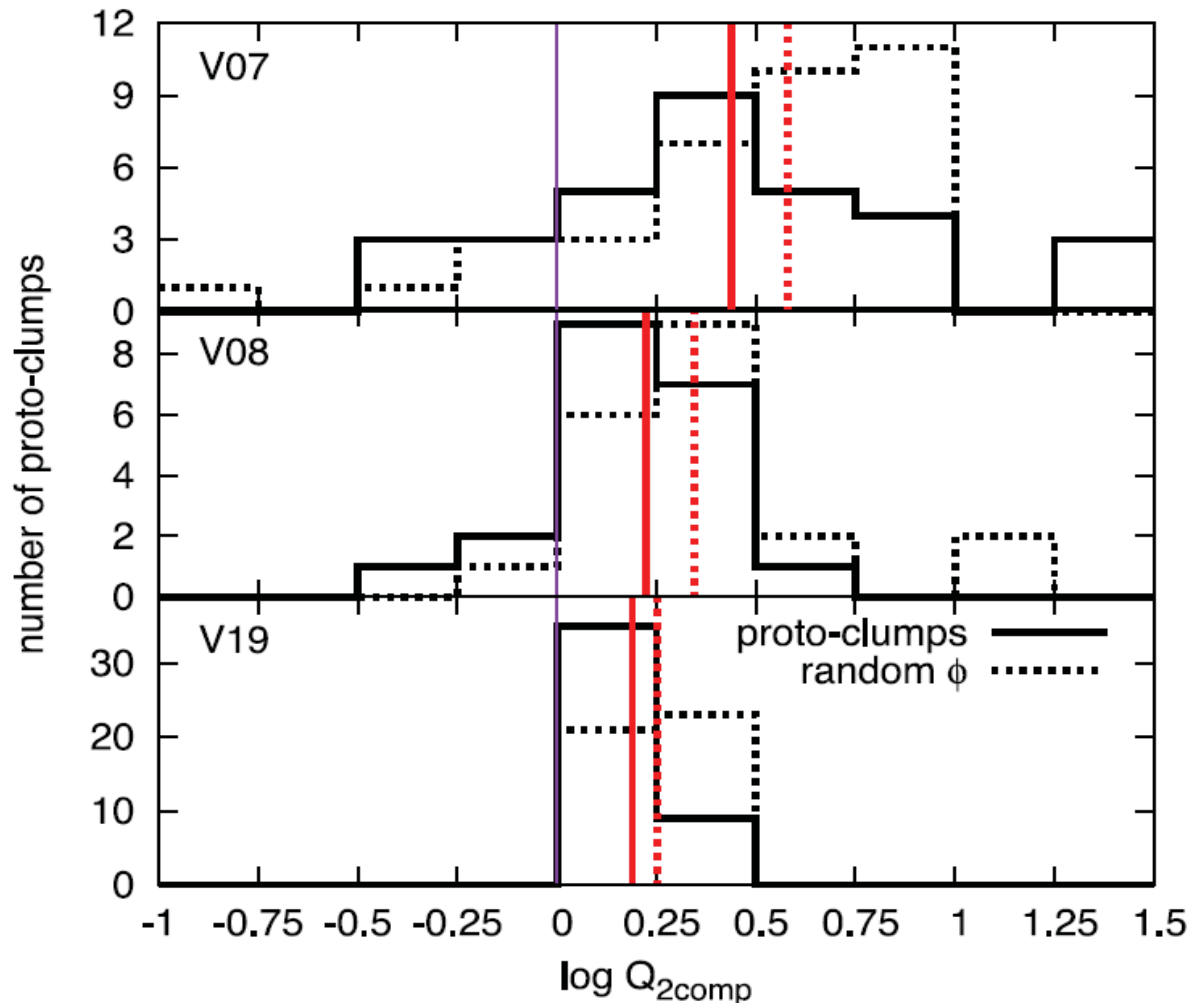


# Non-linear formation of clumps

- Distributions of  $Q$  on proto-clumps.
  - The initial masses  $M_{\text{clump}} > 10^8 M_{\odot}$

Clump detection scheme  
(Mandelker+ 2014)

We trace clumps back in  
time and space, and then  
we look into proto-clumps  
which are detected for  
the first time.

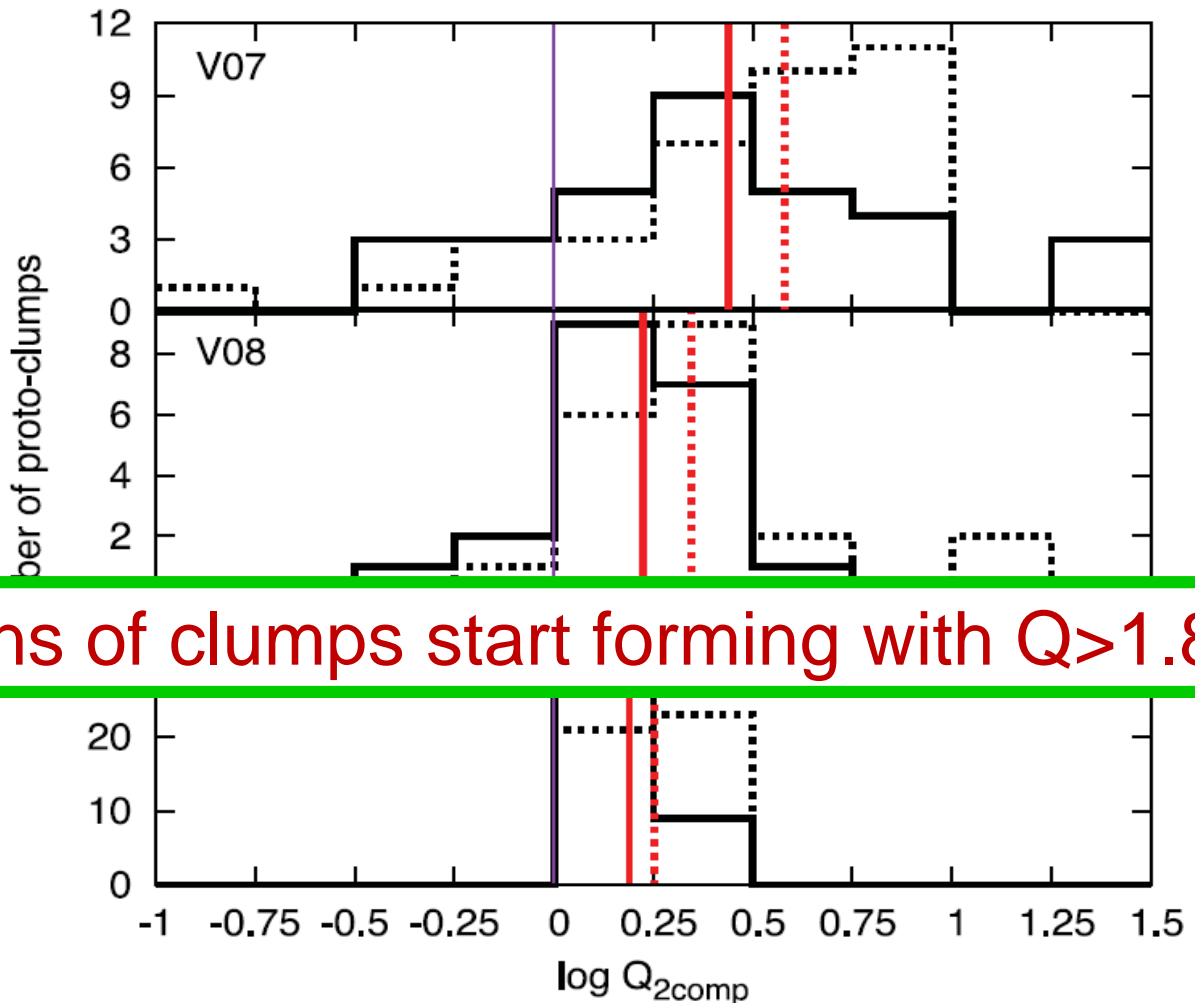


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Clump detection scheme  
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Significant fractions of clumps start forming with  $Q > 1.8$

# How do giant clumps form?

- Non-perturbative scenarios

- **Gas dissipation**

- $Q_{crit} = 2 - 3$  if gas cooling is rapid. (*Elmegreen 2011*)



# How do giant clumps form?

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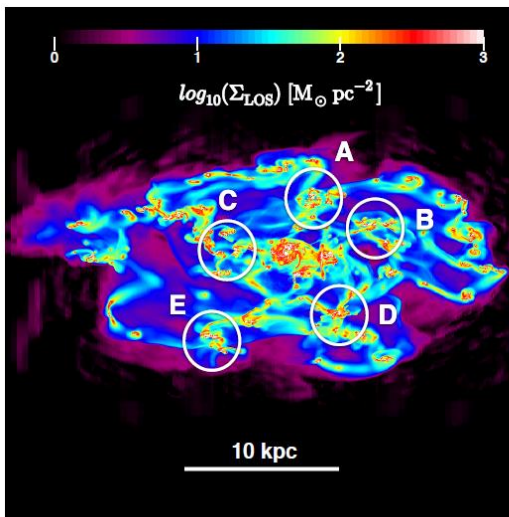
- $Q_{crit} = 2 - 3$  if gas cooling is rapid. (*Elmegreen 2011*)

- **Small-scale formation and merger/accretion growth**

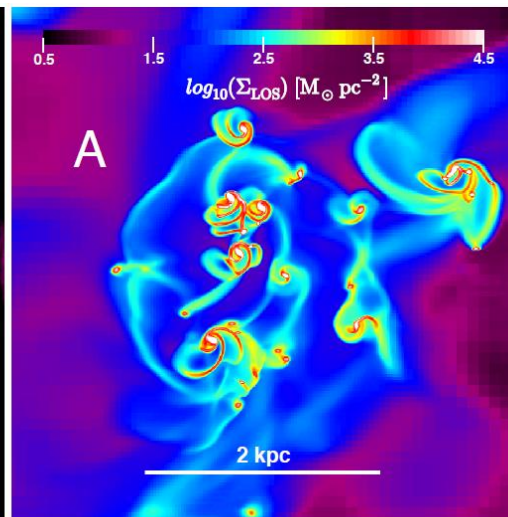
- $Q$  can be  $<1$  on small scales (*e.g. Romeo et al 2010*)

- $Q$ -measurement can depend on physical scales, e.g. Larson law

- We applied the Gaussian smoothing with FWHM=1.2 kpc



(a) Gas surface density



(b) Zoom onto cluster A

A giant clump may form by mergers of small clumps. (Behrendt et al. 2015)

# How do giant clumps form?

- Non-perturbative scenarios

- **Gas dissipation**

- $Q_{crit} = 2 - 3$  if gas cooling is rapid. (*Elmegreen 2011*)

- **Small-scale formation and merger/accretion growth**

- $Q$  can be  $< 1$  on small scales (*e.g. Romeo et al 2010*)

- **Non-axisymmetric perturbation**

- $m \neq 0$  perturbations (*Griv & Gedalin 2012*)

- unstable up to  $Q \cong 2$  for finite thickness.

# How do giant clumps form?

- Perturbative scenarios

- **Minor mergers**

- Satellite accretion can disturb a disc.

- **Pre-existing clumps**

- Clumps also disturb a disc and stimulate formation of other clumps.

- **Cold stream flowing in a disc**

- Streams can join a disc with slow or counter rotation.
  - Slow rotation leads to low  $\kappa$

# How do giant clumps form?

- Perturbative scenarios

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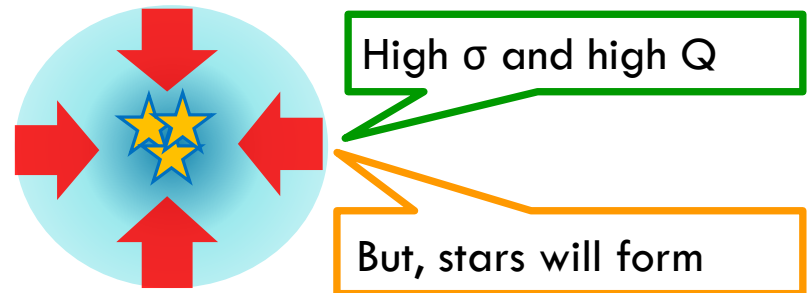
- Clumps also disturb a disc and stimulate formation of other clumps.

- **Cold stream flowing in a disc**

- Streams can join a disc with slow or counter rotation.

- **Compressive turbulence**

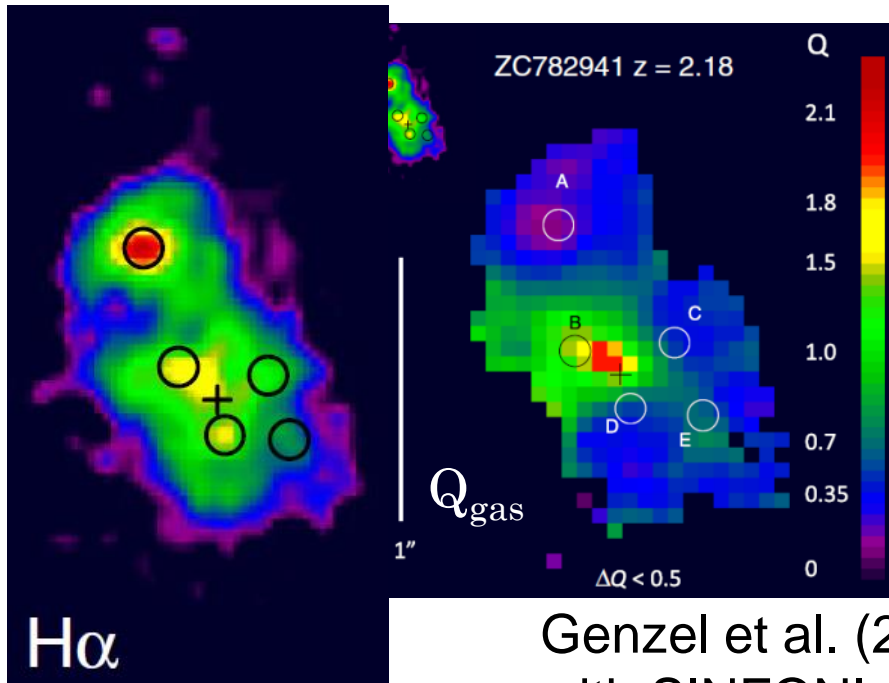
- Compressing gas can indicate a high  $\sigma$  (i.e. high  $Q$ )
  - But a clump will form there



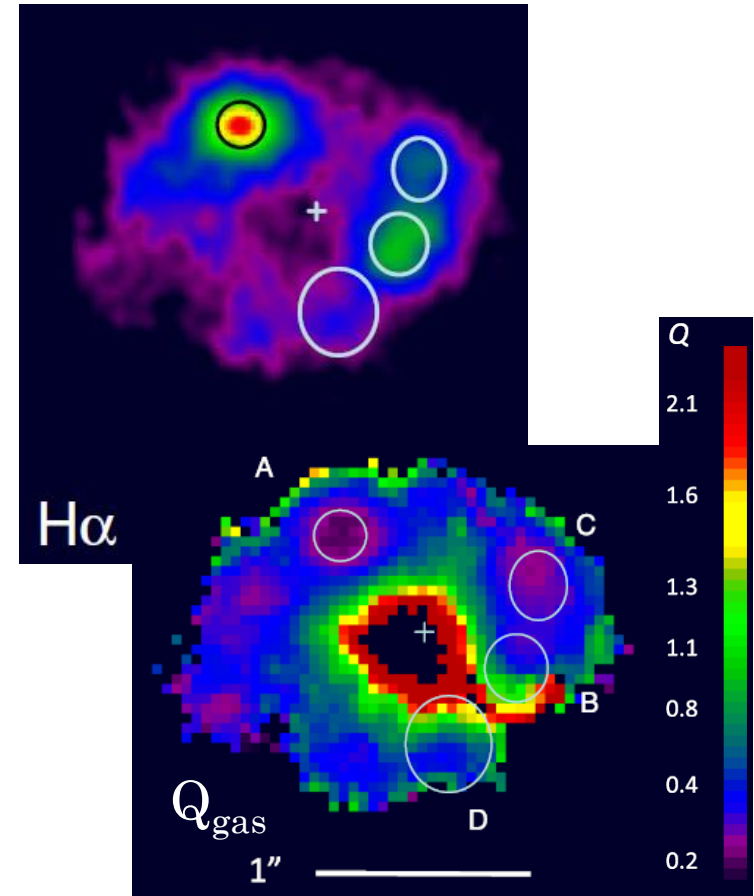


# Toomre instability

- In observations,



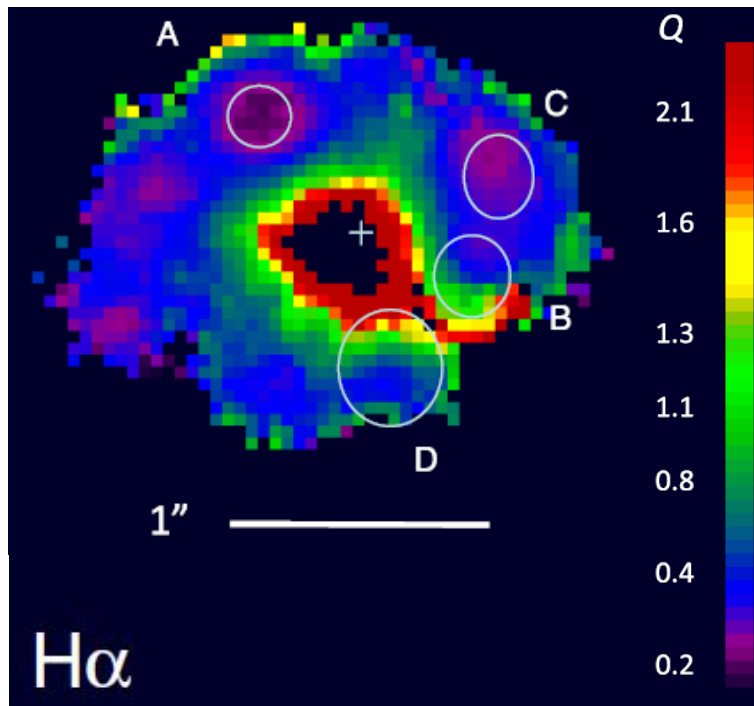
Genzel et al. (2011)  
with SINFONI



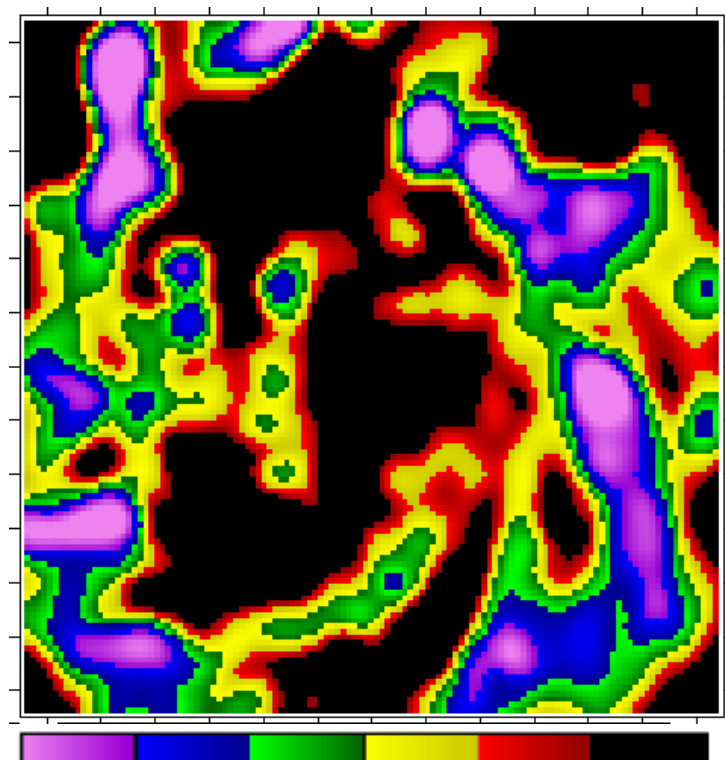
$Q \leq 1$  in the observations.  
 $Q > 1$  in our simulations.

# Obs. vs. sims.

- Toomre  $Q$  of gas component.
- **$Q \leq 1$  in the observations.**



Genzel et al. (2011)

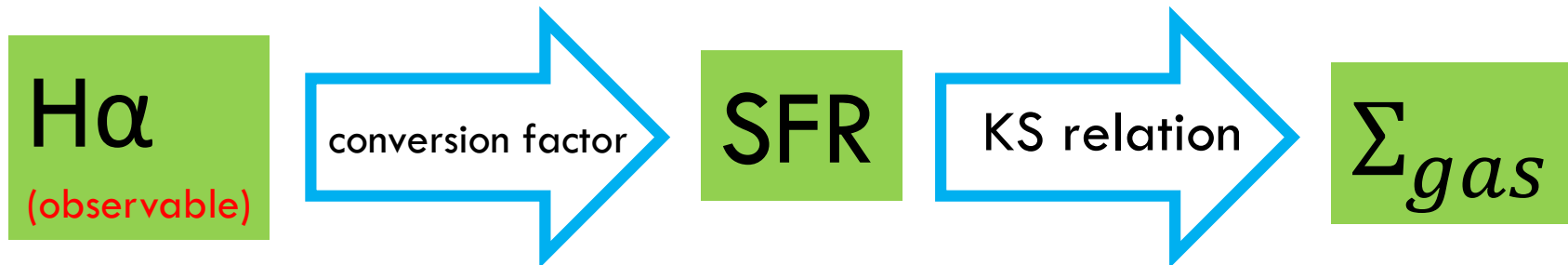


**$\sim 3-5$  times lower in the obs.**

$\log Q_{\text{Gas}}$

# Obs. vs. sims.

- Toomre  $Q$  of gas component.
- **$Q \leq 1$  in the observations.**
- The observation might be underestimating  $Q$ .
  - Perhaps, it might be due to overestimation of gas density.
    - **The gas density in obs. is measured from H $\alpha$  luminosity.**



- e.g.
  - KS relation may be different in high- $z$  galaxies...?
  - Star-formation efficiency may be higher in high- $z$  galaxies...?

# Summary

- $Q > 2-3$  in disc (inter-clump) regions,
- $Q < 1$  inside/around giant clumps.
- Formation of new clumps can start with  $Q > 2-3$ .

• **Clump formation is NOT NECESSARILY due to the (standard) Toomre instability.**

- Maybe induced by other mechanisms.
  - minor mergers, pre-existing clumps, cold streams, etc..

- There is tension between our sims and IFS obs.
  - Gas density may be overestimated in IFS?

**Transition of giant clump formation  
mechanisms at  $z \sim 2$ :  
from Toomre to spiral-arm instabilities**

***Beyond Toomre's  $Q$***

**MNRAS in press  
arXiv: 1706.01895**

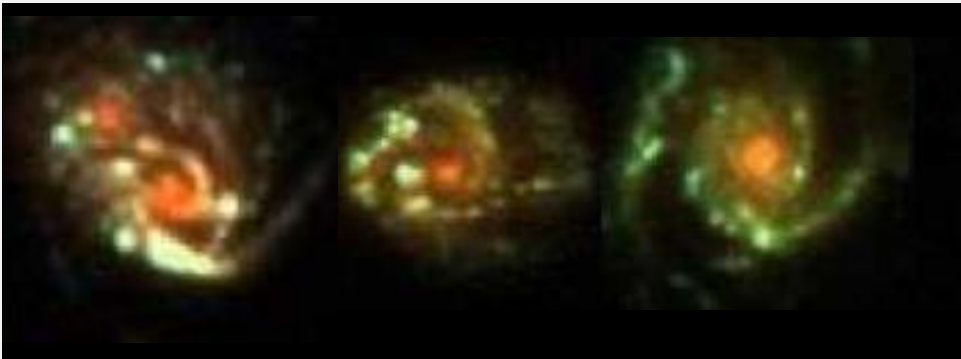
Shigeaki Inoue (Kavli IPMU / U Tokyo)

w/ Naoki Yoshida, Takatoshi Shibuya



# Spiral or Clumpy?

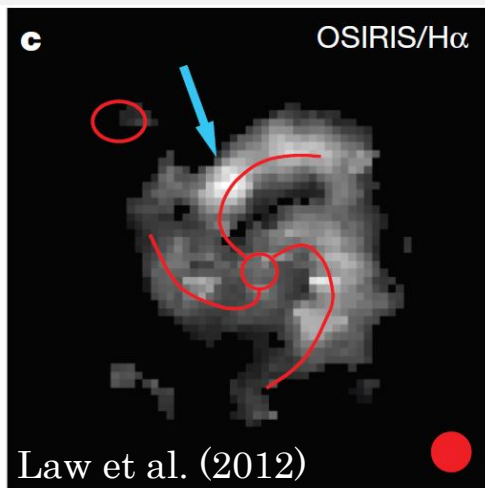
- Clumpy galaxies
  - **Giant clumps**
  - Gas-rich ( $f_{\text{gas}} > 30\%$ )



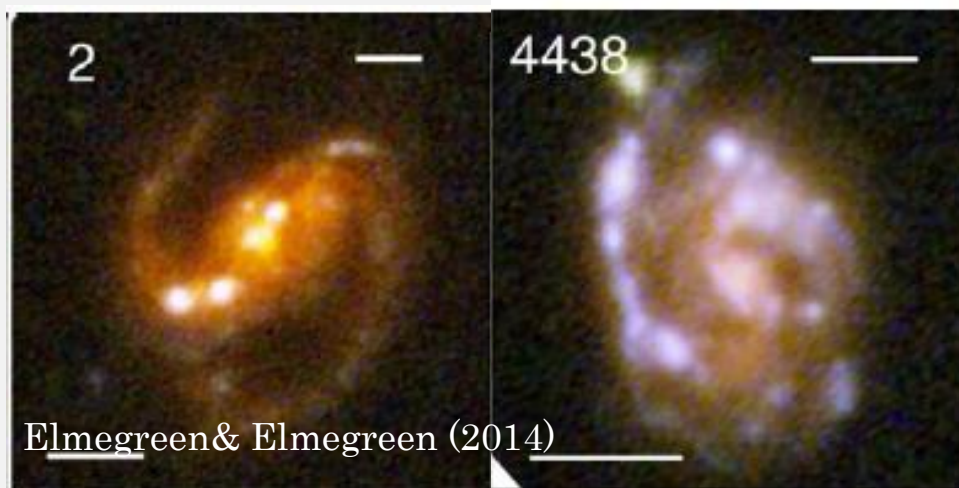
Guo et al. (2014)

## Spiral-arm fragmentation?

Spiral galaxies emerge at  $z < 2$  (Elmegreen+14)



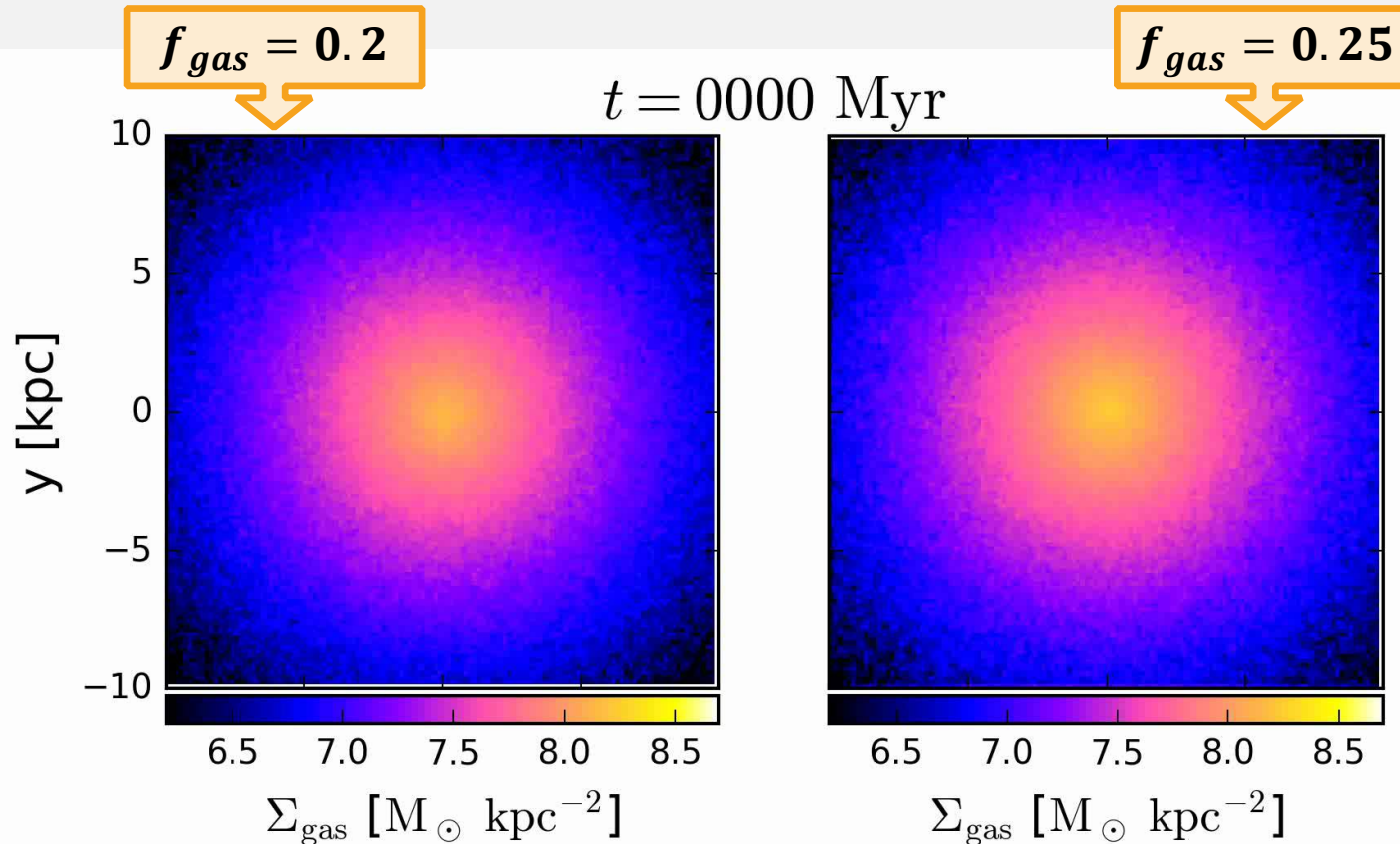
Law et al. (2012)



Elmegreen & Elmegreen (2014)

# Spiral or Clumpy?

- Isolated disc galaxy simulations
  - Gas + stellar discs
  - Isothermal gas (no star formation, no feedback)
  - Moving-mesh code: Arepo



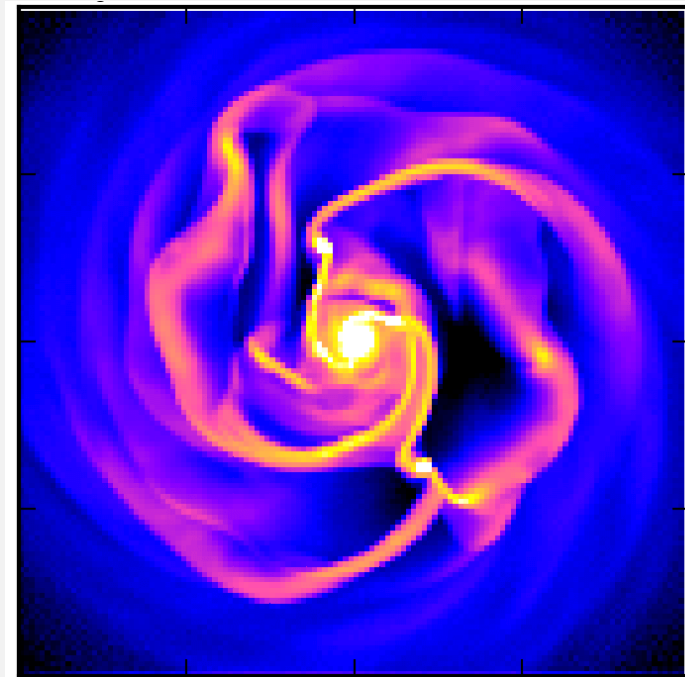
# Spiral-arm fragmentation as a clump formation mechanism

- Spiral arms can fragment into clumps,
  - if the gas fraction is high and/or the disc is kinematically cold.
- **Spiral-arm fragmentation is not Toomre instability!**
- Spiral-arm fragmentation could be a possible mechanism of giant clump formation.

## ***Beyond Toomre's $Q$***

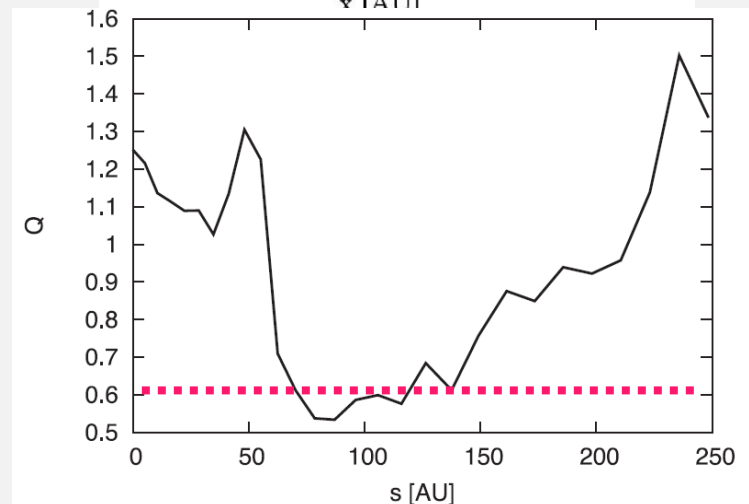
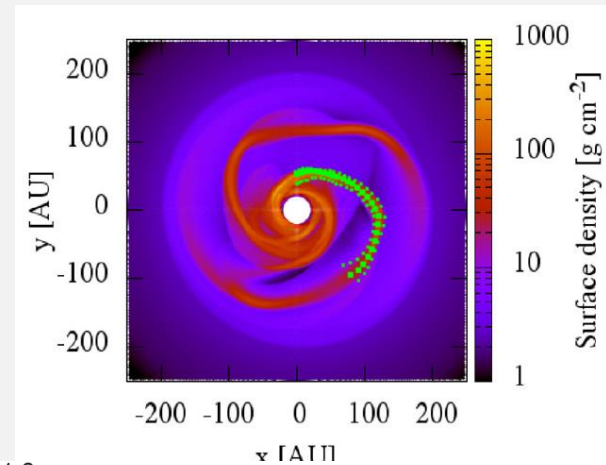
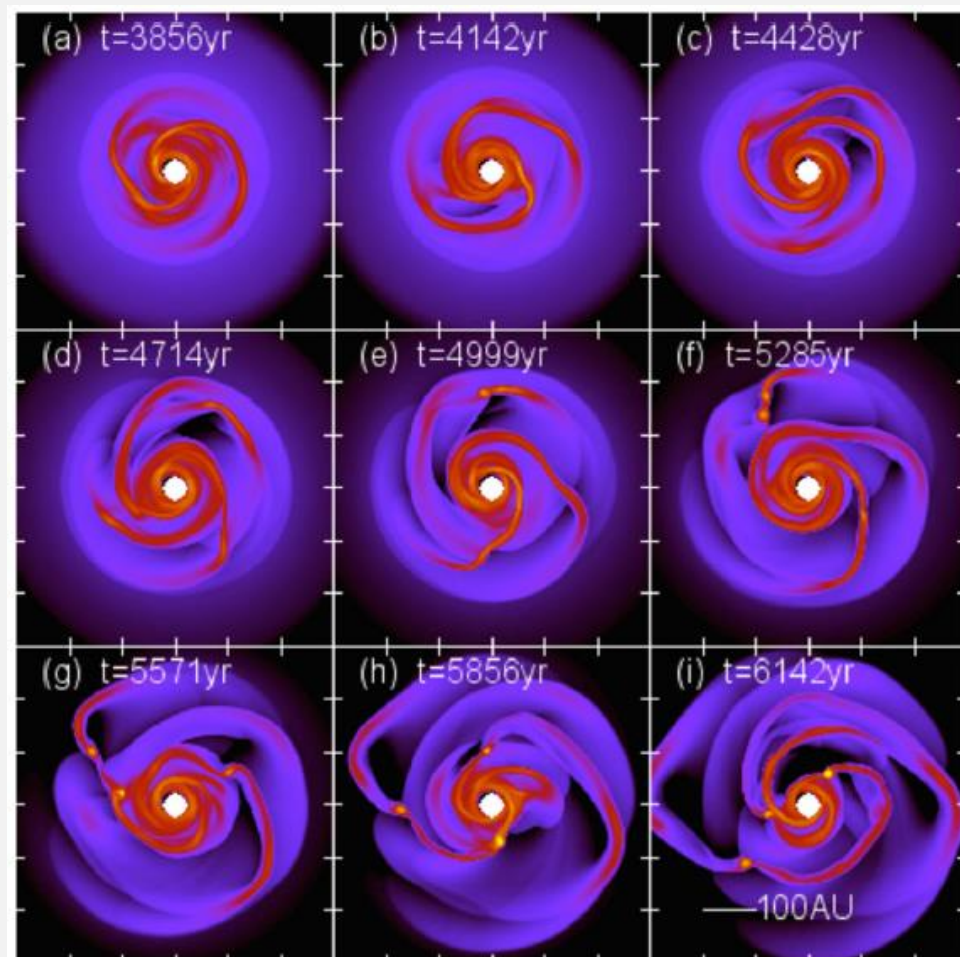
- The aims of this study:
  - How spiral-arm fragmentation occurs?
    - Derive **an instability parameter and its criterion**

***linear perturbation theory for a spiral arm***



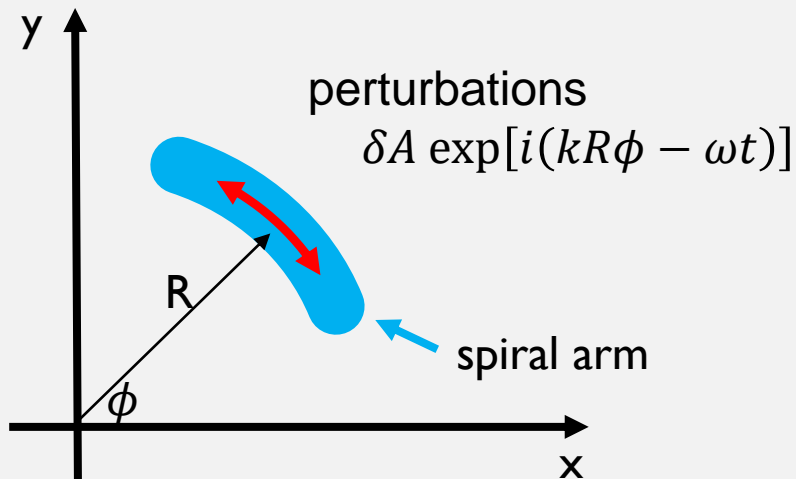
# Takahashi, Tsukamoto & Inutsuka (2016)

- Proto-planetary discs
- Spiral-arm fragmentation takes place only if  $Q < 0.6$  on the spiral arm.
- **Their linear perturbation analysis also supports this criterion.**



# Set-up for the linear perturbation theory

- Now considering...
  - Gravitational instability for **azimuthal** perturbations on an **axisymmetric** spiral (ring).



Assuming:

- The spiral has **a rigid rotation** since self-gravitating.

$$\Omega = -B$$

- Replace surface density  $\Sigma$  with line-mass  $\Upsilon = 1.4W\Sigma$  (**Gaussian**).

continuity: 
$$\frac{\partial}{\partial t} \delta\Sigma + \frac{1}{R} \frac{\partial}{\partial R} (R\Sigma_0 \delta v_R) + \Omega \frac{\partial}{\partial \phi} \delta\Sigma + \frac{\Sigma_0}{R} \frac{\partial}{\partial \phi} \delta v_\phi = 0,$$

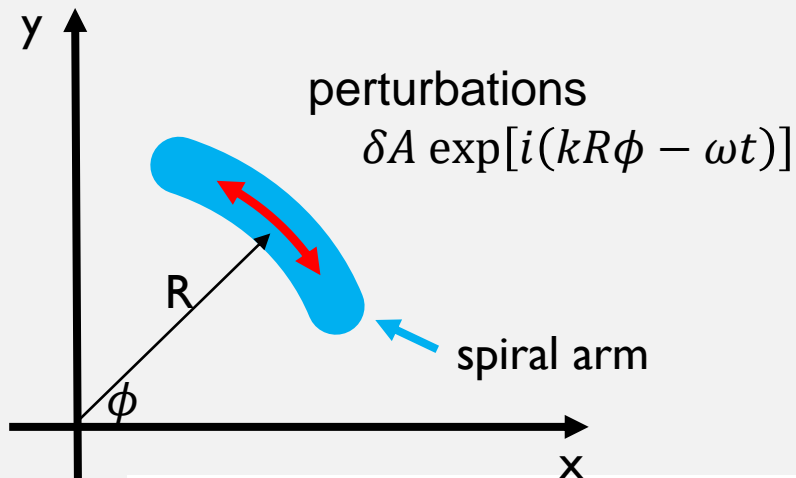
R-momentum: 
$$\frac{\partial}{\partial t} \delta v_R + v_R \frac{\partial}{\partial R} \delta v_R + \Omega \frac{\partial}{\partial \phi} \delta v_R - 2\Omega \delta v_\phi = -\frac{\partial}{\partial R} \left( c_s^2 \frac{\delta\Sigma}{\Sigma_0} + \delta\Phi \right),$$

$\phi$ -momentum: 
$$\frac{\partial}{\partial t} \delta v_\phi + v_R \frac{\partial}{\partial R} \delta v_\phi + \Omega \frac{\partial}{\partial \phi} \delta v_\phi - 2B \delta v_R = -\frac{1}{R} \frac{\partial}{\partial \phi} \left( c_s^2 \frac{\delta\Sigma}{\Sigma_0} + \delta\Phi \right).$$



# Set-up for the linear perturbation theory

- Now considering...
  - Gravitational instability for **azimuthal** perturbations on an **axisymmetric** spiral (ring).



Assuming:

- The spiral has **a rigid rotation** since self-gravitating.

$$\Omega = -B$$

- Replace surface density  $\Sigma$  with line-mass  $\Upsilon = 1.4W\Sigma$  (**Gaussian**).

continuity:  $\omega \delta \Upsilon = k \Upsilon \delta v_\phi,$

R-momentum:  $-i\omega \delta v_R = 2\Omega \delta v_\phi,$

$\phi$ -momentum:  $-i\omega \delta v_\phi = -2\Omega \delta v_R - ik \frac{c_s^2}{\Upsilon} \delta \Upsilon - ik \delta \Phi.$

# A dispersion relation for a single-component model

- One can obtain the dispersion relation for the perturbations,

$$\omega^2 = \left( c_s^2 + \frac{\Upsilon}{\delta\Upsilon} \delta\Phi \right) k^2 + 4\Omega^2.$$

- The Poisson equation for the perturbations is

$$\delta\Phi = \int_{-W}^W -G\delta\Upsilon K_0(|kx|)/W dx$$

$$= -\pi G\delta\Upsilon \left[ \underline{K_0(kW)L_{-1}(kW) + K_1(kW)L_0(kW)} \right]$$

$f(kW)$

$W$  : half width of arm

$K$  : Bessel function

$L$  : Struve function

# A dispersion relation for a single-component model

- One can obtain the dispersion relation for the perturbations,

$$\omega^2 = (c_s^2 - \pi G f(kW) \Upsilon) k^2 + 4\Omega^2.$$

(cf. Takahashi, Tsukamoto & Inutsuka 2016)

- This can be transformed as

$$\frac{c_s^2 k^2 + 4\Omega^2 - \omega^2}{\pi G f(kW) \Upsilon k^2} = 1.$$

- When  $\omega^2 < 0$ , the spiral is unstable.
- Considering this in the boundary case  $\omega^2 = 0$ , the new instability parameter and its criterion can be defined as

$$S \equiv \frac{c_s^2 k^2 + 4\Omega^2}{\pi G f(kW) \Upsilon k^2} < 1.$$

# A dispersion relation for a two-component model

- A galaxy usually has gas and stars. The dispersion relations of gas and stars are,

$$\text{gas: } \omega^2 = \left( c_s^2 + \frac{\Upsilon_g}{\delta\Upsilon_g} \delta\Phi \right) k^2 + 4\Omega^2, \quad \delta\Upsilon_g = k^2 \frac{\Upsilon_g}{\omega^2 - 4\Omega^2 - c_s^2 k^2} \delta\Phi,$$

$$\text{stars: } \omega^2 = \left( \sigma_\phi^2 + \frac{\Upsilon_s}{\delta\Upsilon_s} \delta\Phi \right) k^2 + 4\Omega^2, \quad \delta\Upsilon_s = k^2 \frac{\Upsilon_s}{\omega^2 - 4\Omega^2 - \sigma_\phi^2 k^2} \delta\Phi,$$

- Because gas and stars interact only through gravity, they are connected in the Poisson eq.,

$$\delta\Phi = -\pi G [\delta\Upsilon_g f(kW_g) + \delta\Upsilon_s f(kW_s)]$$

- Then, one can obtain the two-component dispersion relation,

$$\left[ \frac{\pi G k^2 \Upsilon_g f(kW_g)}{c_s^2 k^2 + 4\Omega^2 - \omega^2} + \frac{\pi G k^2 \Upsilon_s f(kW_s)}{\sigma_\phi^2 k^2 + 4\Omega^2 - \omega^2} \right] = 1,$$

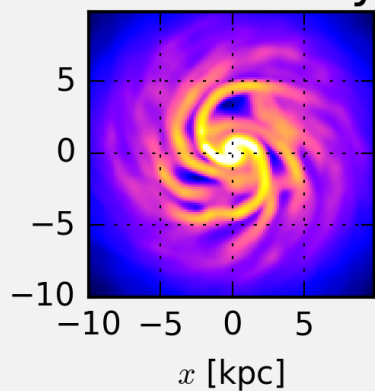
- Finally, I obtain the new instability condition for 2-comp. models,

$$S_2 \equiv \frac{1}{\pi G k^2} \left[ \frac{\Upsilon_g f(kW_g)}{c_s^2 k^2 + 4\Omega_g^2} + \frac{\Upsilon_s f(kW_s)}{\sigma_\phi^2 k^2 + 4\Omega_s^2} \right]^{-1} < 1.$$

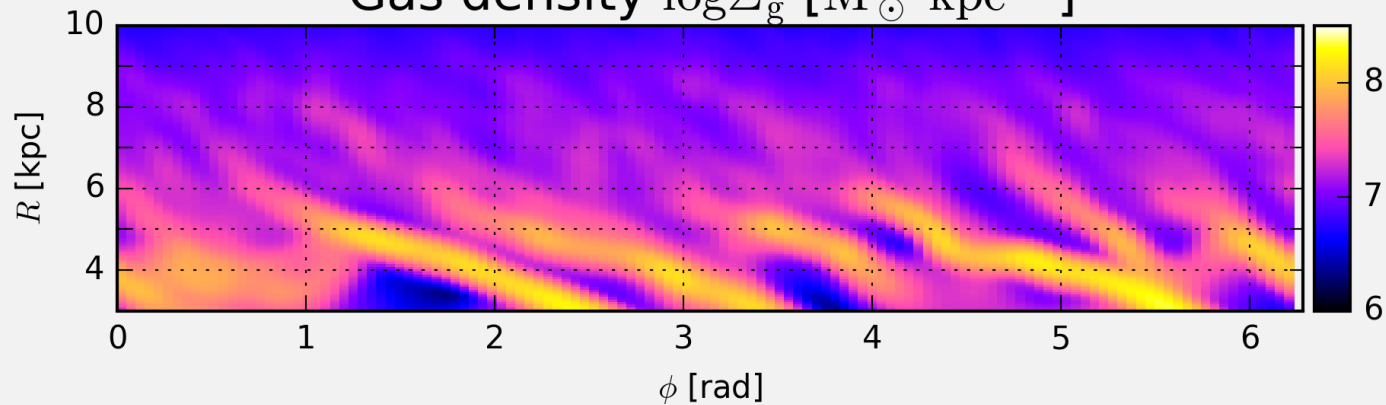
# Demonstration

The fragmenting case

Gas density

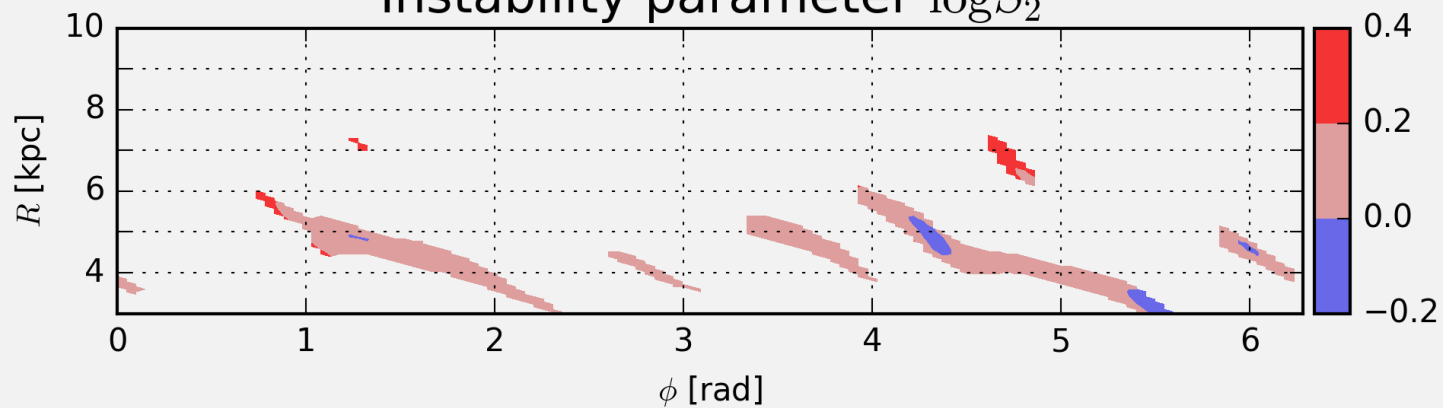


Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



$t=150$  Myr

Instability parameter  $\log S_2$

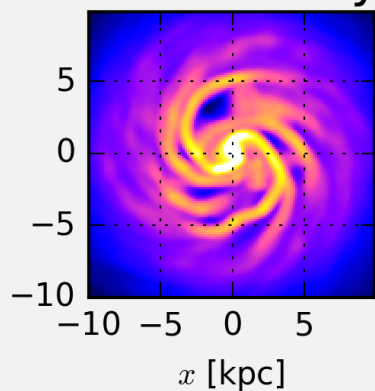




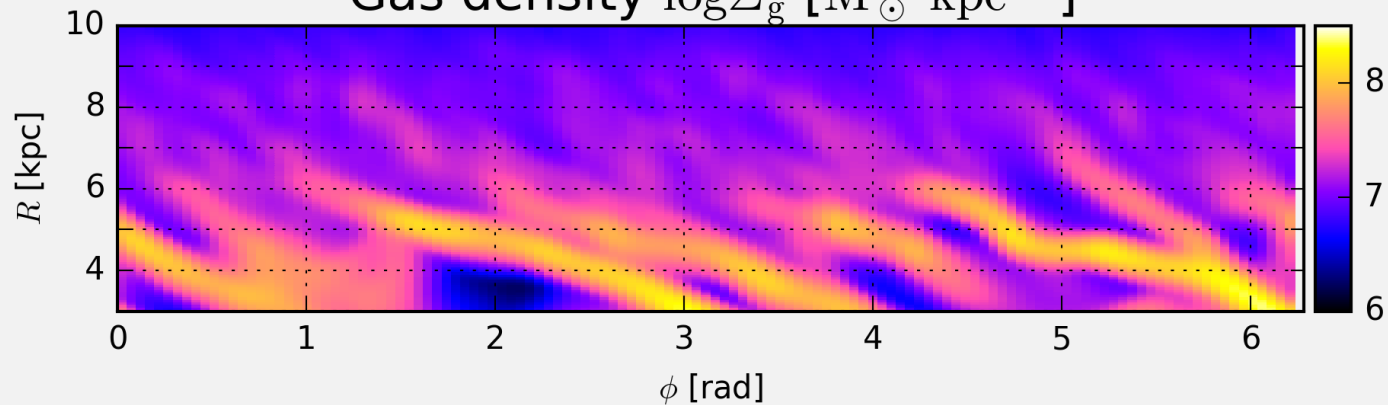
# Demonstration

The fragmenting case

Gas density

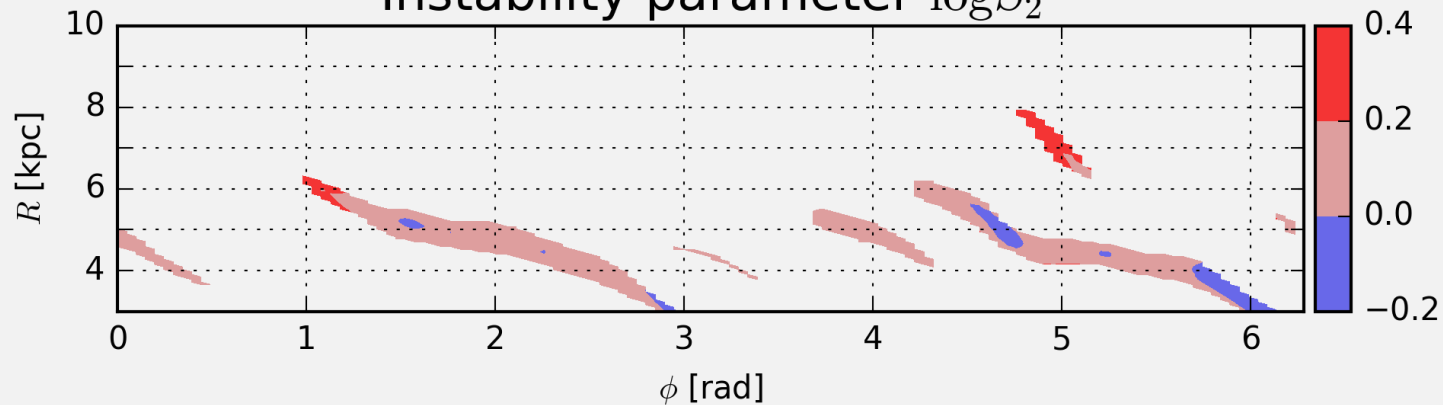


Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



$t=160$  Myr

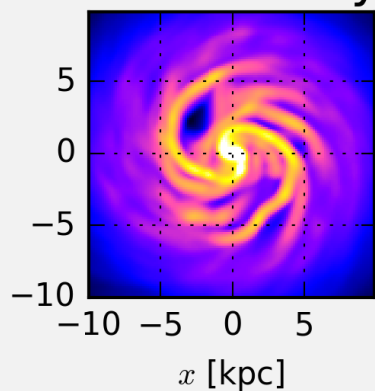
Instability parameter  $\log S_2$



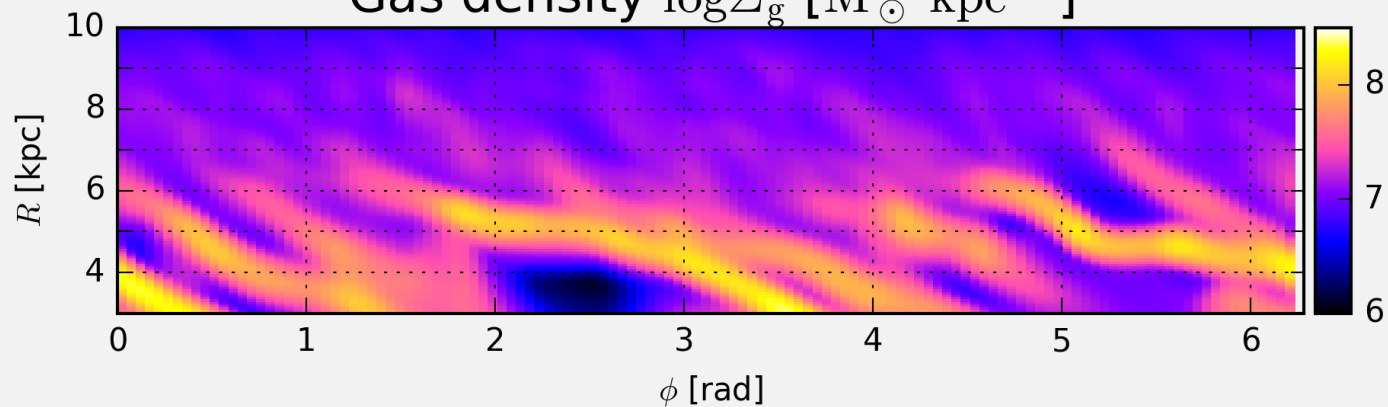
# Demonstration

The fragmenting case

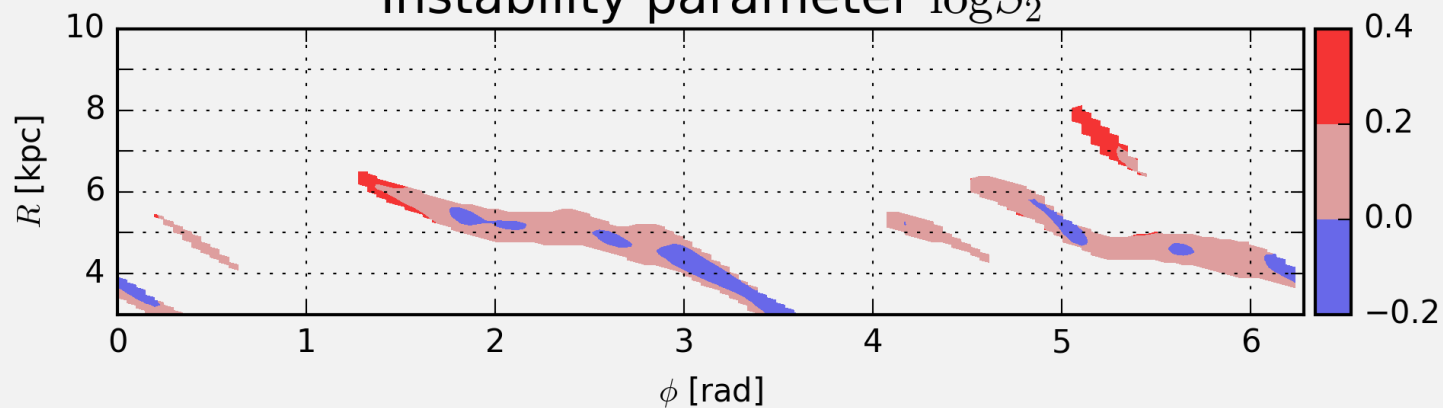
Gas density



Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



Instability parameter  $\log S_2$

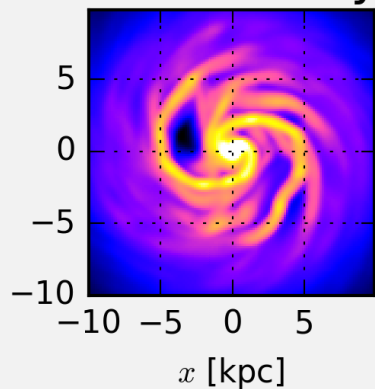


$t=170$  Myr

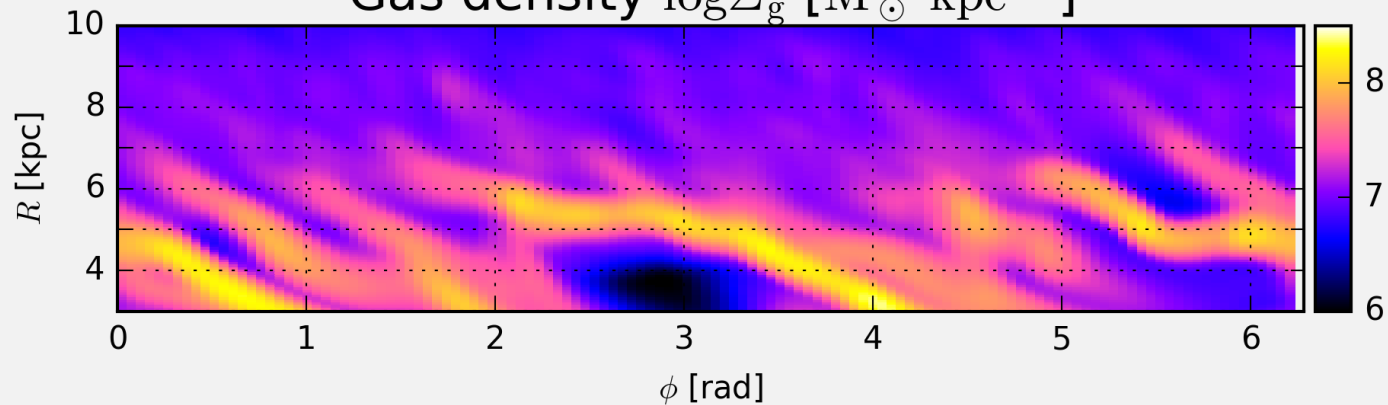
# Demonstration

The fragmenting case

Gas density

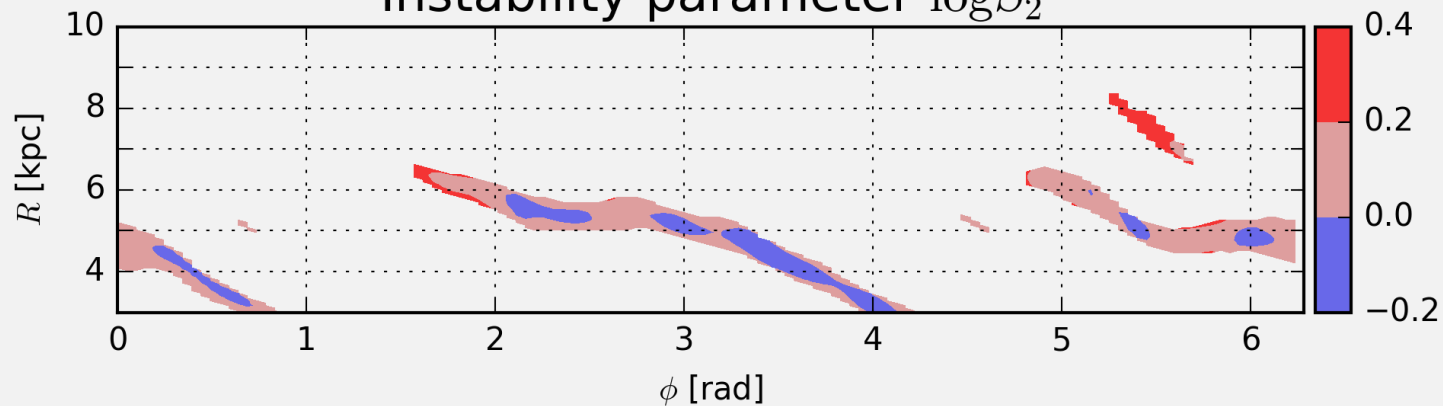


Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



$t=180$  Myr

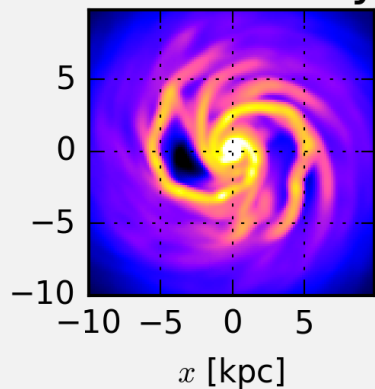
Instability parameter  $\log S_2$



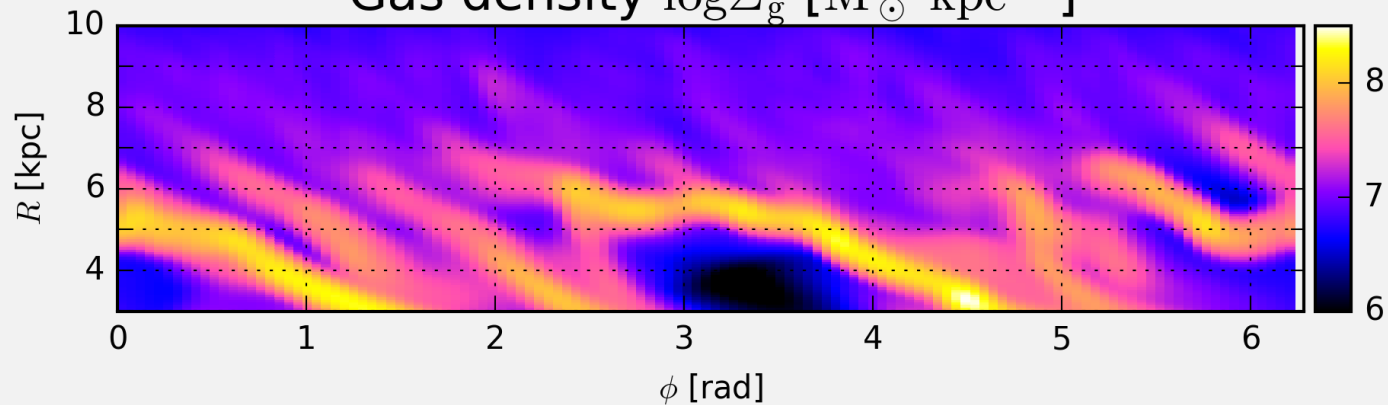
# Demonstration

The fragmenting case

Gas density

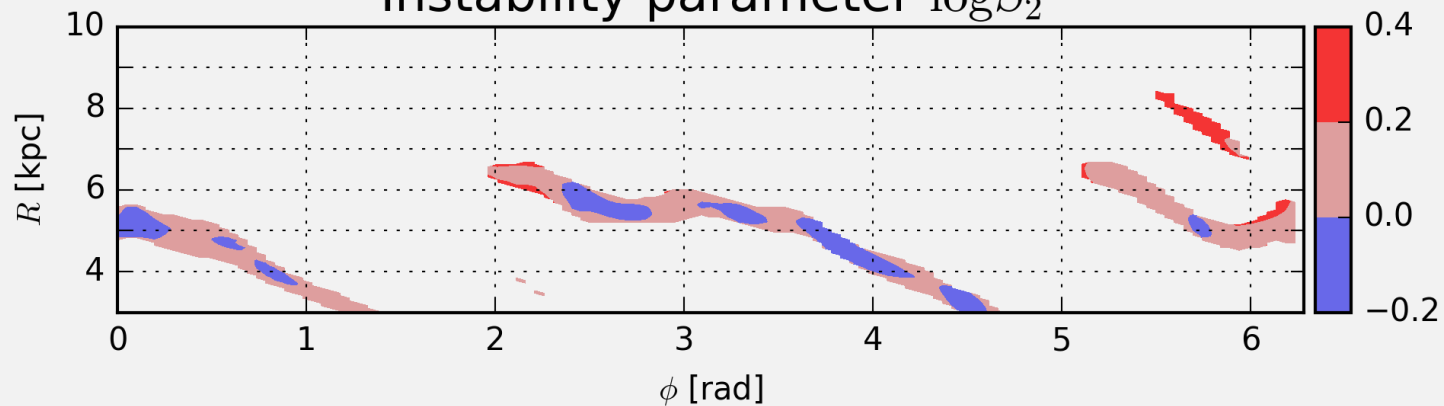


Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



$t=190$  Myr

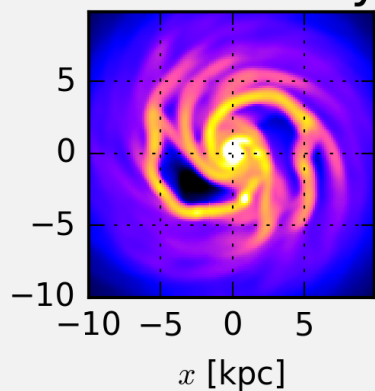
Instability parameter  $\log S_2$



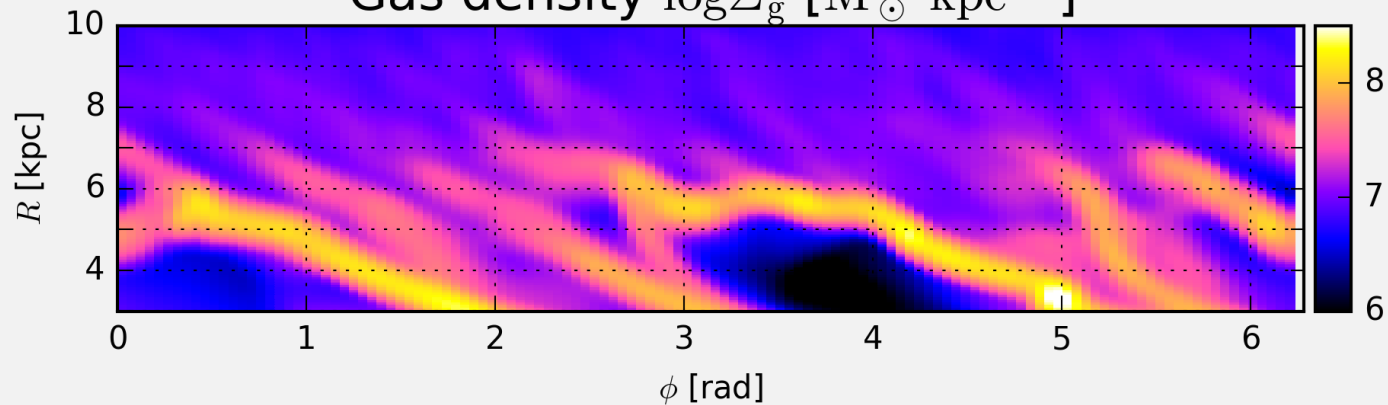
# Demonstration

The fragmenting case

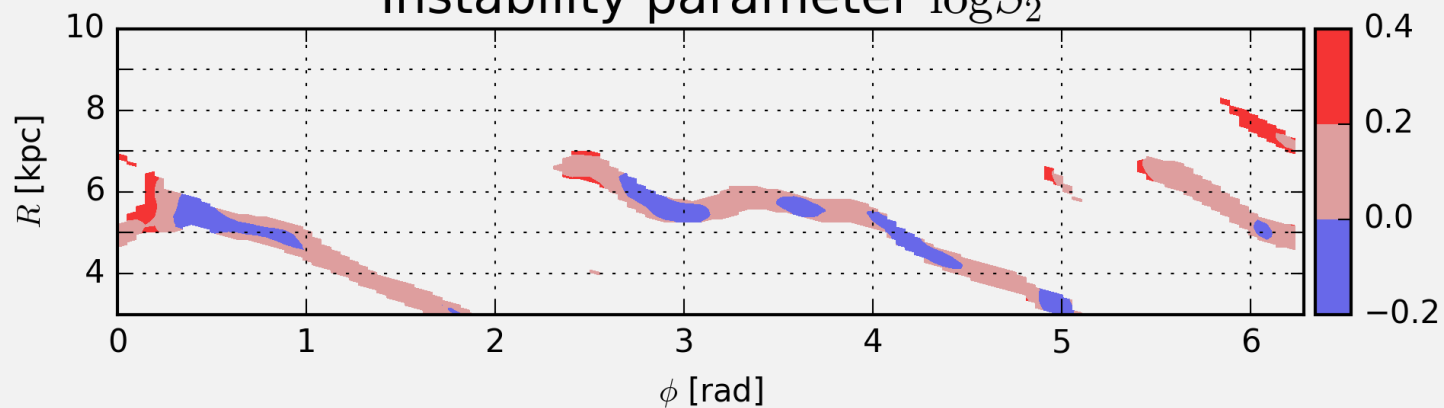
Gas density



Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



Instability parameter  $\log S_2$



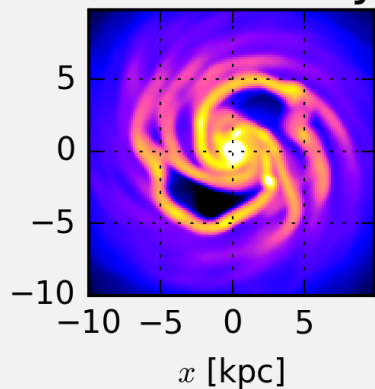
$t=200$  Myr



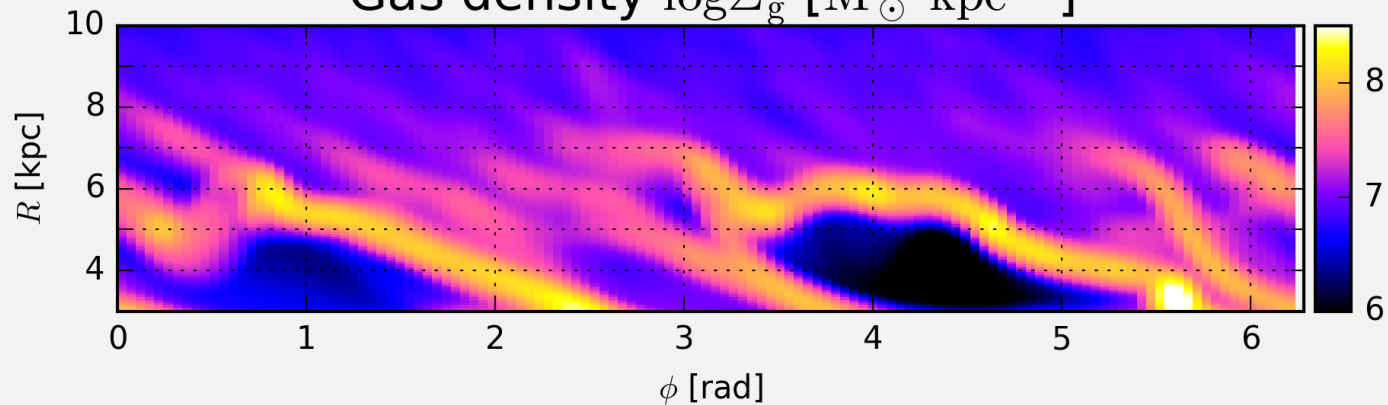
# Demonstration

The fragmenting case

Gas density

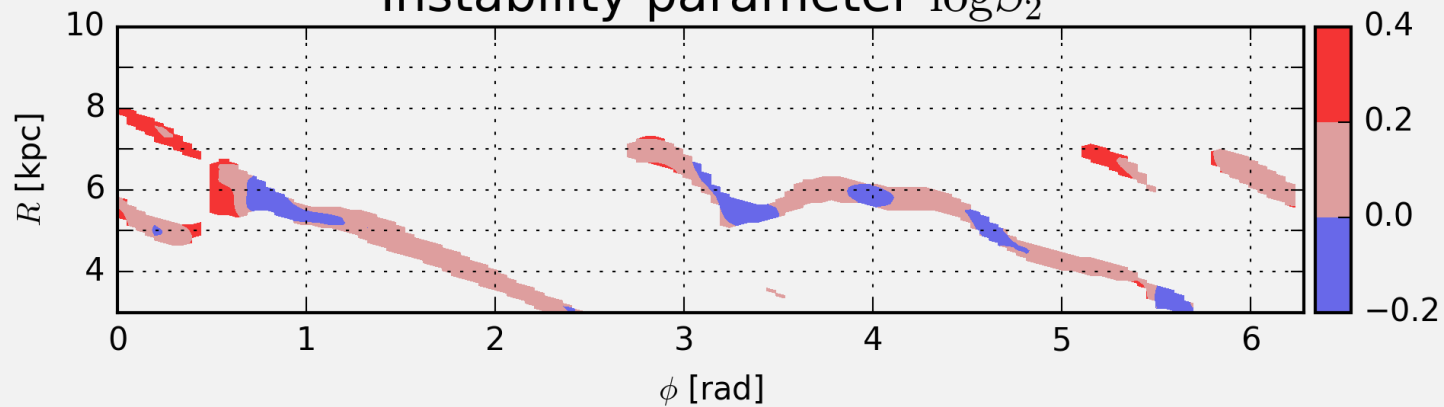


Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



$t=210$  Myr

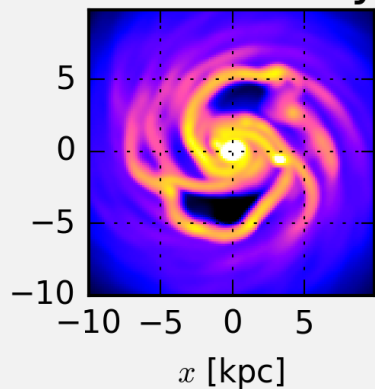
Instability parameter  $\log S_2$



# Demonstration

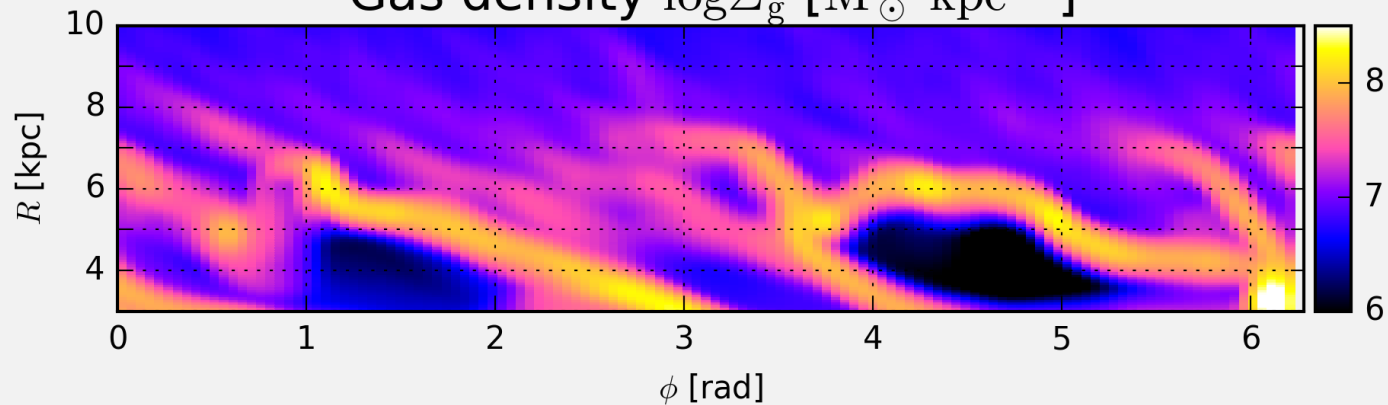
The fragmenting case

Gas density

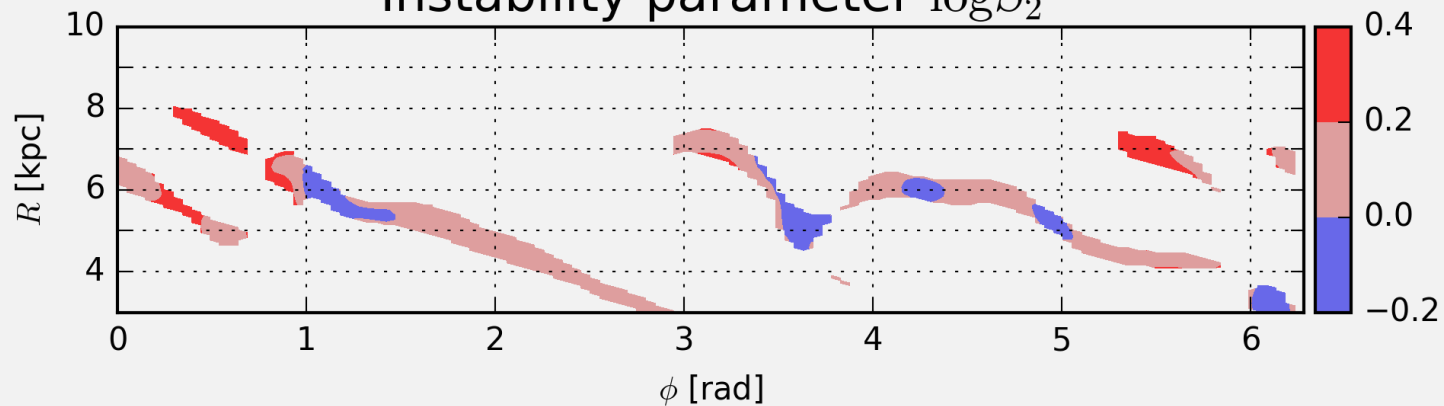


$t=220$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



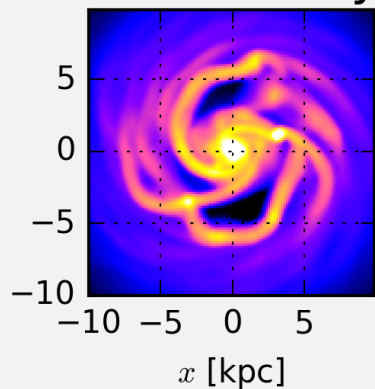
Instability parameter  $\log S_2$



# Demonstration

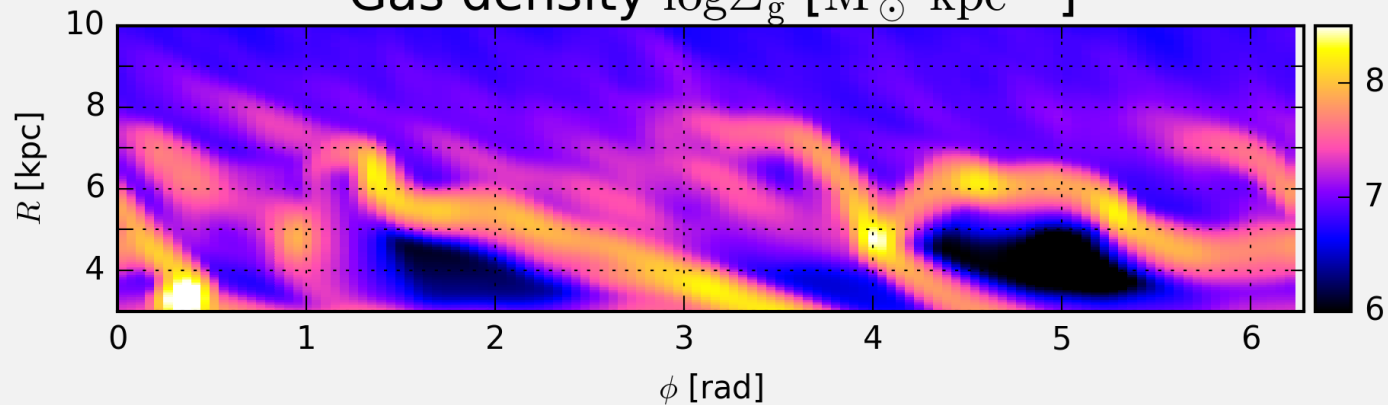
The fragmenting case

Gas density

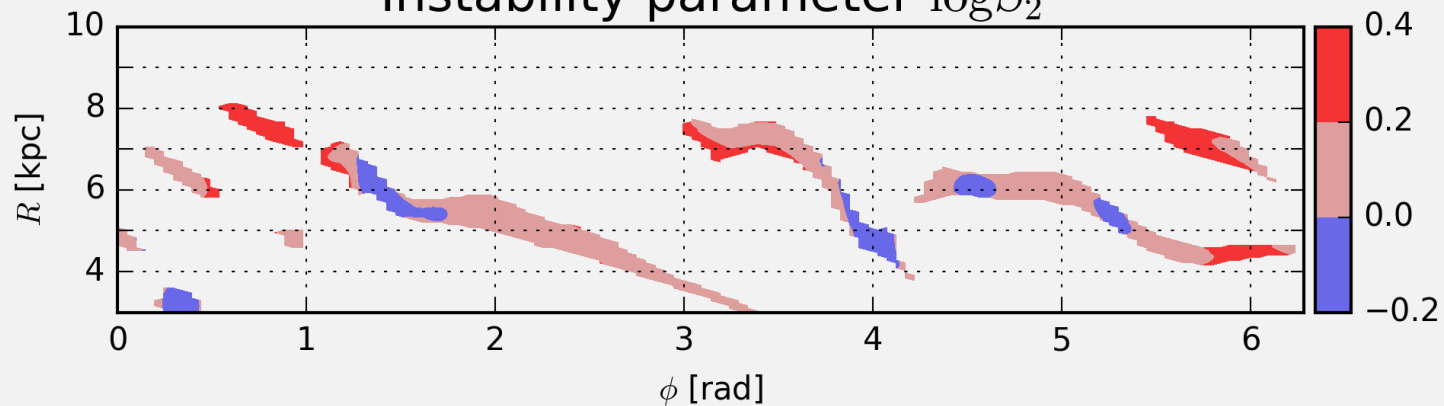


$t=230$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



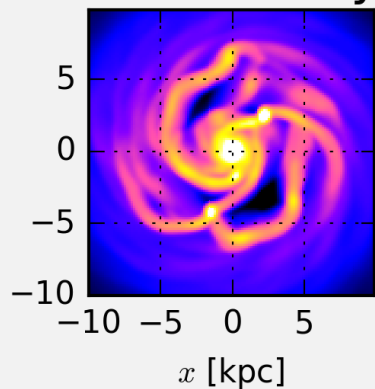
Instability parameter  $\log S_2$



# Demonstration

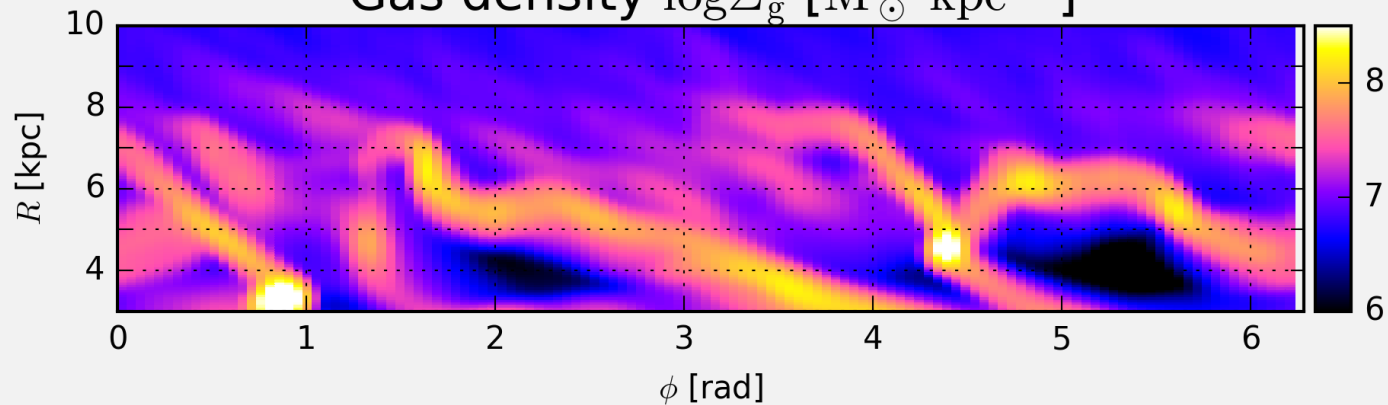
The fragmenting case

Gas density

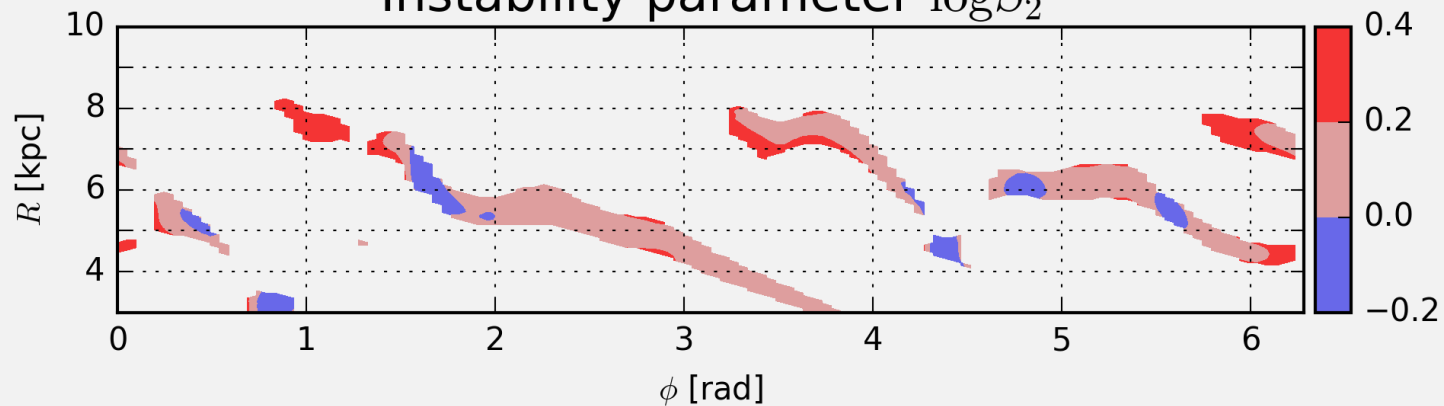


$t=240$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



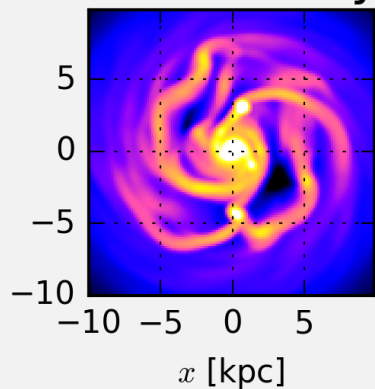
Instability parameter  $\log S_2$



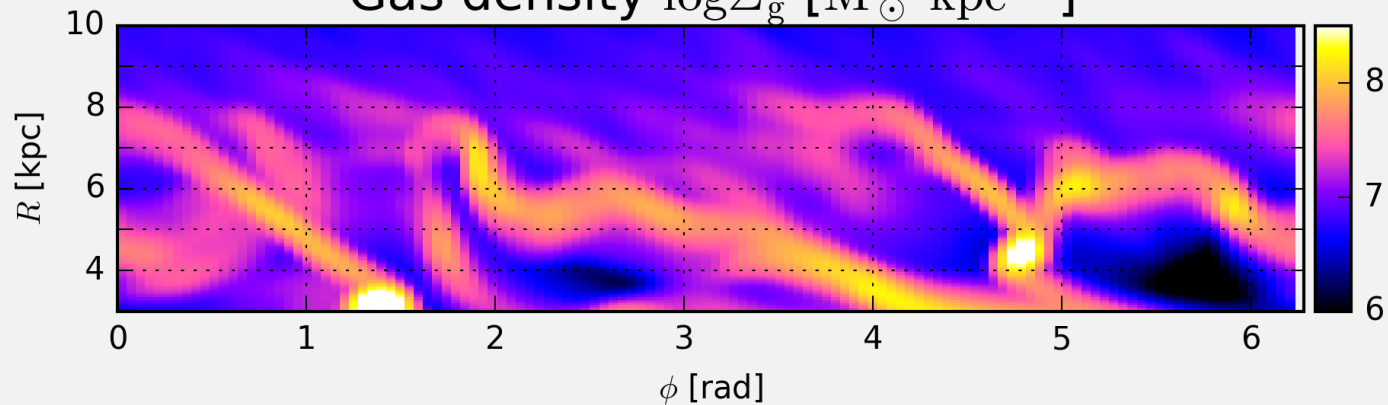
# Demonstration

The fragmenting case

Gas density

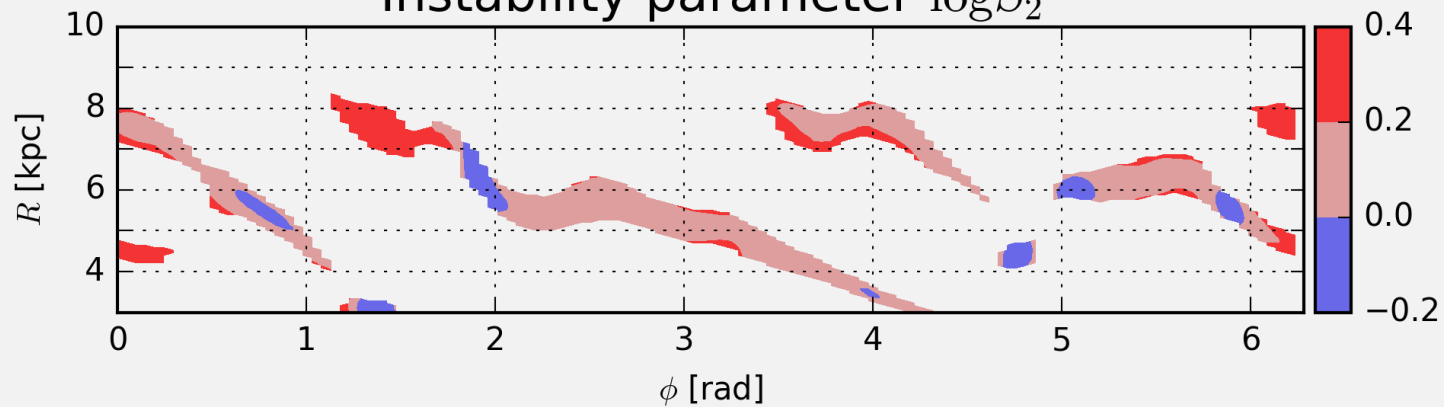


Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



$t=250$  Myr

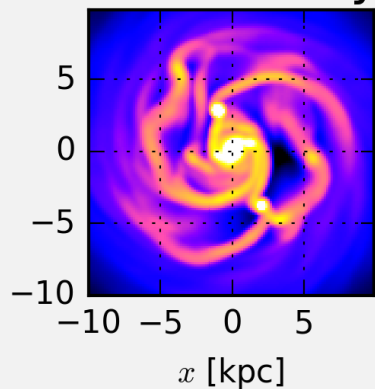
Instability parameter  $\log S_2$



# Demonstration

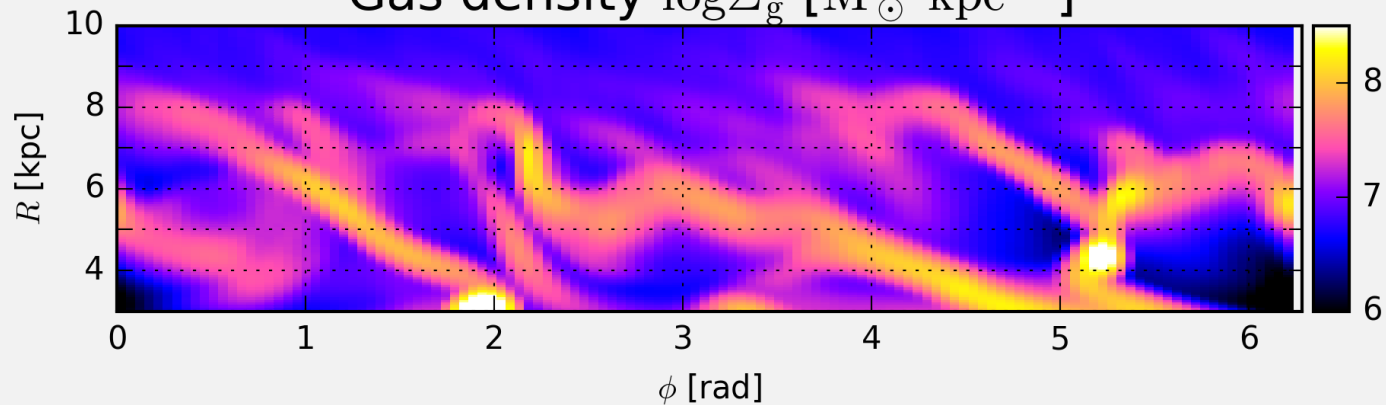
The fragmenting case

Gas density

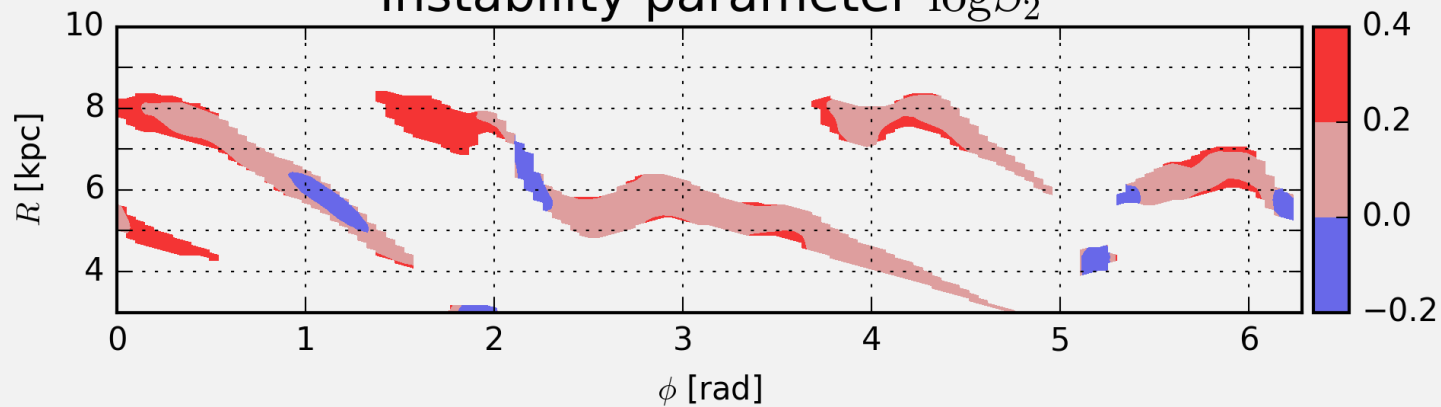


$t=260$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



Instability parameter  $\log S_2$

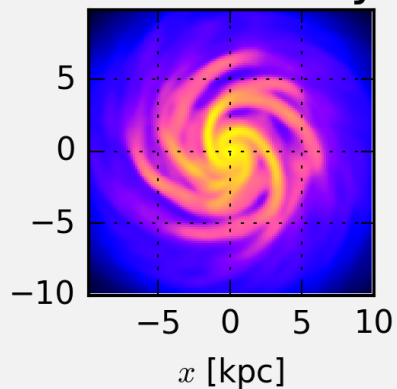




# Demonstration

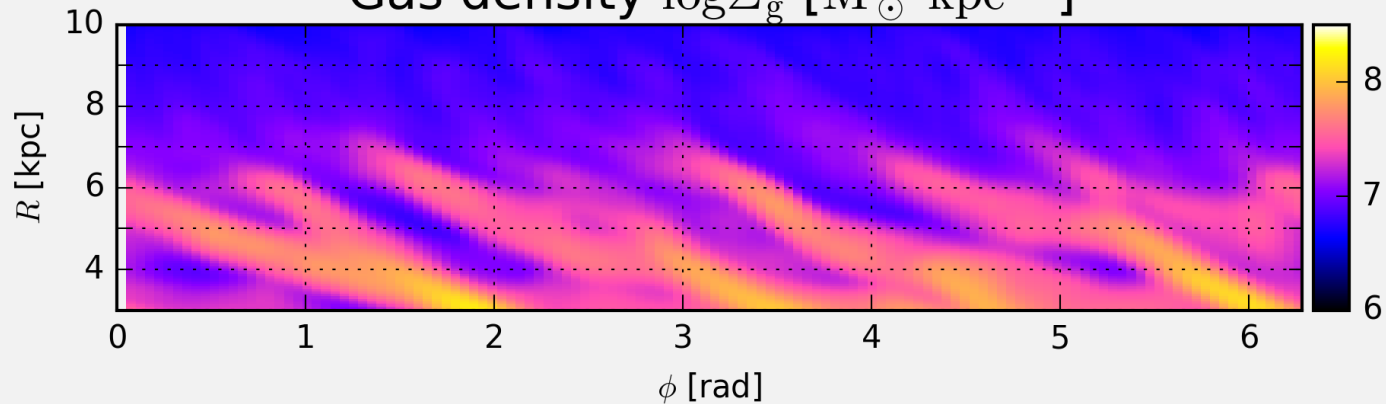
The stable case

Gas density

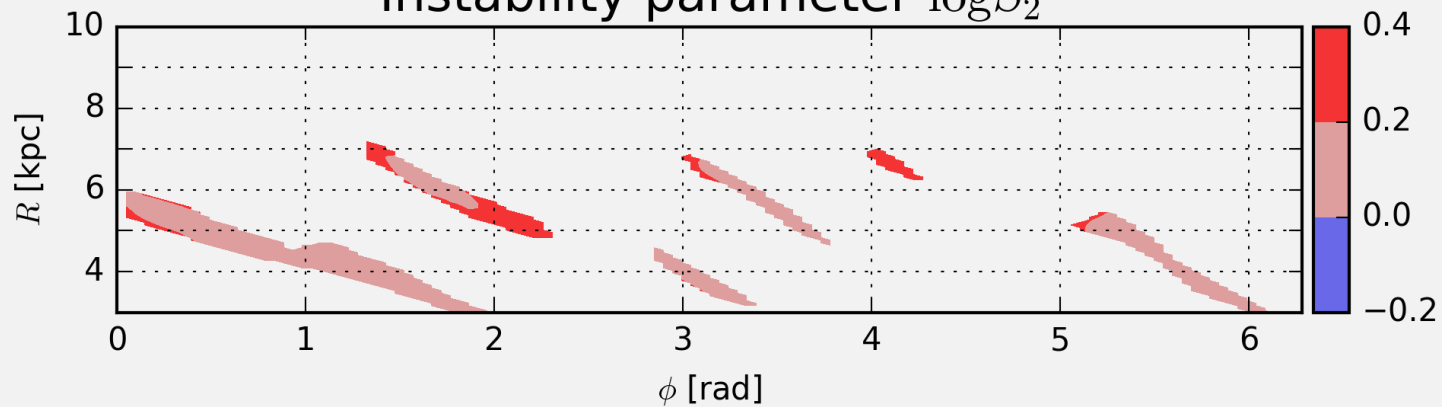


$t=200$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



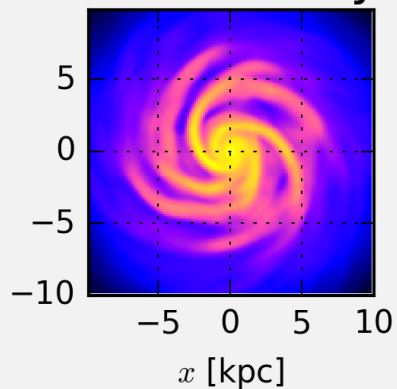
Instability parameter  $\log S_2$



# Demonstration

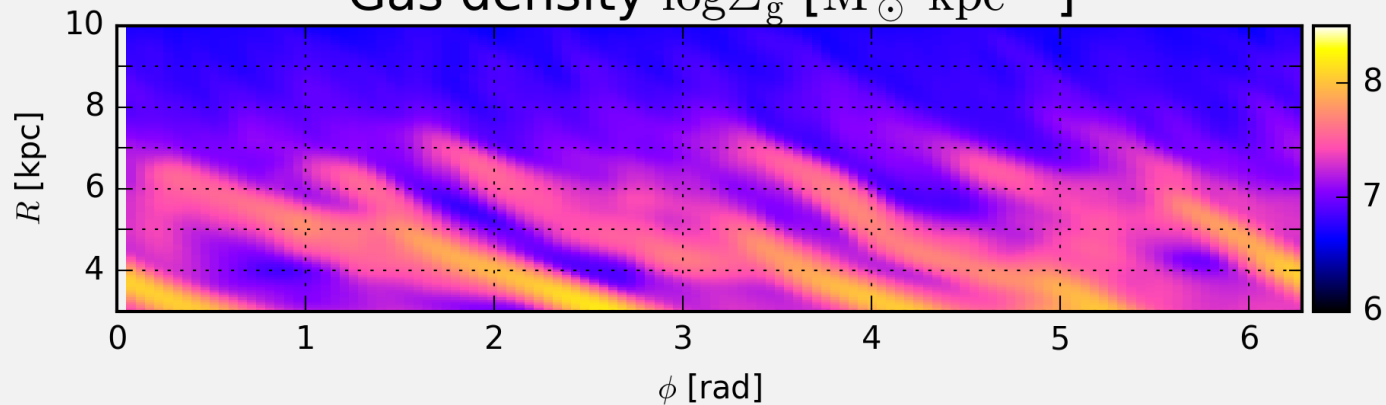
The stable case

Gas density

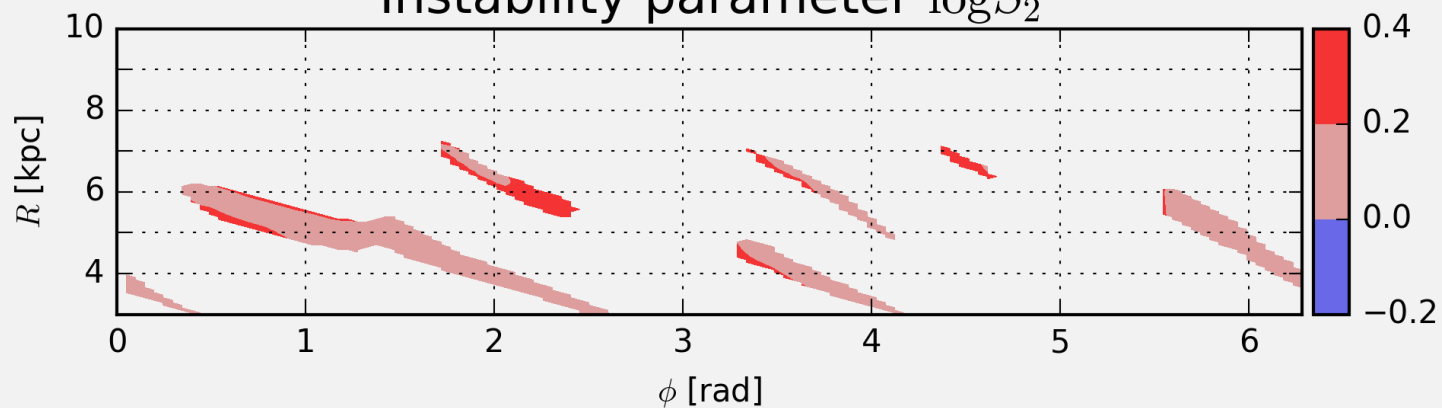


$t=210$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



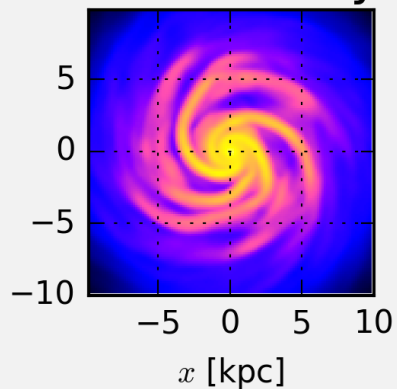
Instability parameter  $\log S_2$



# Demonstration

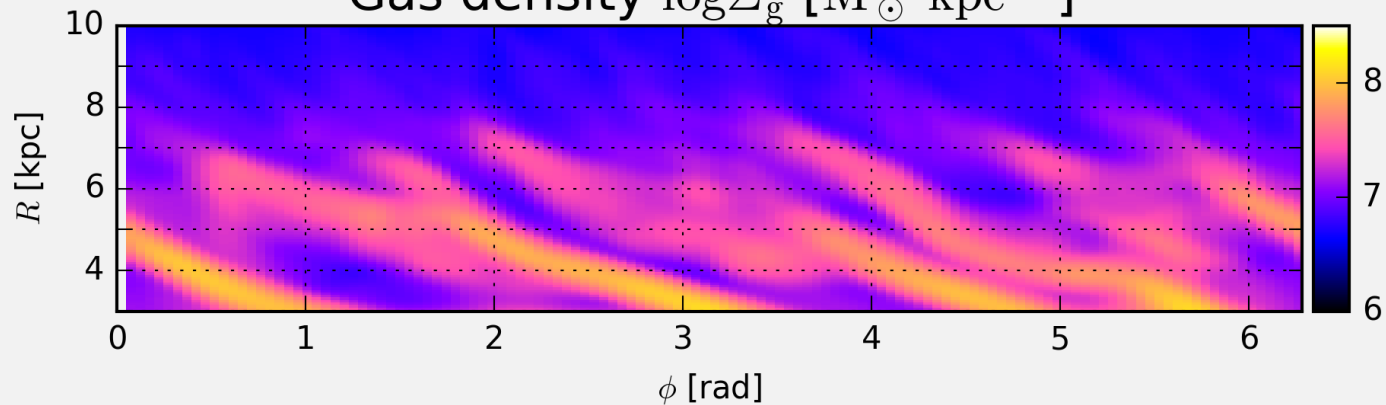
The stable case

Gas density

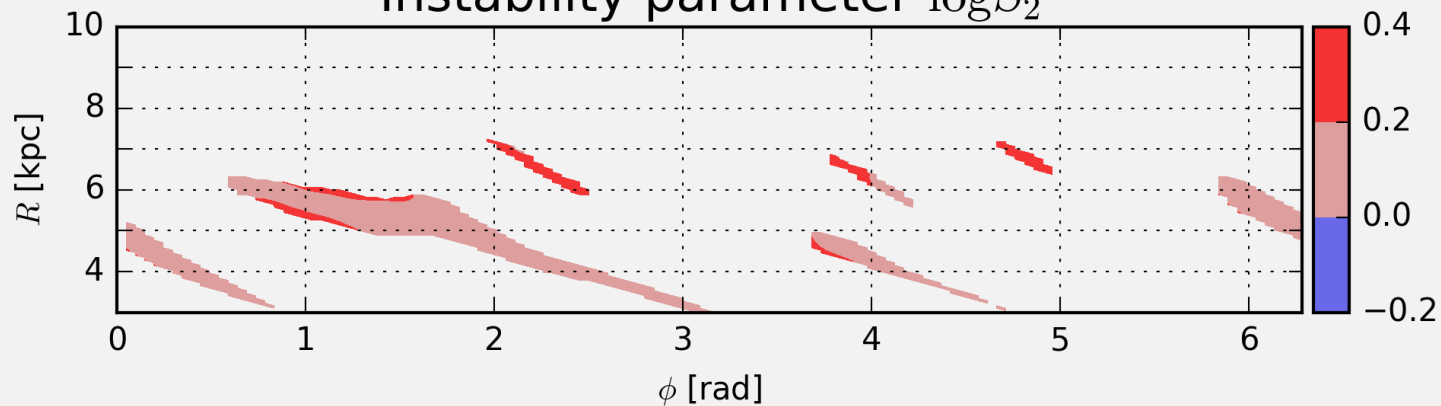


$t=220$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



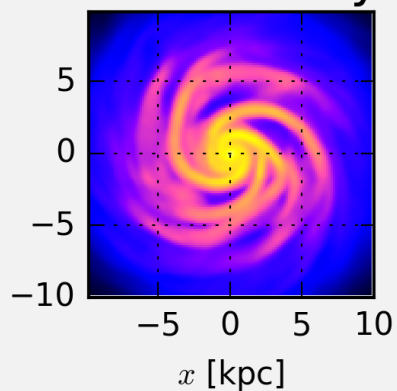
Instability parameter  $\log S_2$



# Demonstration

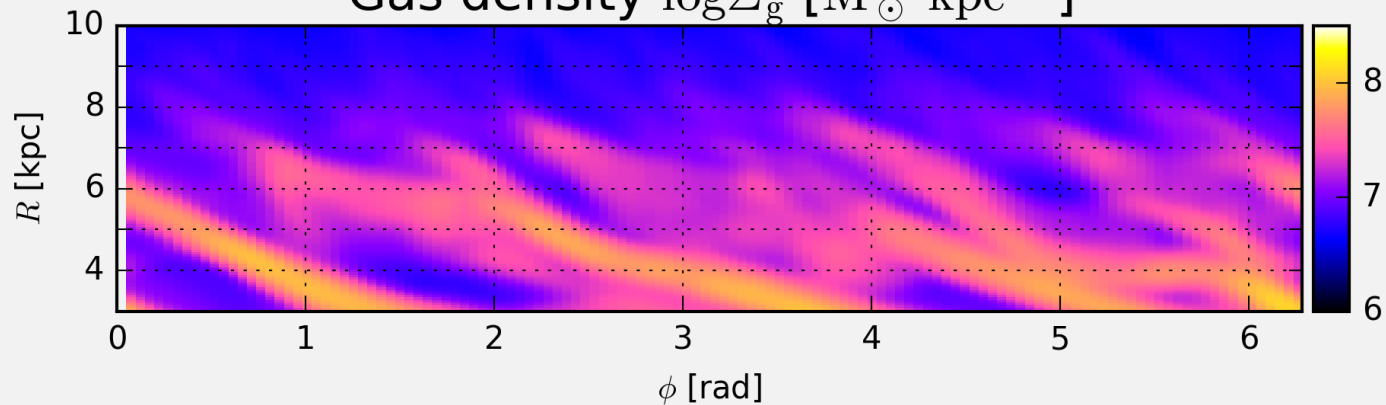
The stable case

Gas density

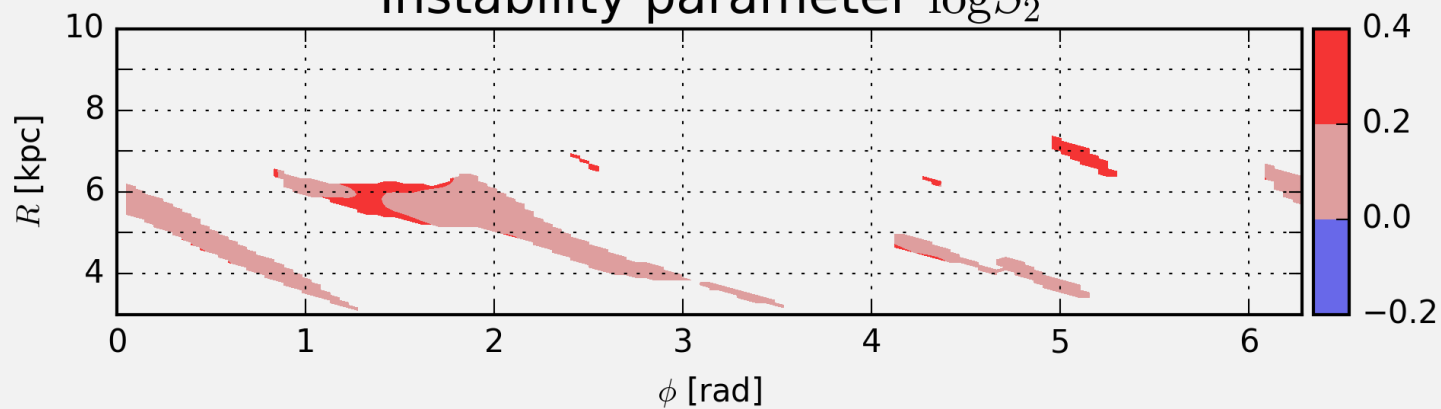


$t=230$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



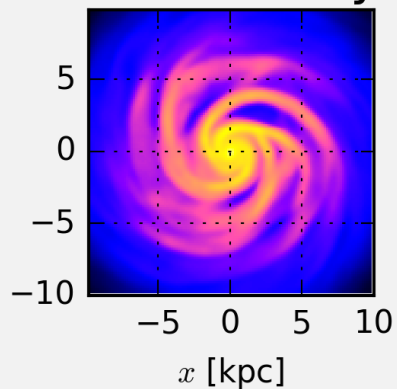
Instability parameter  $\log S_2$



# Demonstration

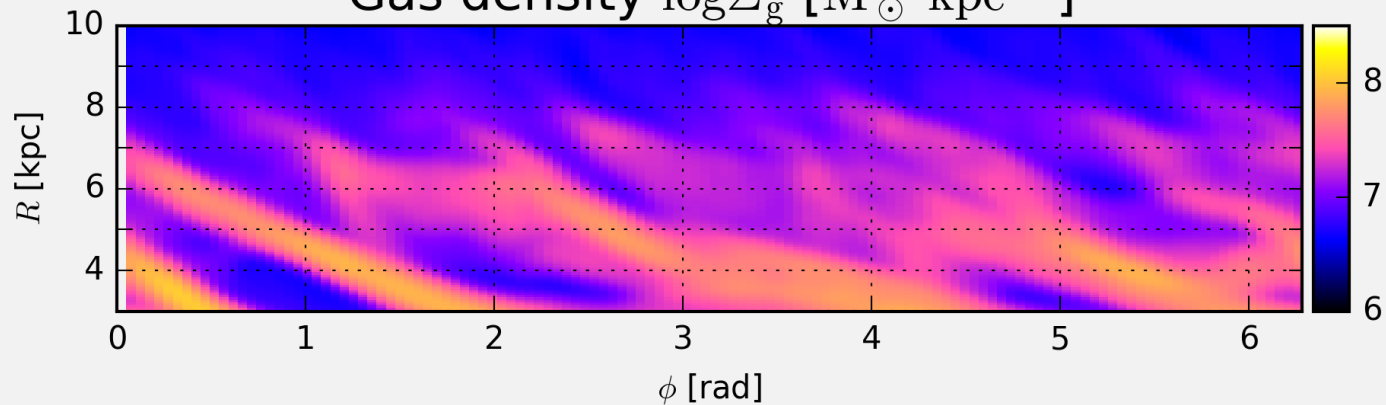
The stable case

Gas density

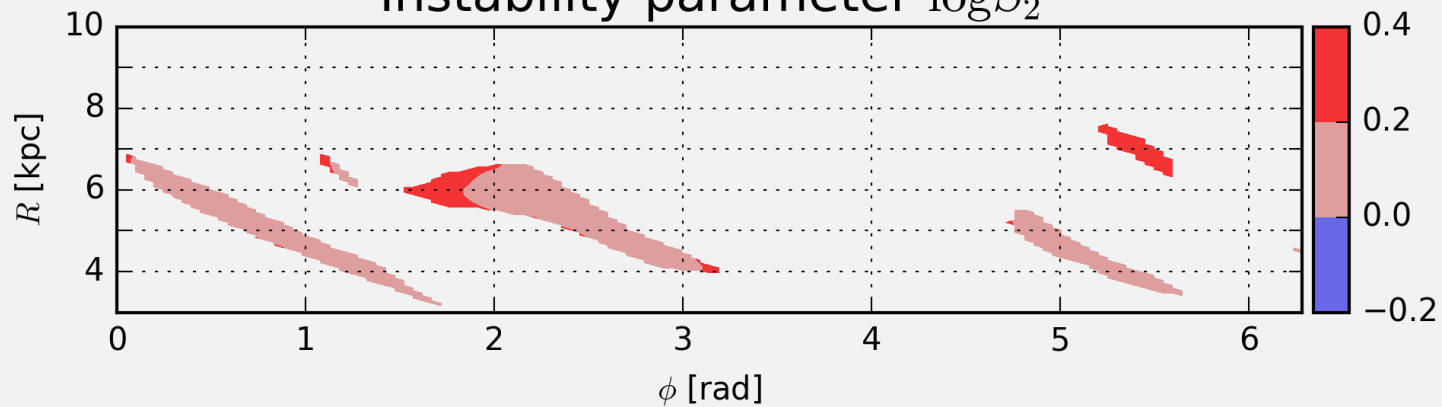


$t=240$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



Instability parameter  $\log S_2$

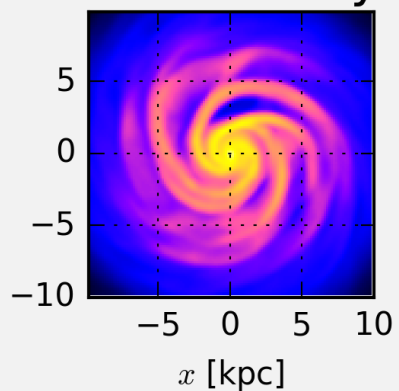




# Demonstration

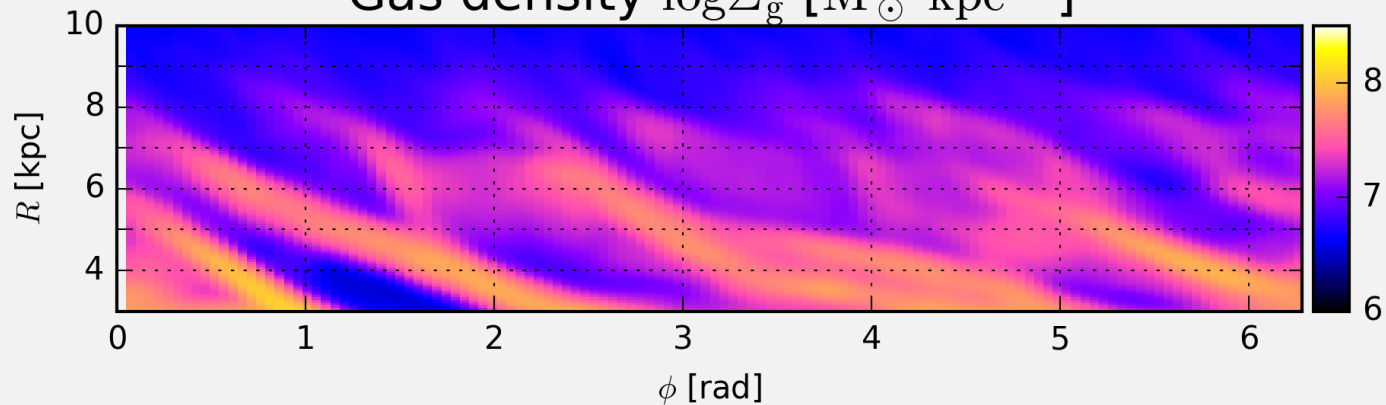
The stable case

Gas density

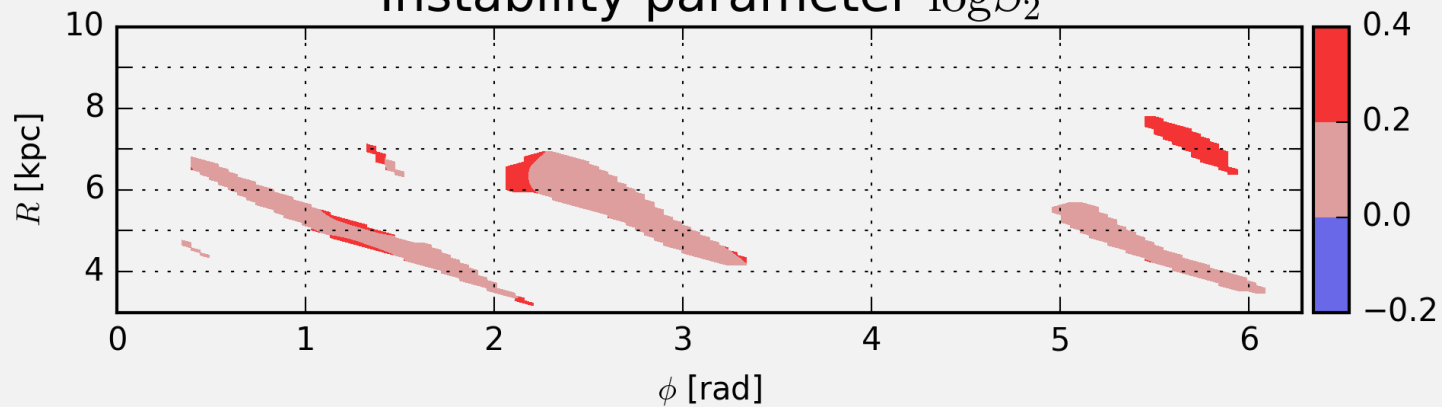


$t=250$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



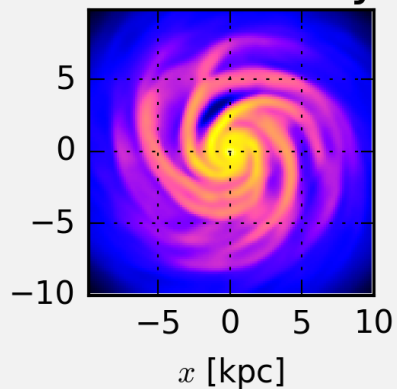
Instability parameter  $\log S_2$



# Demonstration

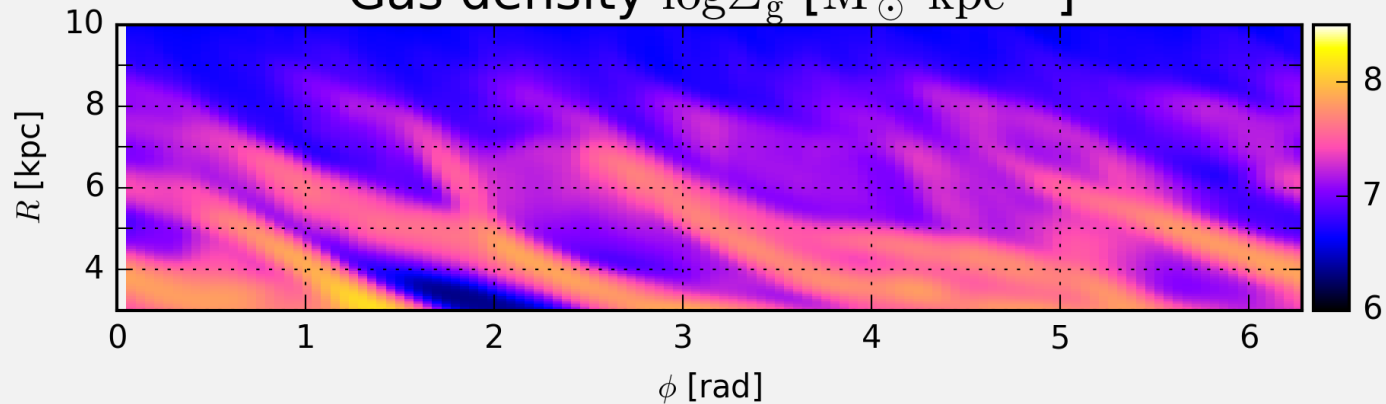
The stable case

Gas density

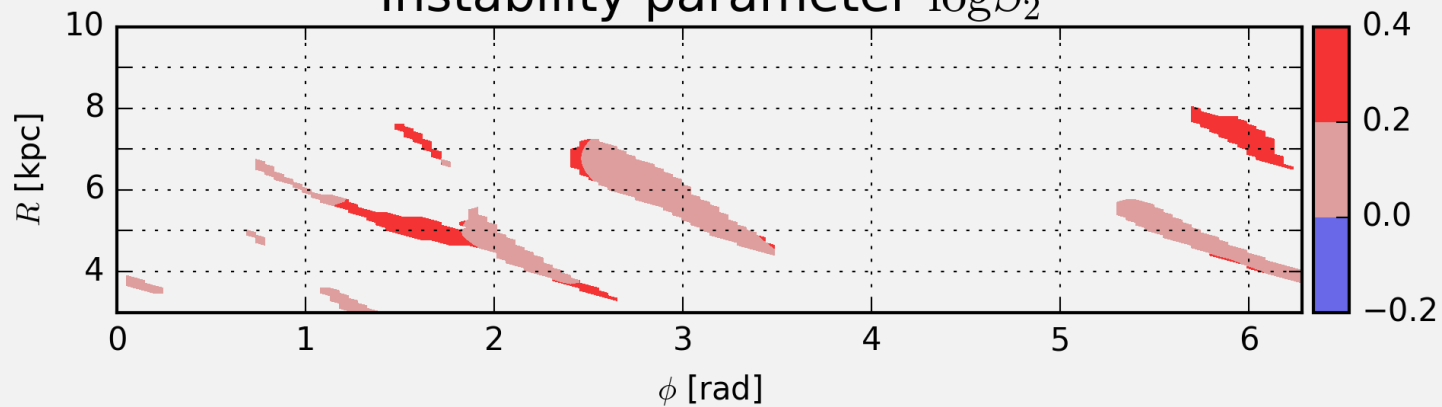


$t=260$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



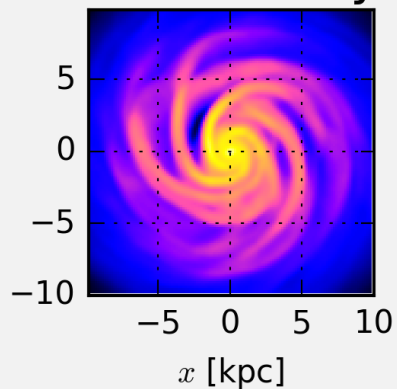
Instability parameter  $\log S_2$



# Demonstration

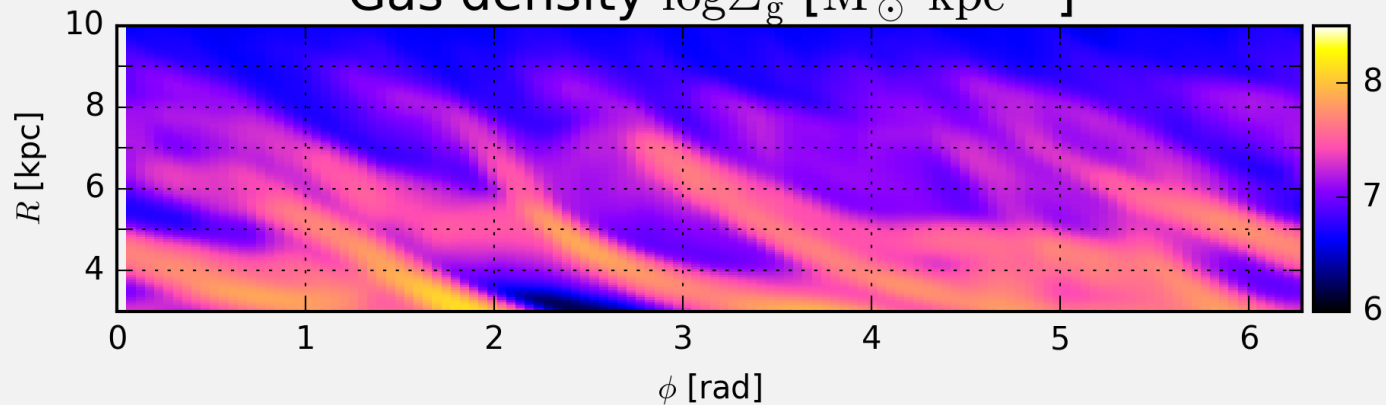
The stable case

Gas density

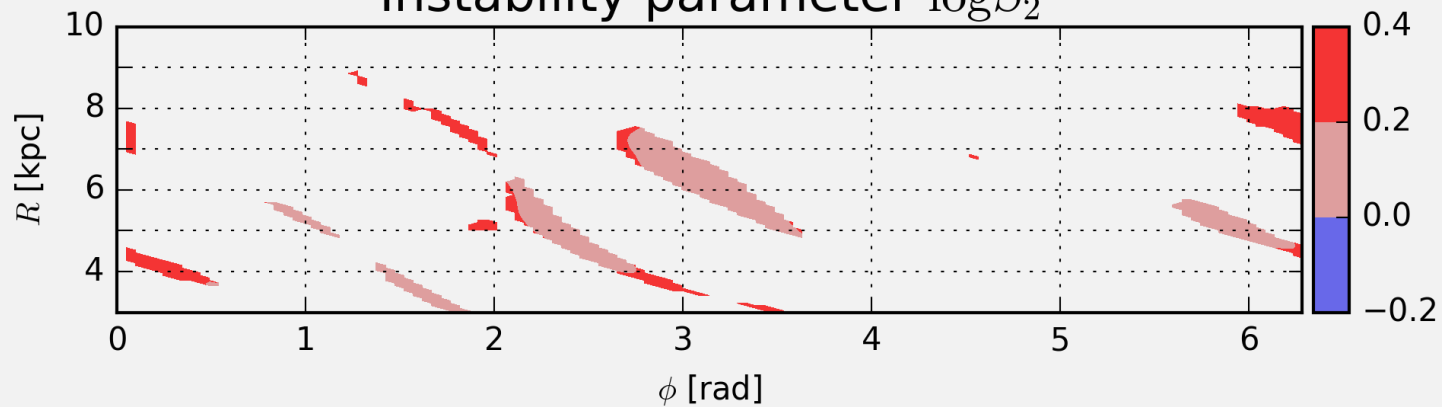


$t=270$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



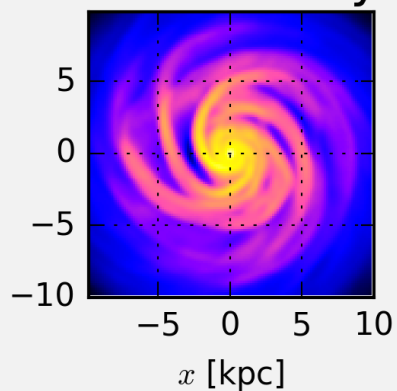
Instability parameter  $\log S_2$



# Demonstration

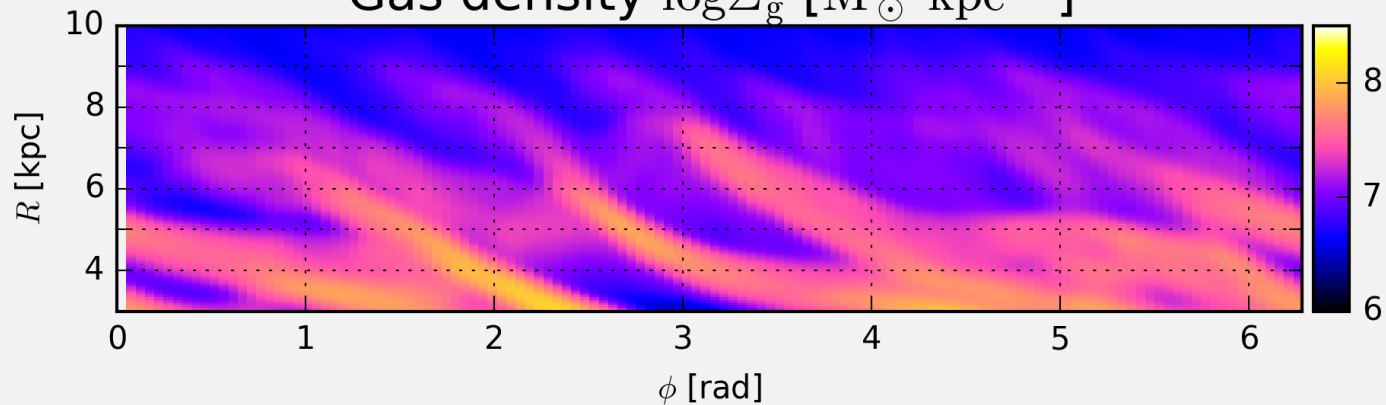
The stable case

Gas density

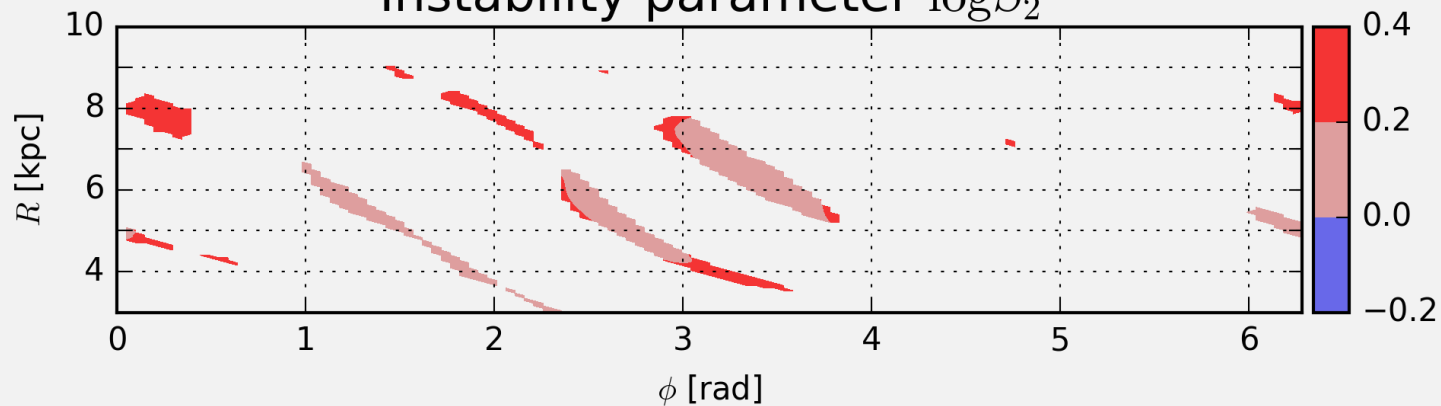


$t=280$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



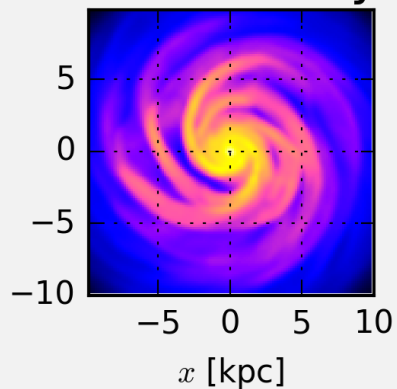
Instability parameter  $\log S_2$



# Demonstration

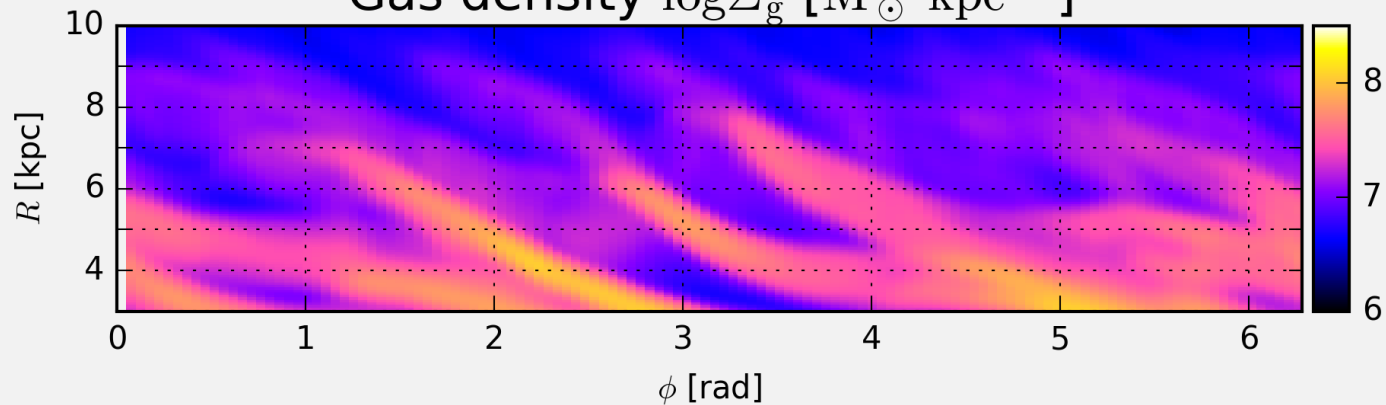
The stable case

Gas density

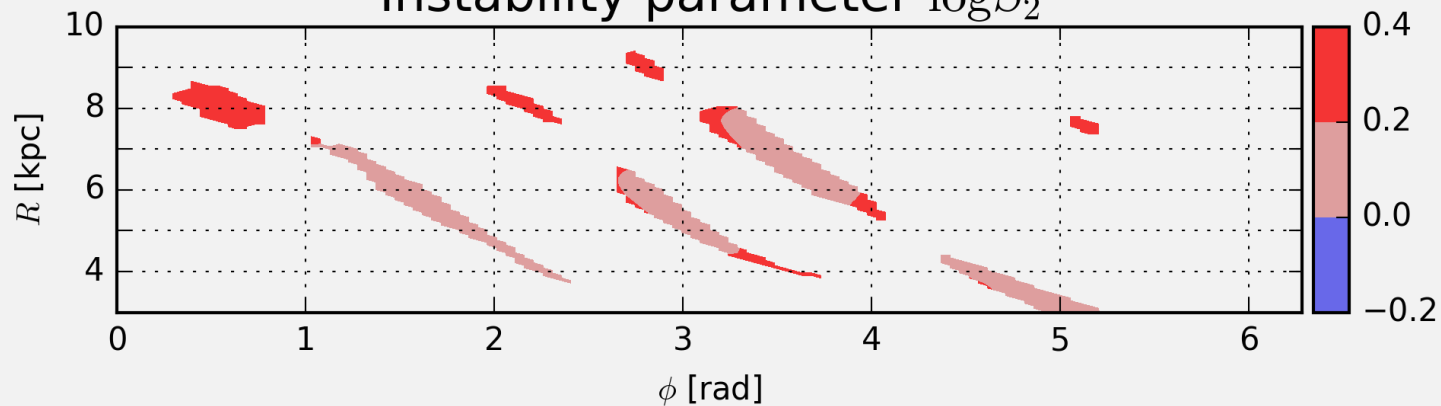


$t=290$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



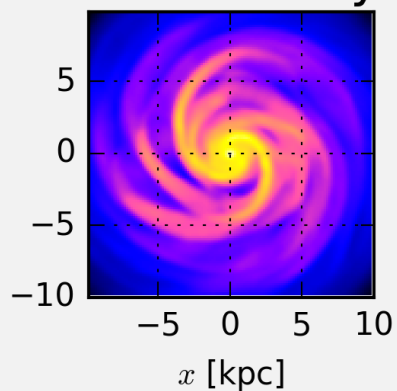
Instability parameter  $\log S_2$



# Demonstration

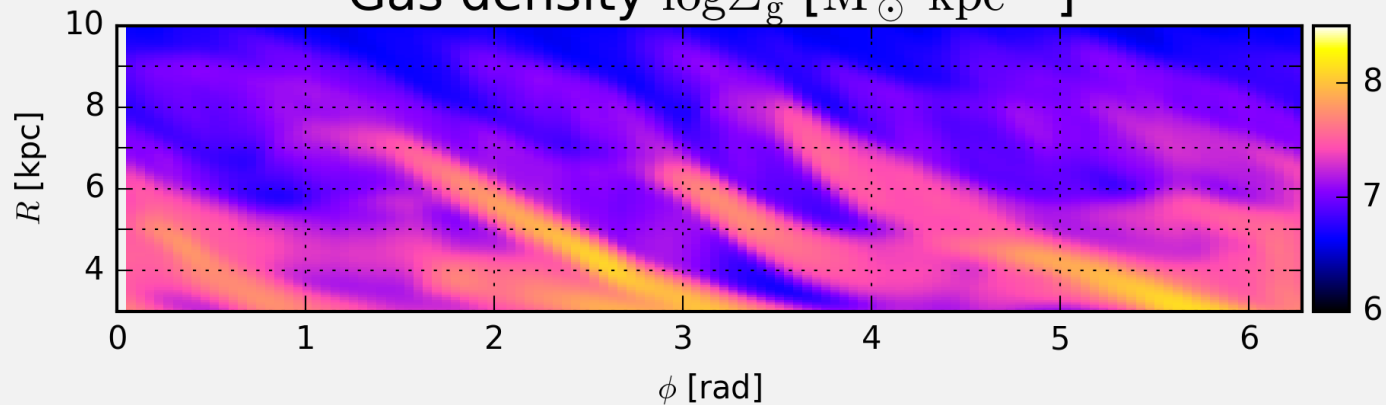
The stable case

Gas density

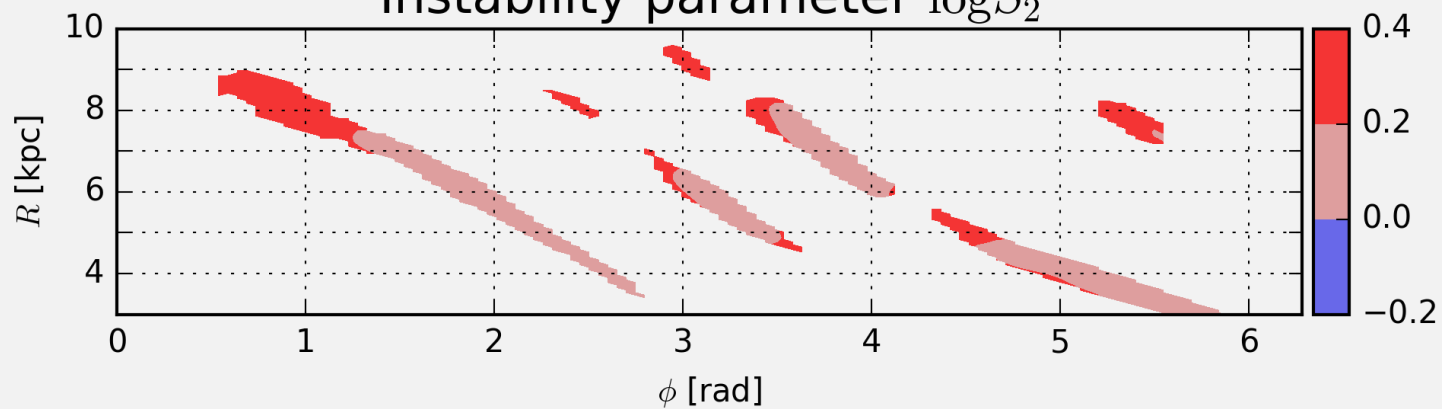


$t=300$  Myr

Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



Instability parameter  $\log S_2$

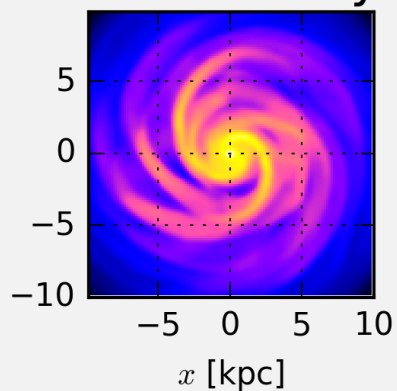




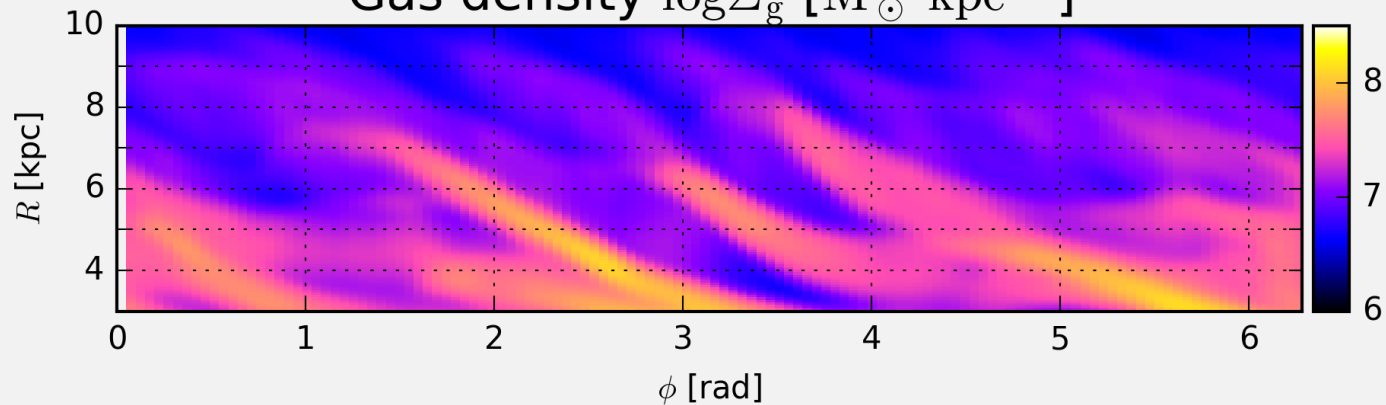
# Demonstration

The stable case

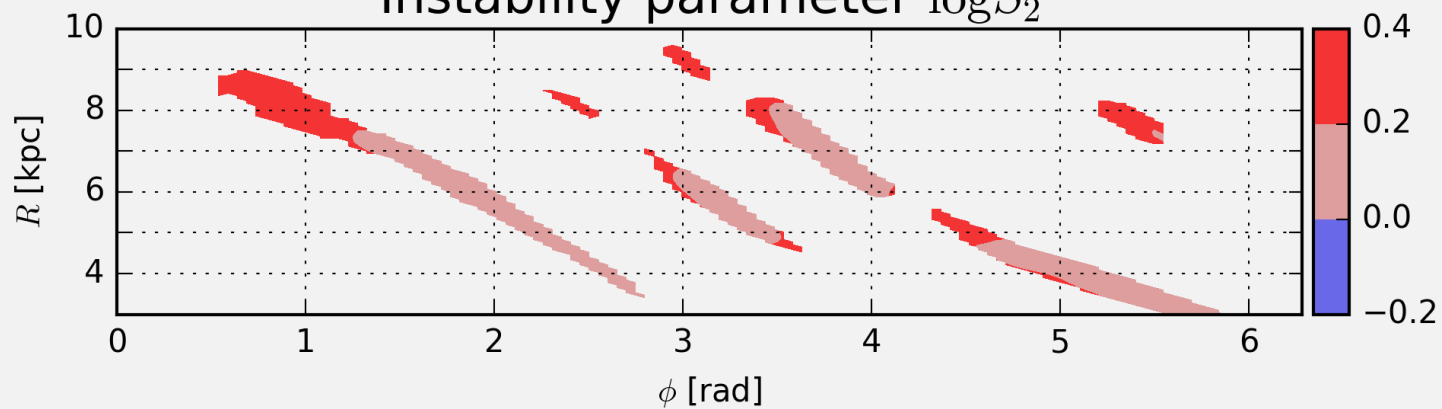
Gas density



Gas density  $\log \Sigma_g$  [ $M_\odot \text{ kpc}^{-2}$ ]



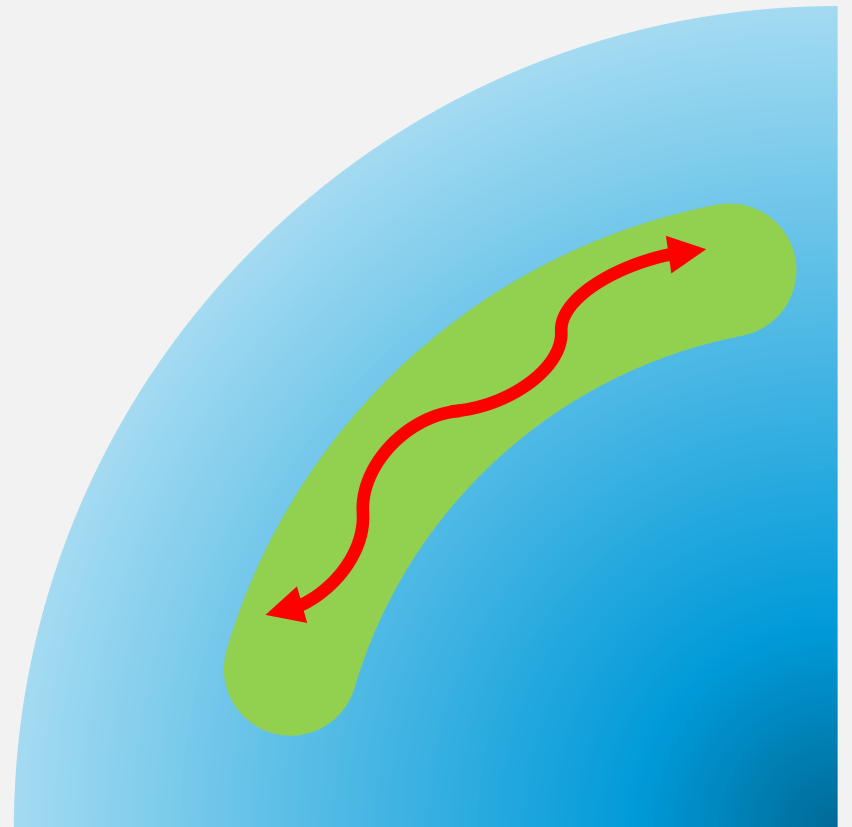
Instability parameter  $\log S_2$



$t=300$  Myr

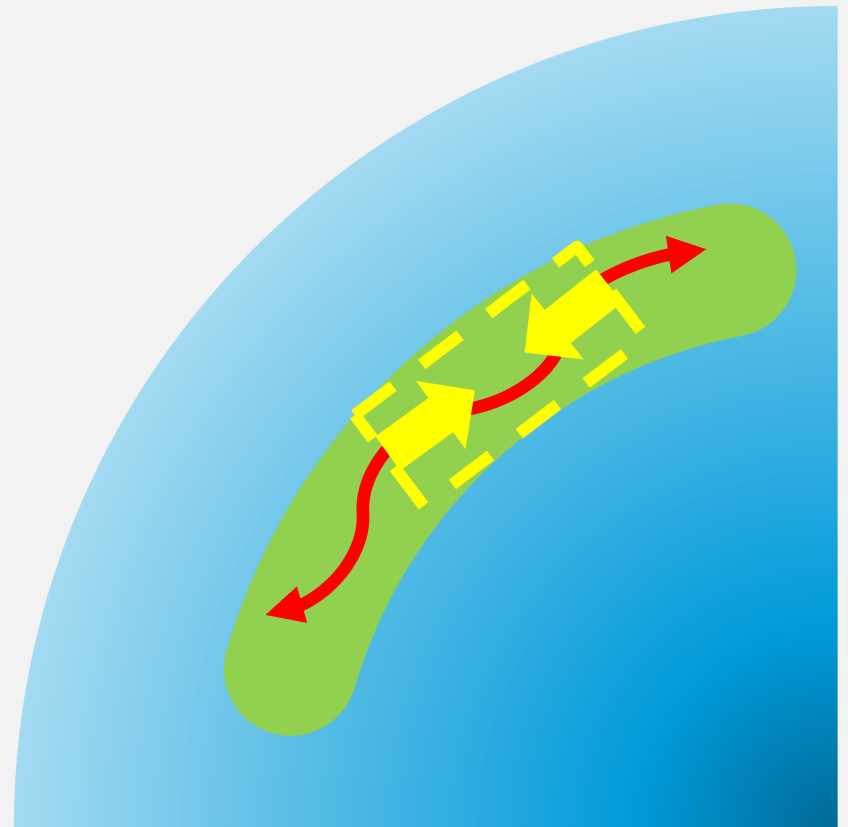
## Clump mass estimation

- If the unstable wavelength is long,  $\lambda \gg W$ ,
- An unstable perturbation is expected to collapse along the arm (1D collapse)



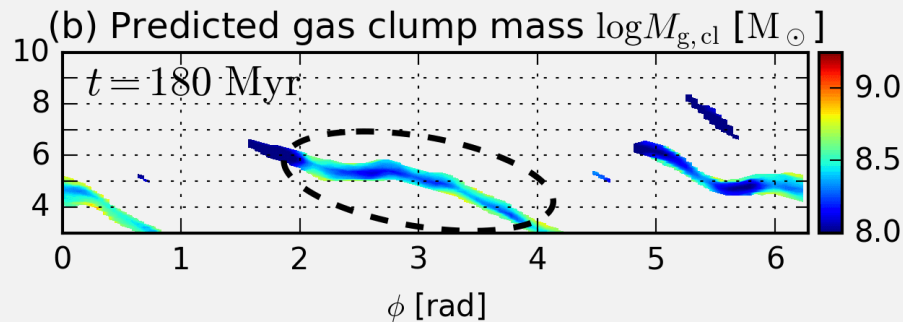
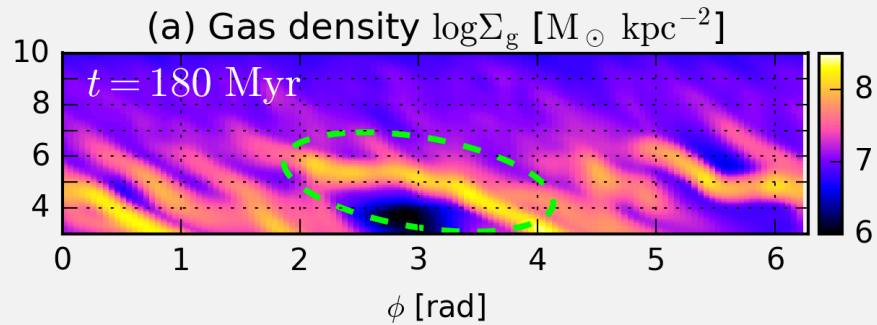
## Clump mass estimation

- If the unstable wavelength is long,  $\lambda \gg W$ ,
  - An unstable perturbation is expected to collapse along the arm (1D collapse)
- $M_{cl} \sim \Sigma W \lambda$



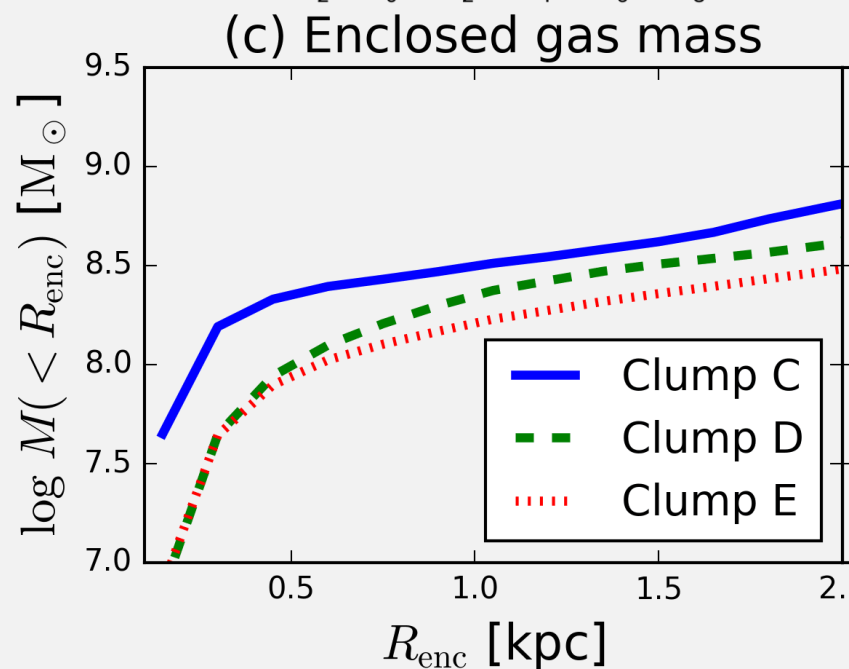
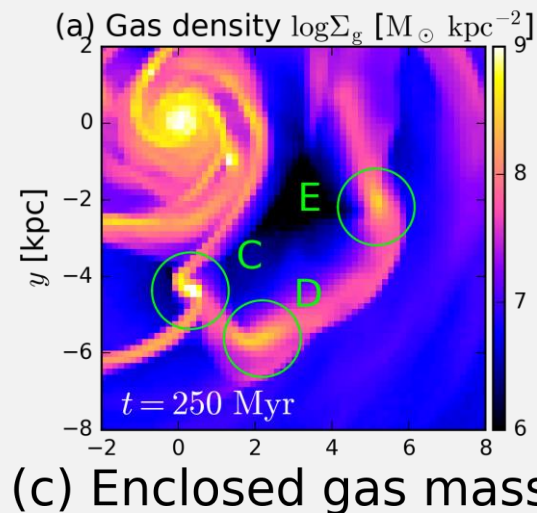
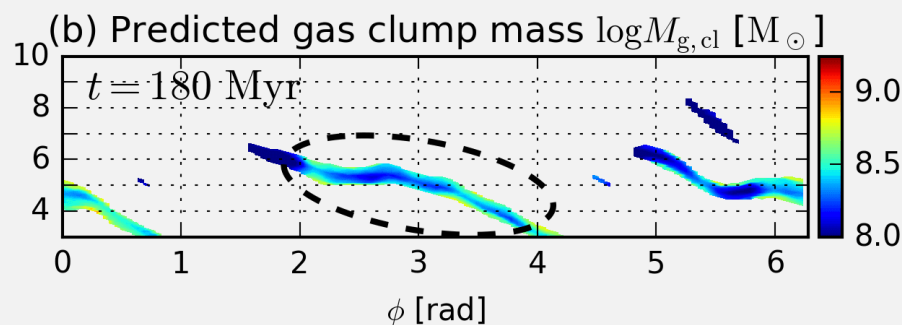
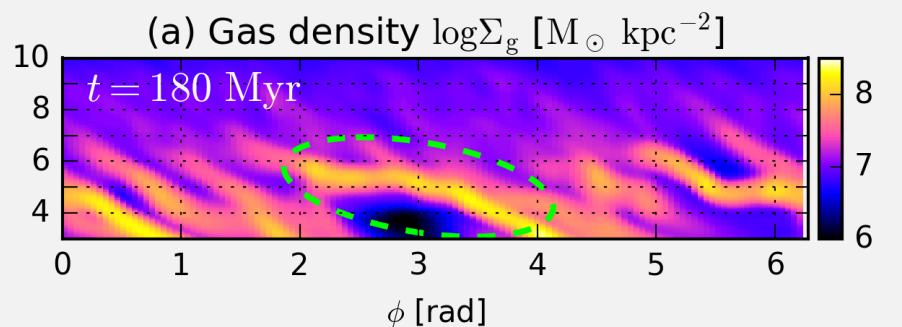
# Clump-mass prediction

- $M_{cl} \sim \Sigma W \lambda$
- $M_{cl} \sim 10^8 - 10^{8.5} M_{\odot}$  (predicted)



# Clump-mass prediction

- $M_{cl} \sim \Sigma W \lambda$
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# Toomre Instability (TI)

(e.g. Dekel et al. 2009)

**V.S.**

# Spiral-Arm Instability (SAI)

(Inoue & Yoshida 2017)

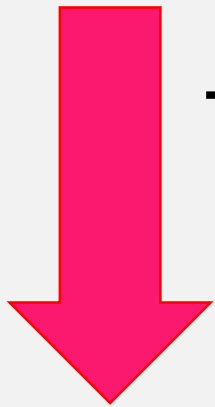
For low- $z$  clumpy galaxies



# TI vs SAI

- Toomre Instability

Disc formation



Toomre instability  
 $Q < 1$

Giant clump formation

- Spiral-Arm Instability

Disc formation



Toomre instability and/or  
swing amplification

Spiral arm formation

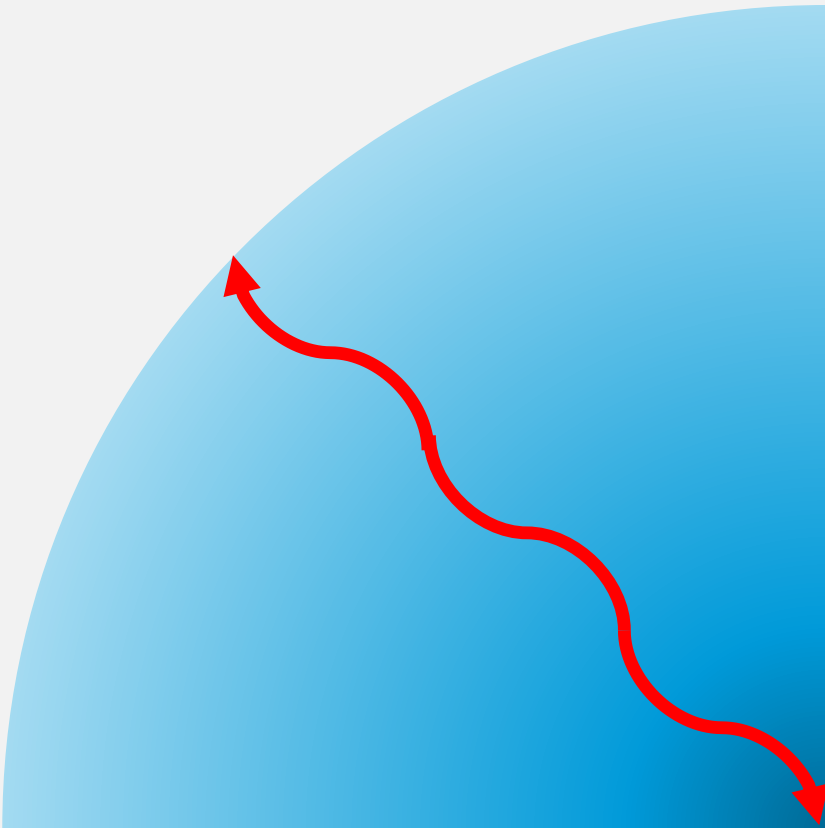


**Spiral-Arm Instability**  
 $S < 1$

Giant clump formation

# TI vs SAI

- Toomre Instability



- Spiral-Arm Instability

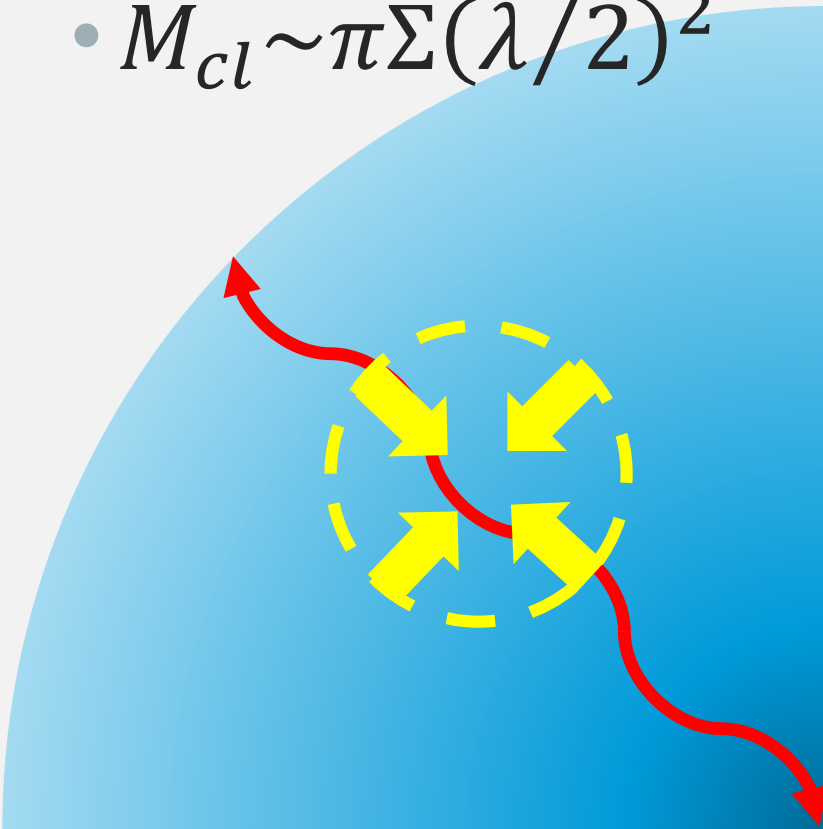


# TI vs SAI

- Toomre Instability

- **2D collapse**

- $M_{cl} \sim \pi \Sigma (\lambda/2)^2$



- Spiral-Arm Instability

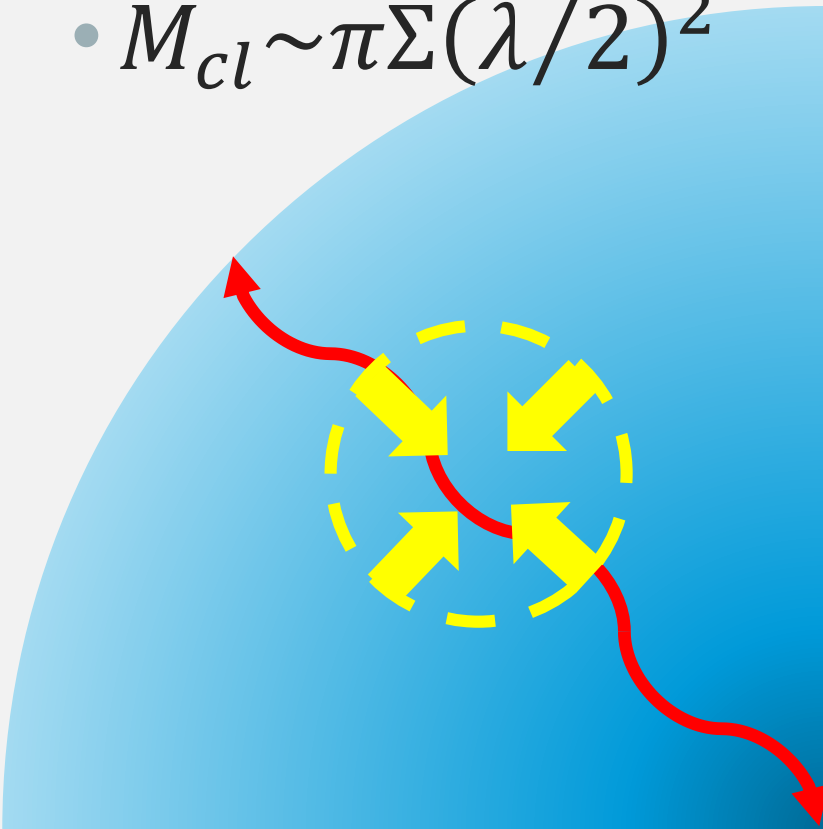


# TI vs SAI

- Toomre Instability

- **2D collapse**

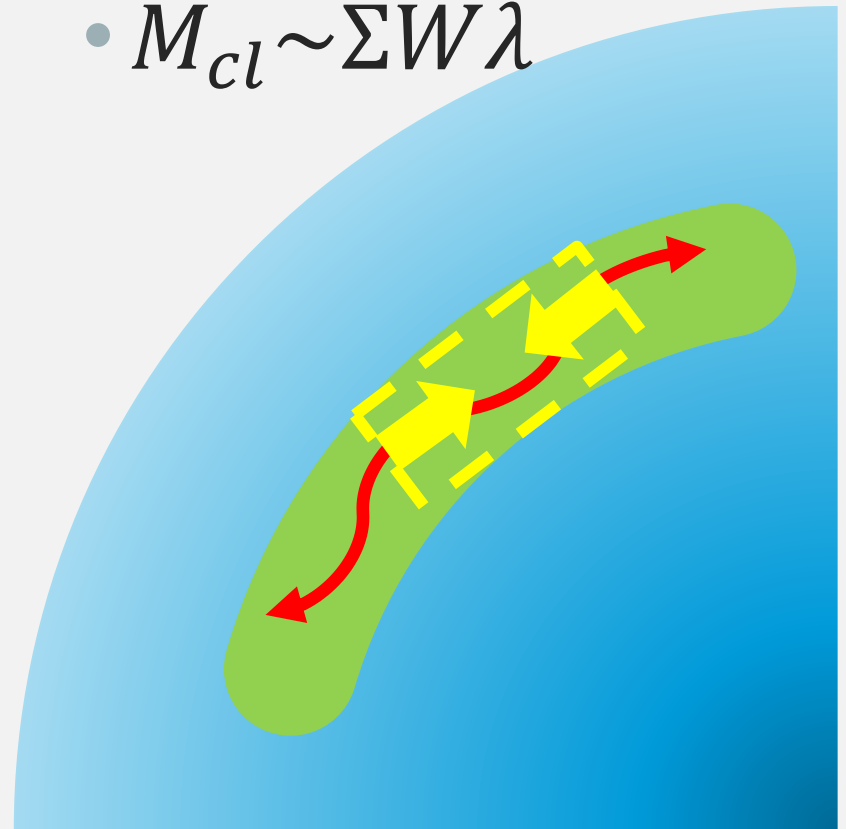
- $M_{cl} \sim \pi \Sigma (\lambda/2)^2$



- Spiral-Arm Instability

- **1D collapse**

- $M_{cl} \sim \Sigma W \lambda$

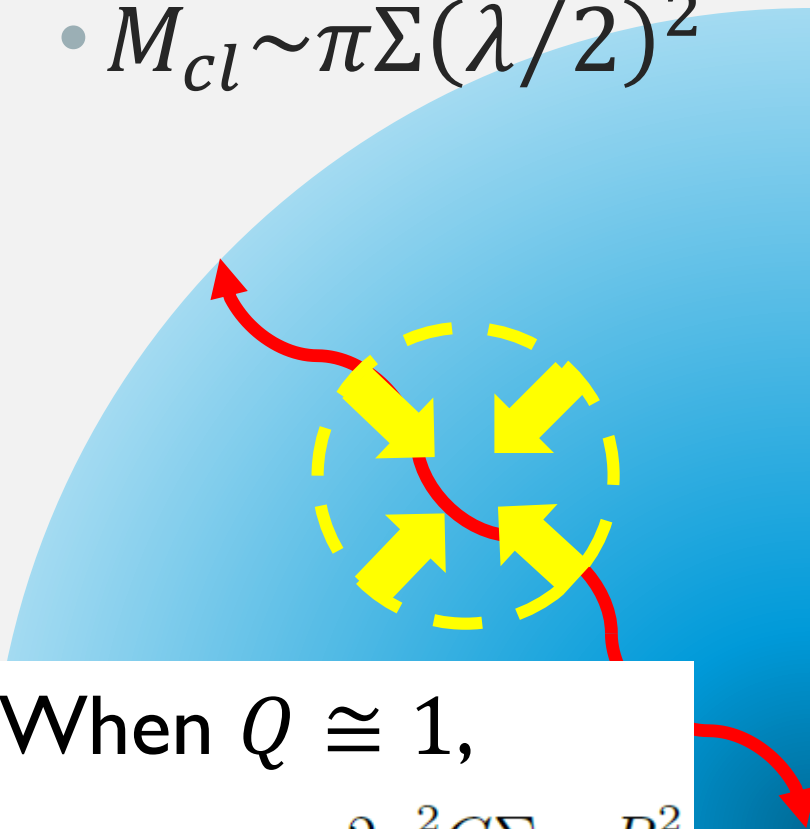


# TI vs SAI

- Toomre Instability

- **2D collapse**

- $M_{cl} \sim \pi \Sigma (\lambda/2)^2$



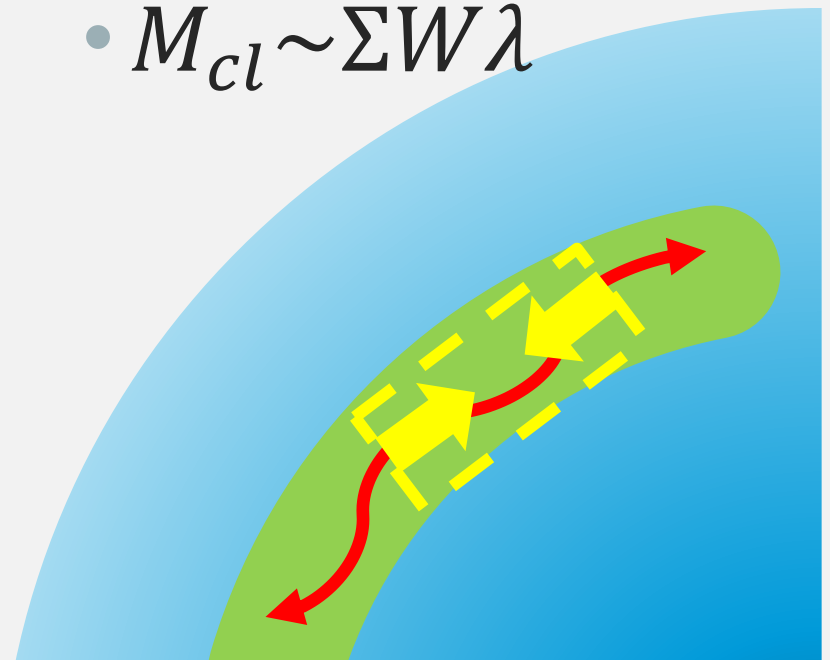
When  $Q \cong 1$ ,

$$\lambda_{\text{MU}} \simeq \frac{2\pi^2 G \Sigma_{\text{g,d}} R_{\text{d}}^2}{a^2 V^2}$$

- Spiral-Arm Instability

- **1D collapse**

- $M_{cl} \sim \Sigma W \lambda$



When  $S \cong 1$ ,

$$\lambda_{\text{MU}} = 2\pi \left( \frac{\pi \alpha G F_0 A \Sigma W^{1-\alpha}}{8\Omega^2} \right)^{\frac{1}{2-\alpha}}$$

# Scaling relations of high-z clumps

- From our analysis, we can obtain scaling relations of properties of giant clumps.

$$\sigma_{\text{cl}}^2 \simeq \frac{16}{3} (\pi\epsilon)^{\alpha-3} (\alpha F_0 f_g)^{-1} \left( \frac{W^{\alpha/2} R_{\text{cl}}^{1-\alpha/2}}{R_d} V \right)^2$$

**Spiral-arm instability**  
expected scaling relation:

$$R_{\text{cl}} \propto \left( \frac{\sigma_{\text{cl}}}{V} R_d \right)^{1.3}$$

$$\sigma_{\text{cl}}^2 \simeq \frac{a^2}{3\pi\epsilon^3 f_g} V^2 \left( \frac{R_{\text{cl}}}{R_d} \right)^2$$

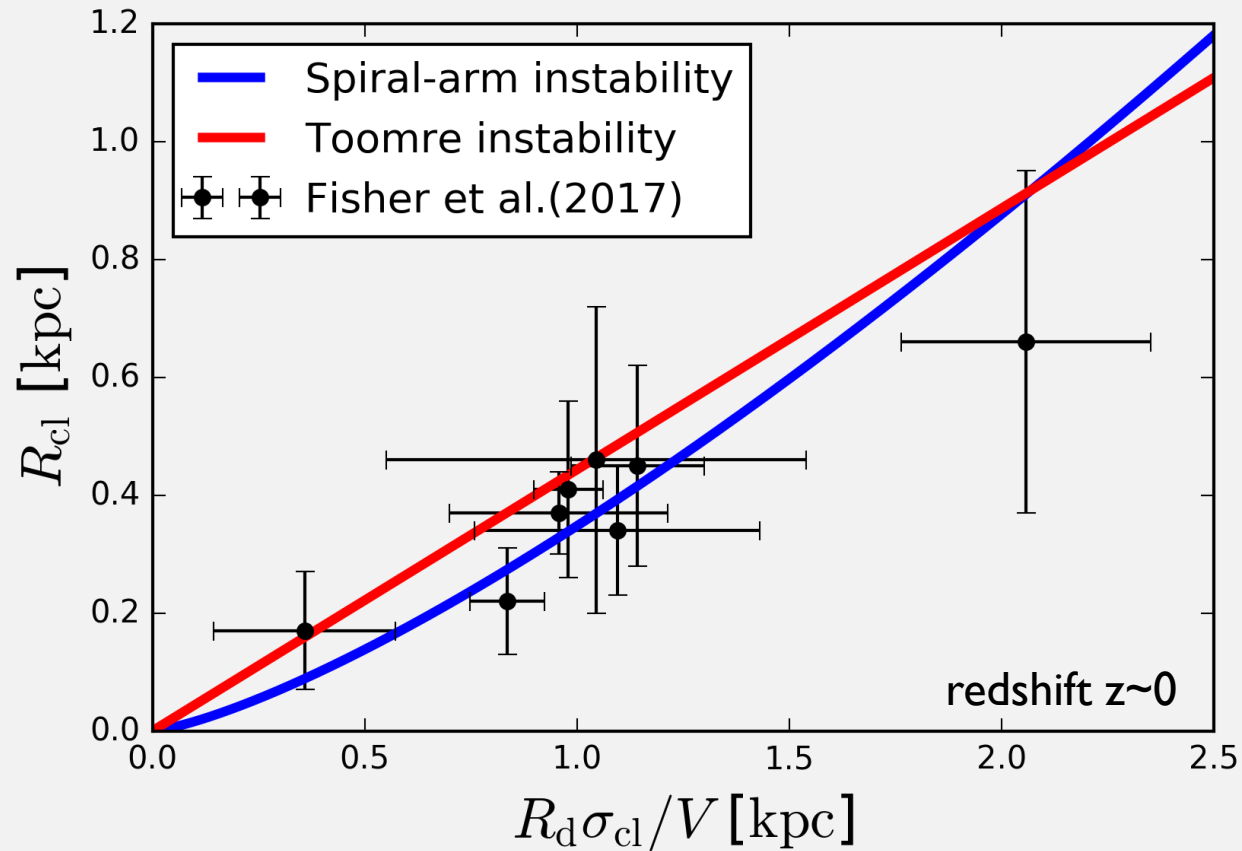
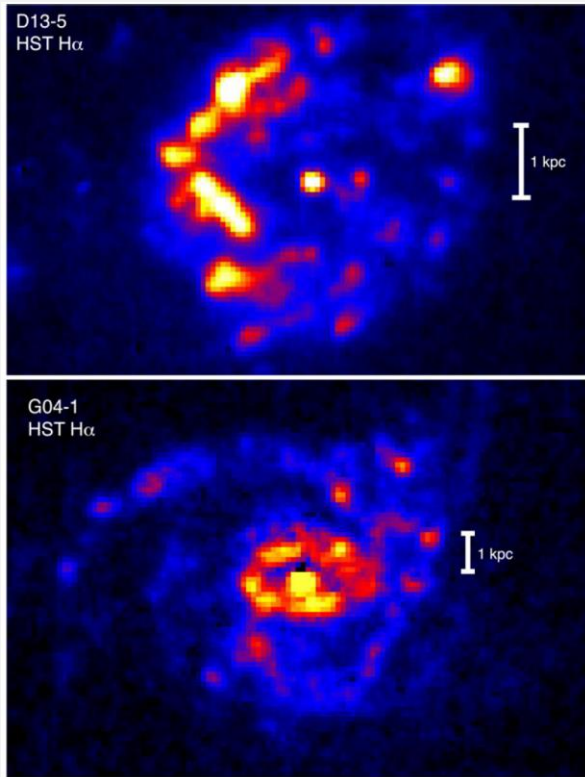
**Toomre instability**  
expected scaling relation:

$$R_{\text{cl}} \propto \frac{\sigma_{\text{cl}}}{V} R_d$$

$R_{\text{cl}}$ : clump radius,       $\sigma_{\text{cl}}$ : vel. disp. with in clump,       $R_d$ : disc radius,       $V$ : disc rot. vel.



# Scaling relations of high-z clumps



Data from Fisher+17: DYNAMO

- Neither model is rejected by the observations.

# Scaling relations of high-z clumps

- From our analysis, we can obtain scaling relations of properties of giant clumps.

$$\frac{M_{\text{cl}}}{M_{\text{d,g+s}}} \simeq 2 \left[ \frac{1}{8} \alpha F_0 (A\beta)^{3-\alpha} \eta \left( \frac{W}{R_{\text{d}}} \right)^{3-2\alpha} \right]^{\frac{1}{2-\alpha}}$$

**Spiral-arm instability**  
expected scaling relation:  $\frac{M_{\text{g,cl}}}{M_{\text{g,d}}} \propto f_{\text{g}}^{0.7} R_{\text{d}}^{-1.3},$

$$\frac{M_{\text{cl}}}{M_{\text{d,g+s}}} \simeq \pi^2 a^{-4} \eta^2.$$

$\eta \approx f_{\text{g}}$  : gas fraction including DM

**Toomre instability**  
expected scaling relation:  $\frac{M_{\text{g,cl}}}{M_{\text{g,d}}} \propto f_{\text{g}}^2,$

$R_{\text{cl}}$ : clump radius,

$\sigma_{\text{cl}}$ : vel. disp. with in clump,

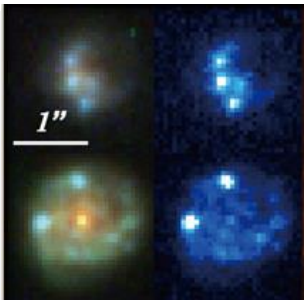
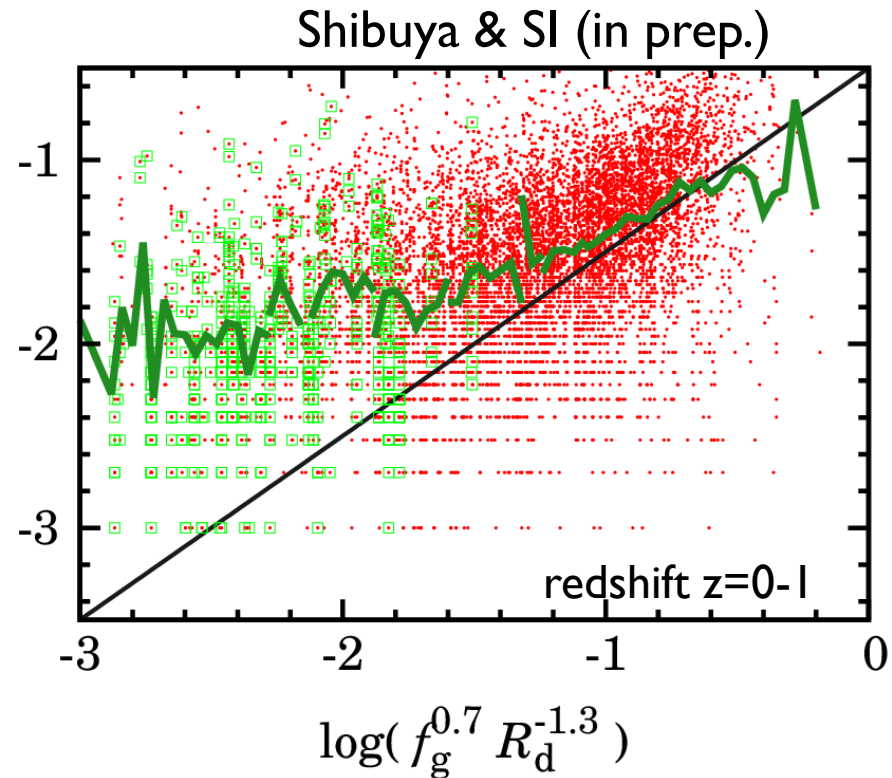
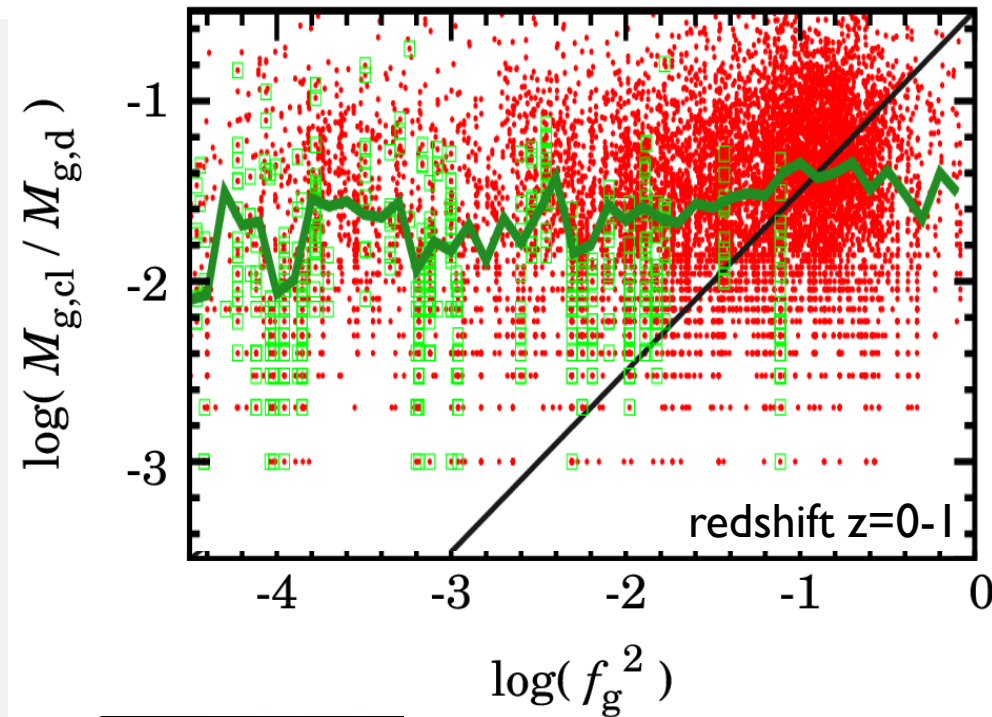
$R_{\text{d}}$ : disc radius,

$V$ : disc rot. vel.

# Scaling relations of high-z clumps

- Toomre Instability

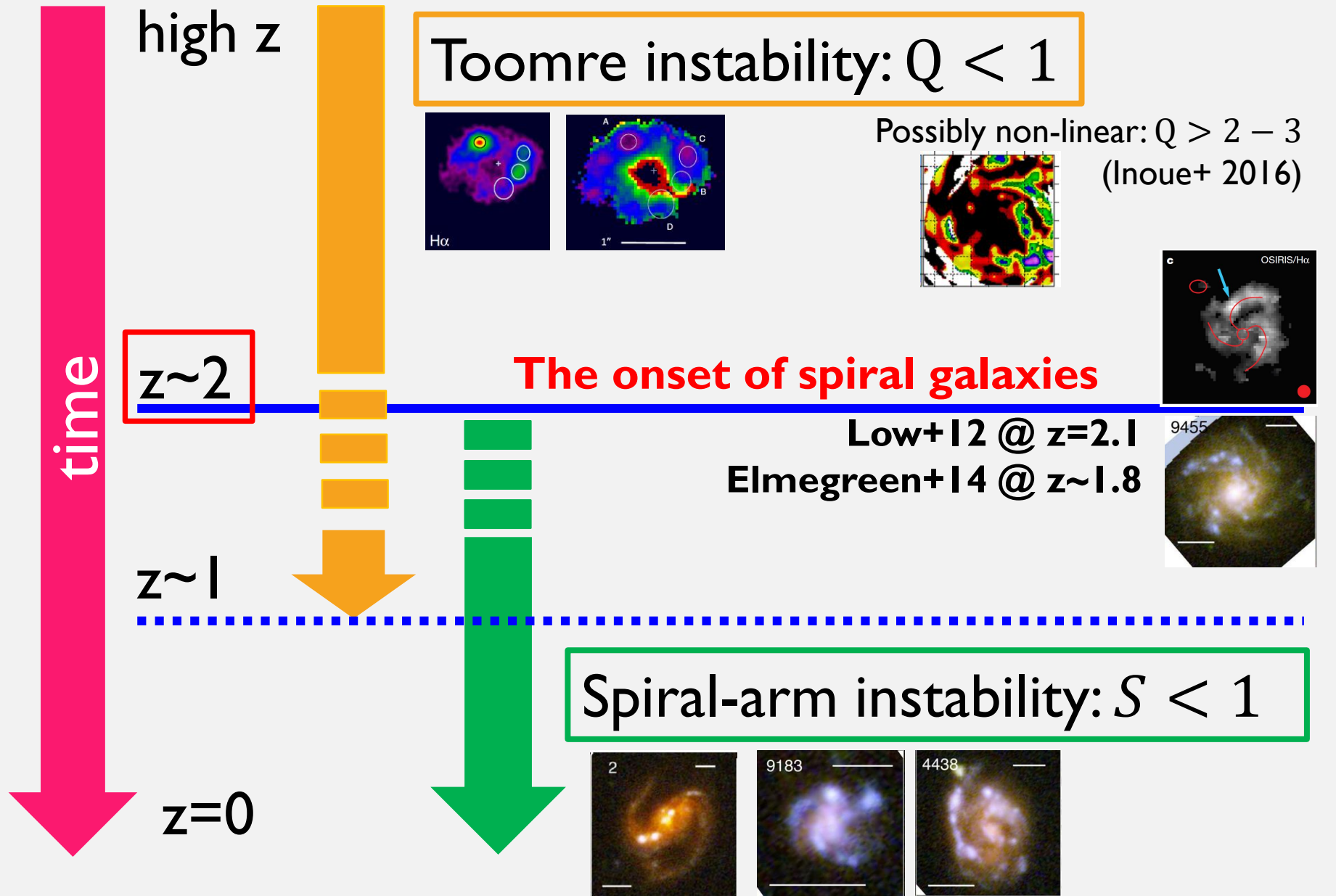
- Spiral-Arm Instability



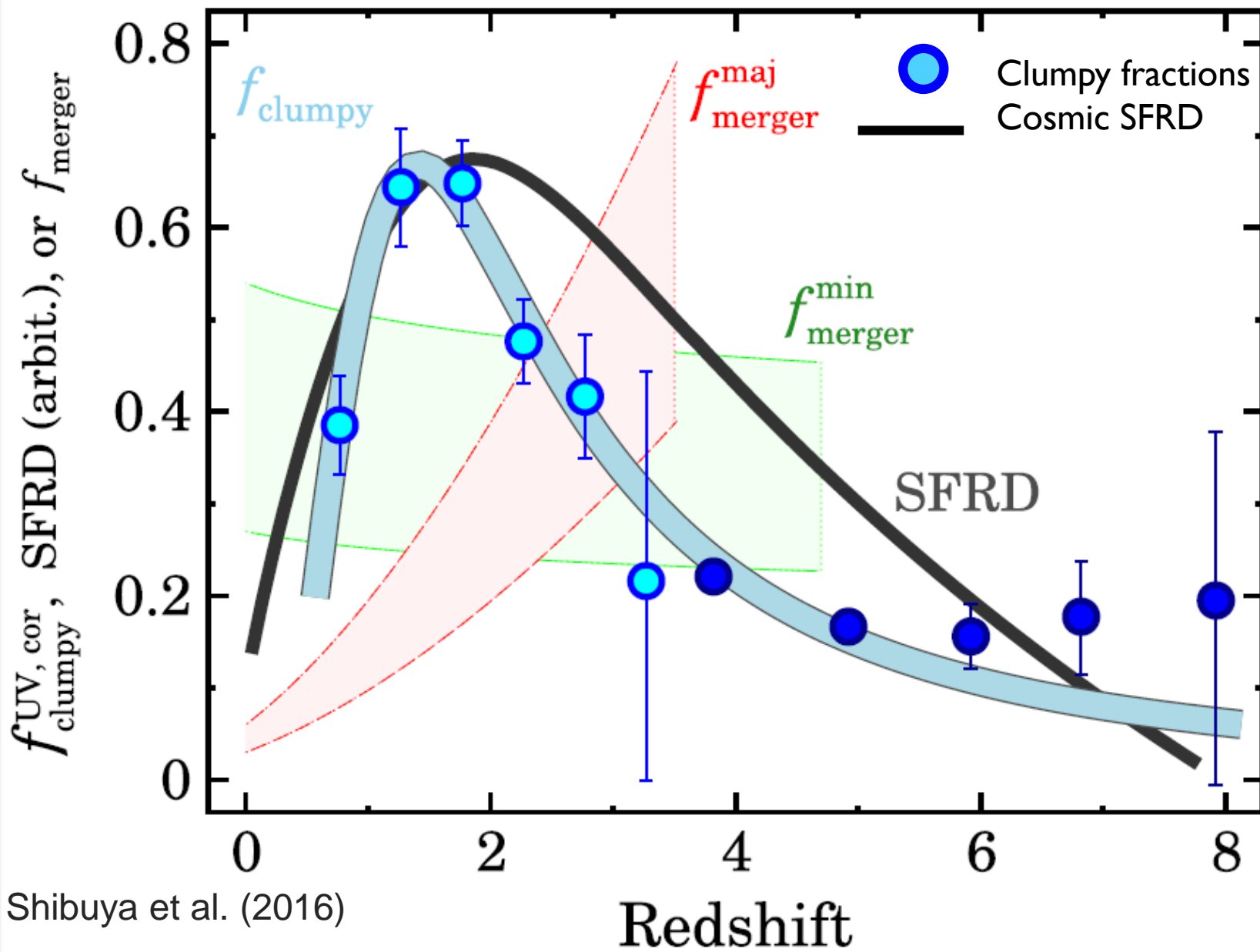
Data from Shibuya+I6: HST @  $z=0-1$

- Our SAI model appears better consistent with the observations of  $M_{cl}/M_d \sim 10\%$  clumps.

# Transition of the clump formation mechanisms

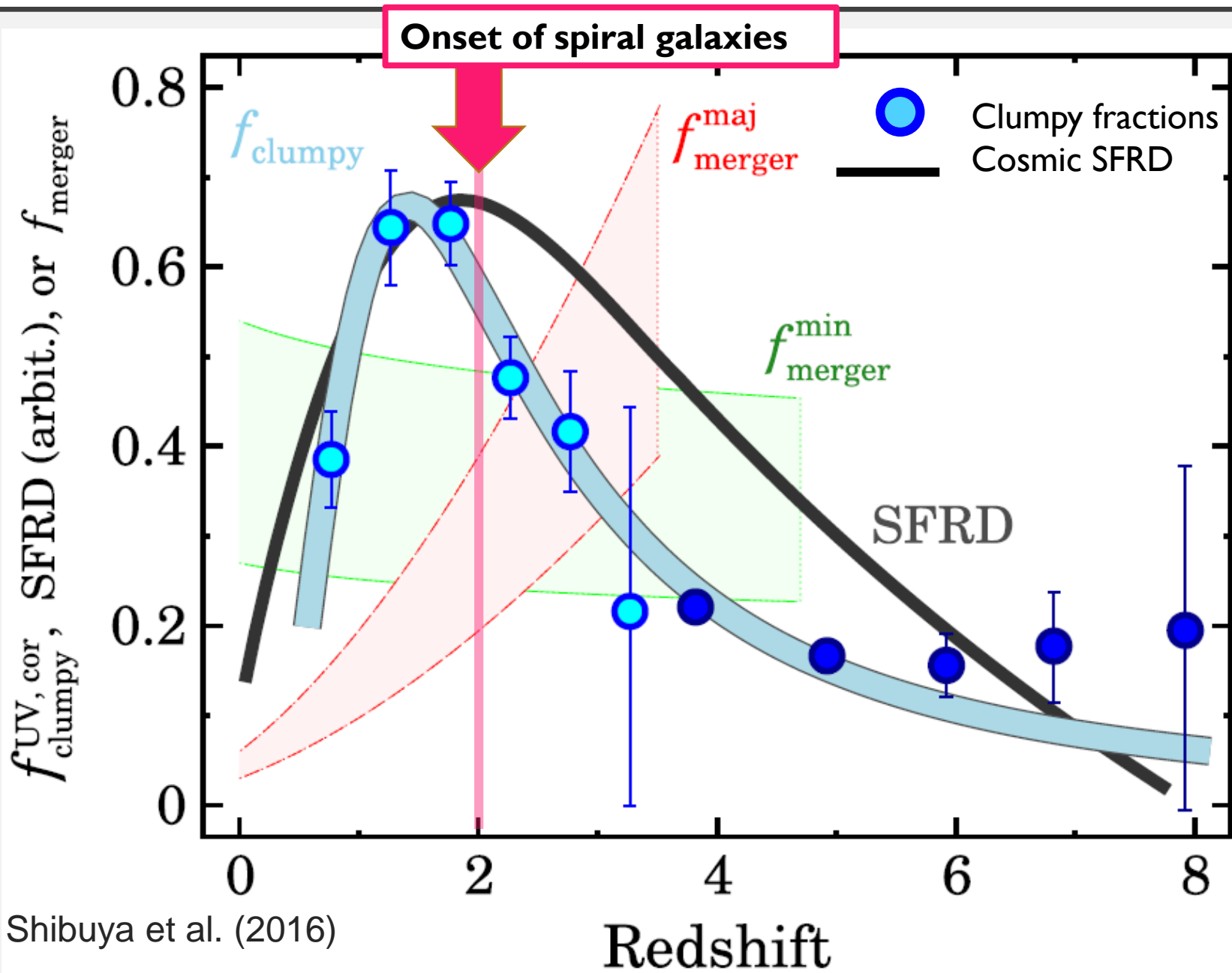


# Clumpy fraction and cosmic SFR



- Shibuya et al. (2016)

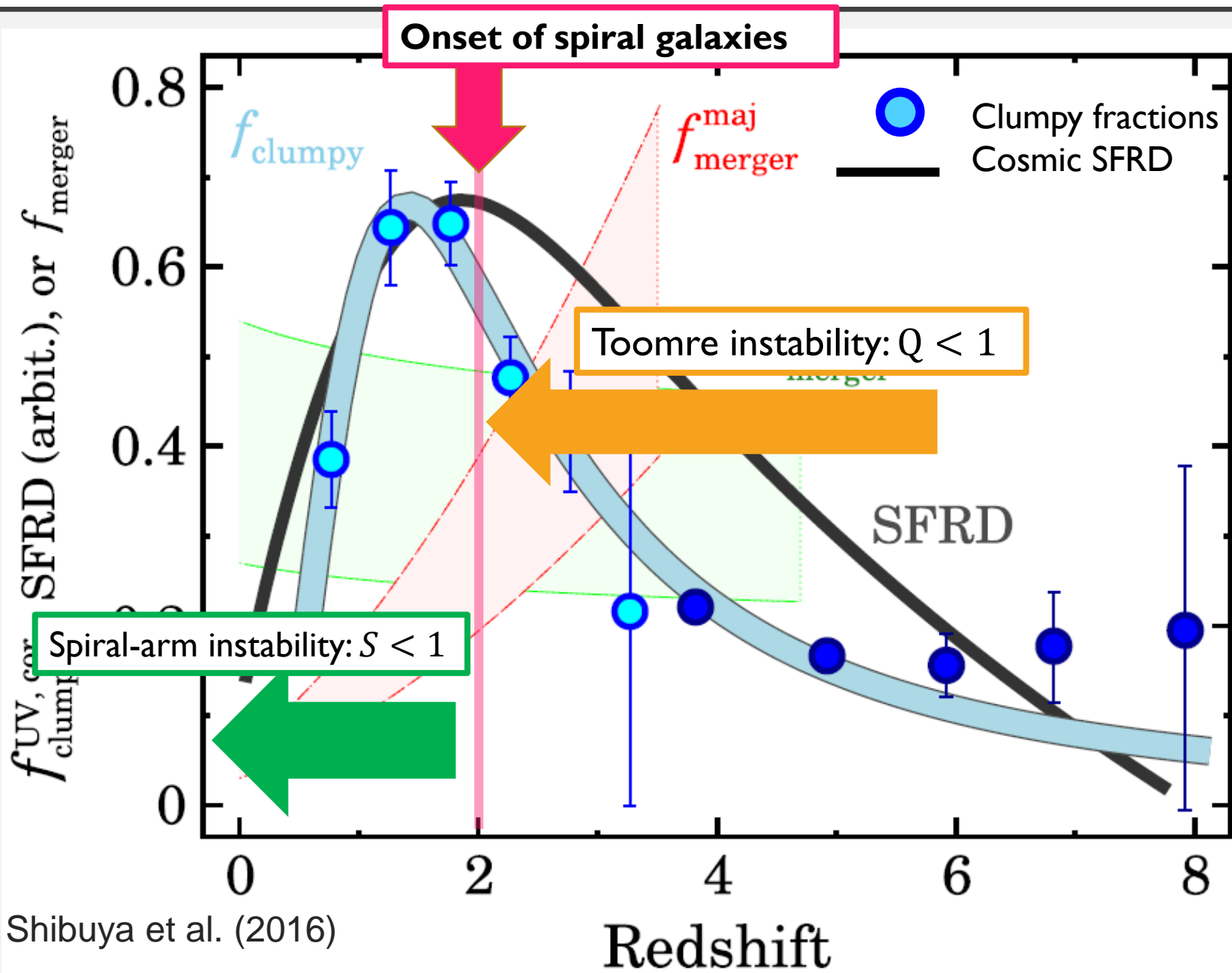
# Clumpy fraction and cosmic SFR



- Shibuya et al. (2016)



# Clumpy fraction and cosmic SFR



- Shibuya et al. (2016)

# Summary

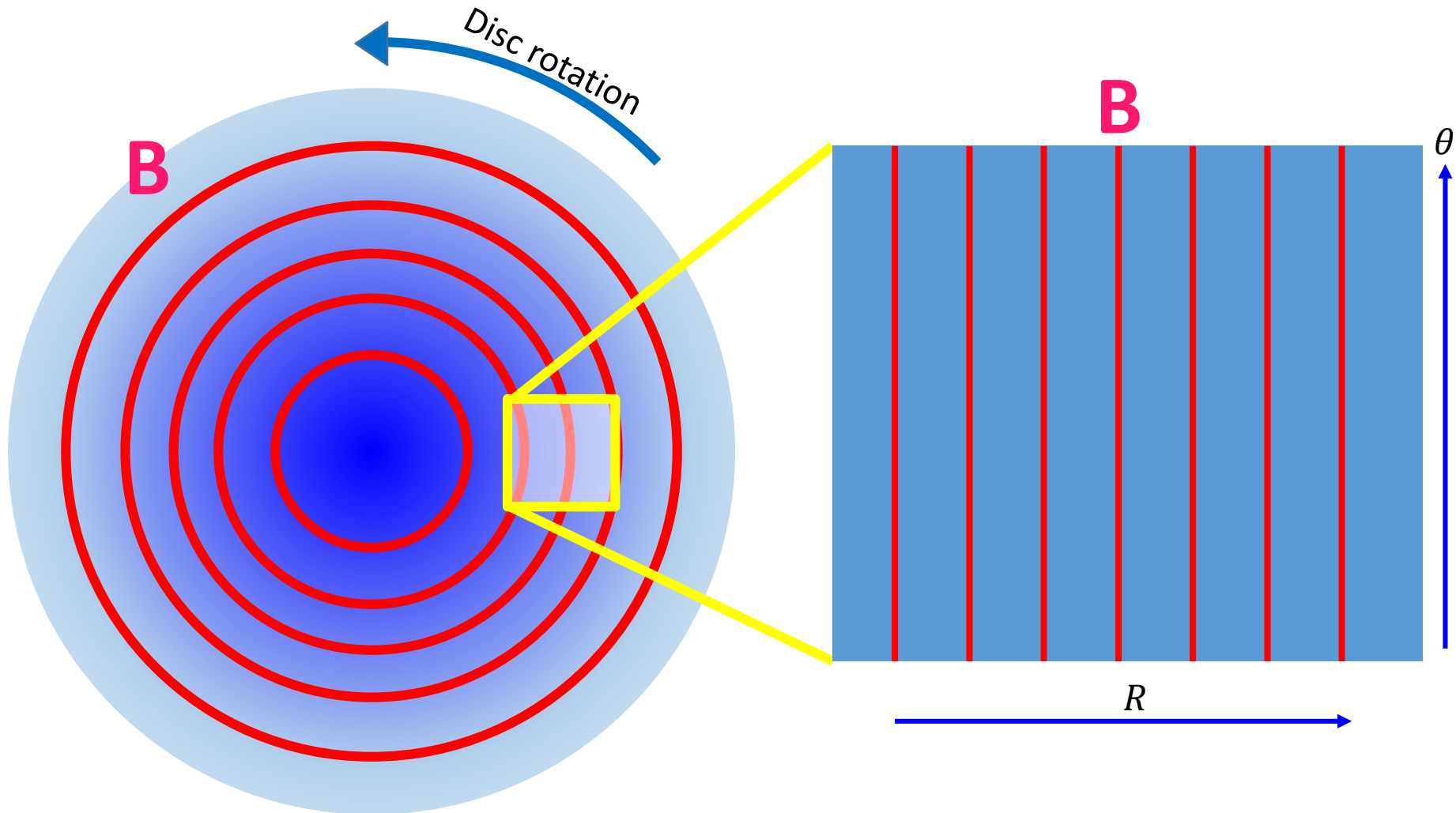
- Our SAI model appears better consistent with the low-z observations.
- The TI model cannot reproduce the scaling relation of the observations despite that the TI model relays on fewer assumptions than our SAI model.
- There could be transition of clump formation mechanisms
  - @  $z=2\sim 1$ , from Toomre instability to spiral-arm instability

**See arXiv: 1706.01895**

A little about magnetic fields  
for Toomre and spiral-arm instabilities

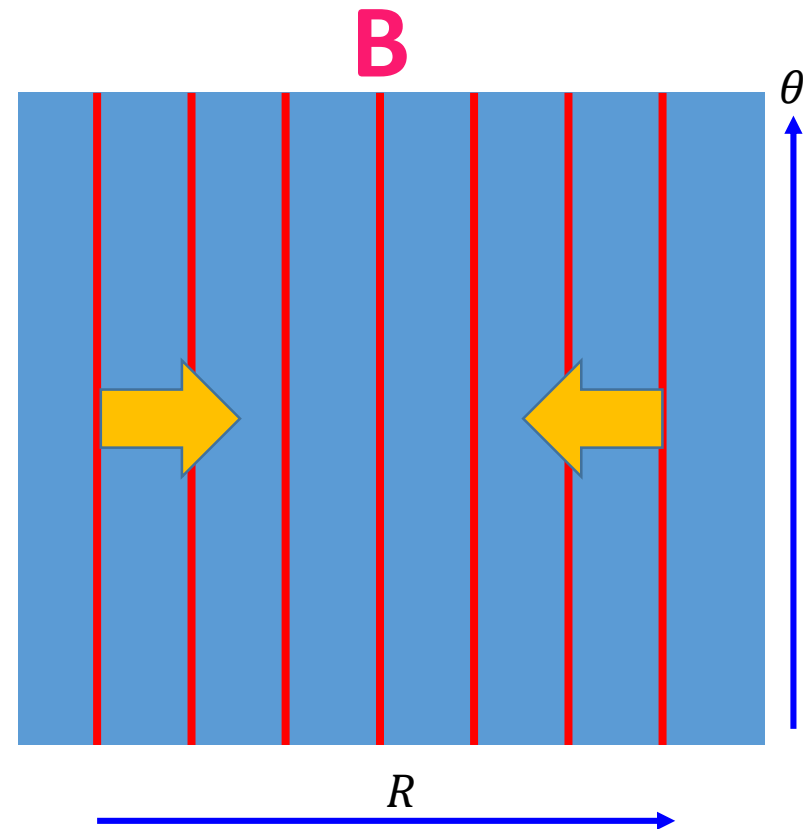
# Toroidal magnetic fields in a disc galaxy

- The Galactic B-fields are approximately toroidal (Rand & Kulkarni 1989).
- $B_\theta \sim 1 \mu\text{G}$  (e.g. Inoue & Tabara 1981, Mouschovias 1983, ).



# Toroidal magnetic fields in a disc galaxy

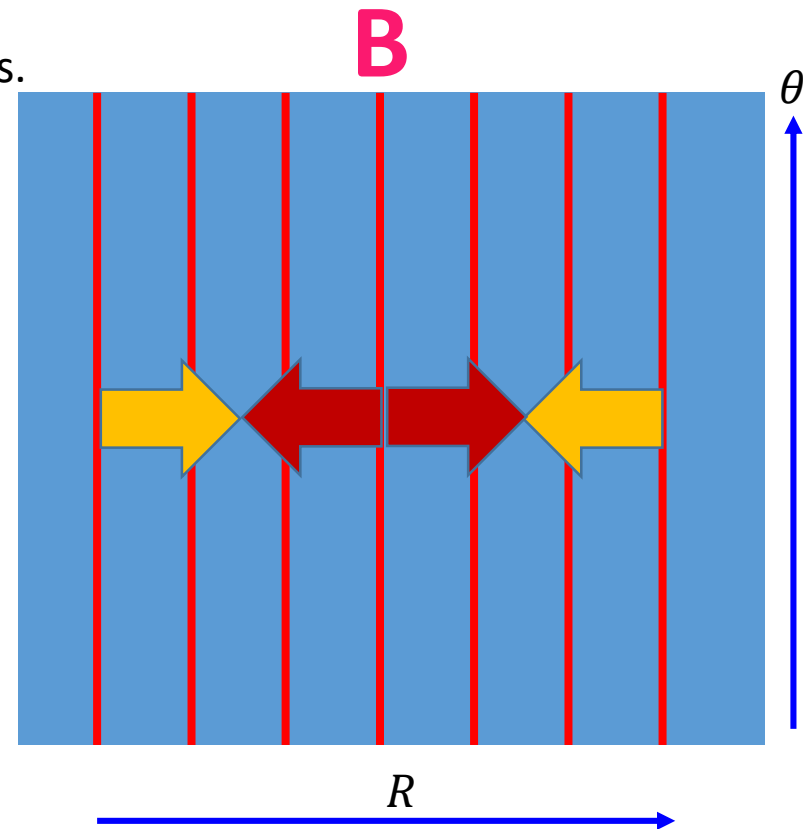
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- Radial perturbations
  - The B-fields work against the perturbations.

Azimuthal B-fields can stabilize azimuthal perturbations by magnetic pressure.

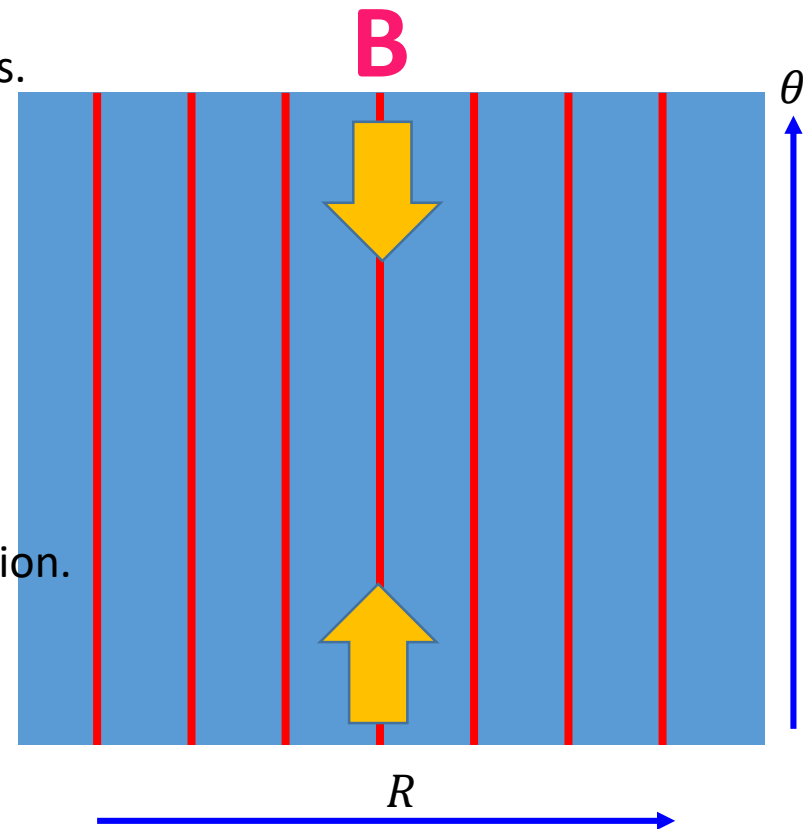


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  - The B-fields do nothing in azimuthal direction.





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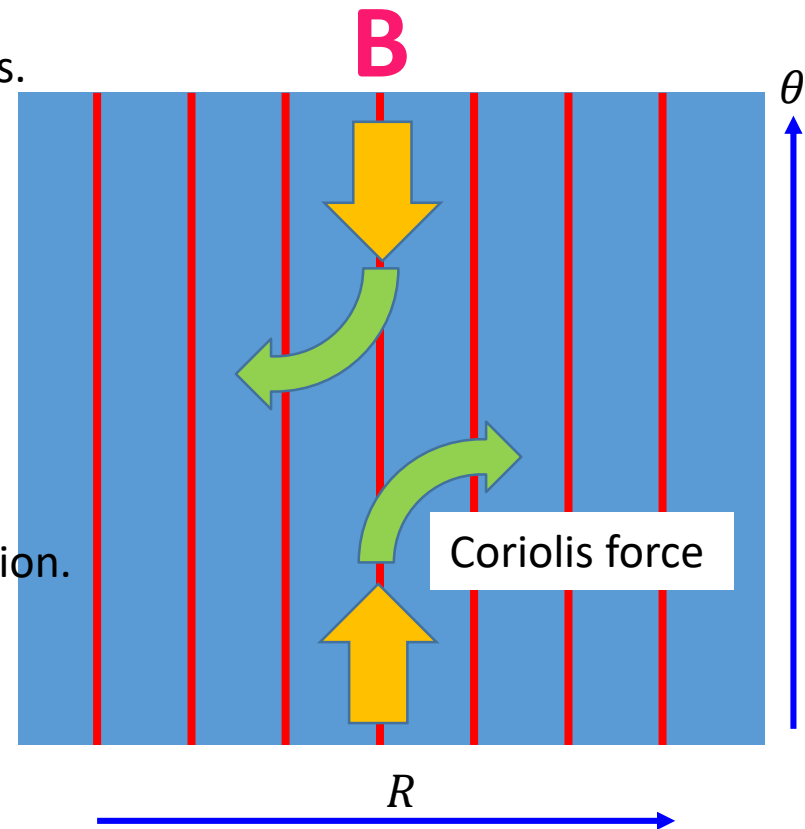
- Radial perturbations

- The B-fields work against the perturbations.

Azimuthal B-fields can stabilize azimuthal perturbations by magnetic pressure.

- Azimuthal perturbations

- The B-fields do nothing in azimuthal direction.
  - But, work against Coriolis force.



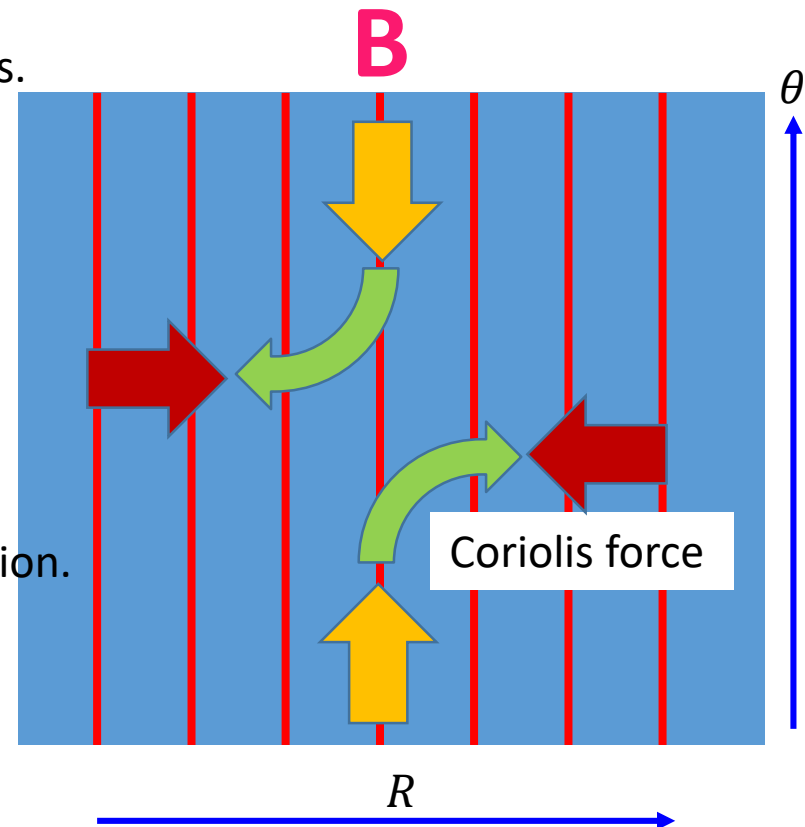
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- Azimuthal perturbations
  - The B-fields do nothing in azimuthal direction.
  - But, work against Coriolis force.

Azimuthal B-fields can destabilize azimuthal perturbations by cancelling Coriolis force.



# Toroidal magnetic fields in a disc galaxy

- The Galactic B-fields are approximately toroidal (Rand & Kulkarni 1989).
- $B_\theta \sim 1 \mu\text{G}$  (e.g. Inoue & Tabara 1981, Mouschovias 1983, ).

- Radial perturbations: **Toomre instability**

- The B-fields work against the perturbations.

Dispersion relation:  $\omega^2 = (c_s^2 + \underline{v_A^2})k^2 - 2\pi G\Sigma k + \kappa^2.$

(modified) Toomre Q:  $Q' = \frac{\kappa \sqrt{c_s^2 + v_A^2}}{\pi G\Sigma}.$

- Azimuthal perturbations: **Spiral-arm instability**

- The B-fields do nothing in azimuthal direction.
- But, work against Coriolis force.

Dispersion relation:  $\omega^2 = [c_s^2 - \pi G\delta\Upsilon f(kW)] k^2 + \frac{4\Omega^2\omega^2}{\omega^2 + \underline{k^2 v_A^2}}.$

# Ideal MHD simulation

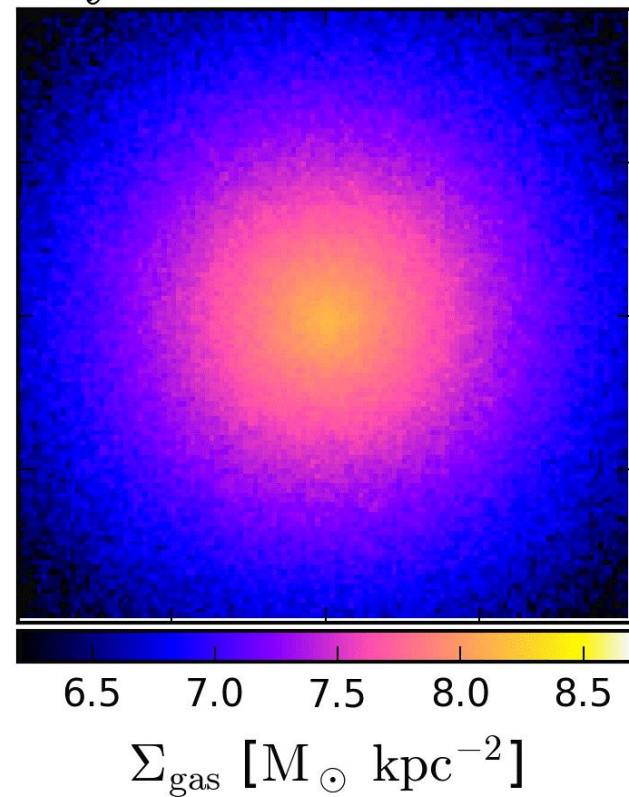
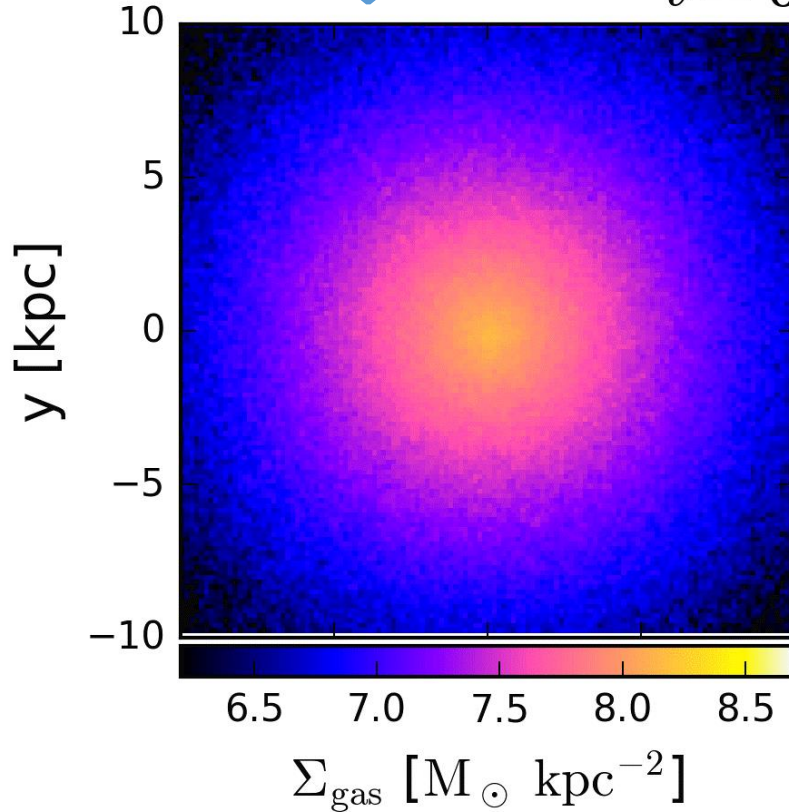
- Gas + stellar discs ( $f_{gas} = 0.2$ , isothermal gas)

- Initial conditions  $Q' = \frac{\kappa \sqrt{c_s^2 + v_A^2}}{\pi G \Sigma} \simeq 1.5$ .

$$\frac{c_s^2}{v_A^2} = 2, \quad B_\theta \sim 10 \mu\text{G}$$

No magnetic fields

$t = 0000$  Myr



# Summary

- Assuming toroidal magnetic fields,
  - The magnetic fields can suppress growth of radial perturbations.
    - Toomre instability can be mitigated.
  - The magnetic fields can enhance growth of azimuthal perturbations.
    - By cancelling Coriolis force
    - Therefore, spiral-arms can be destabilized by the magnetic fields.
- **Giant-clump formation by spiral-arm fragmentation can be enhanced in toroidal magnetic fields in a spiral galaxy.**