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# Approach to Nucleation in Astronomical Environments

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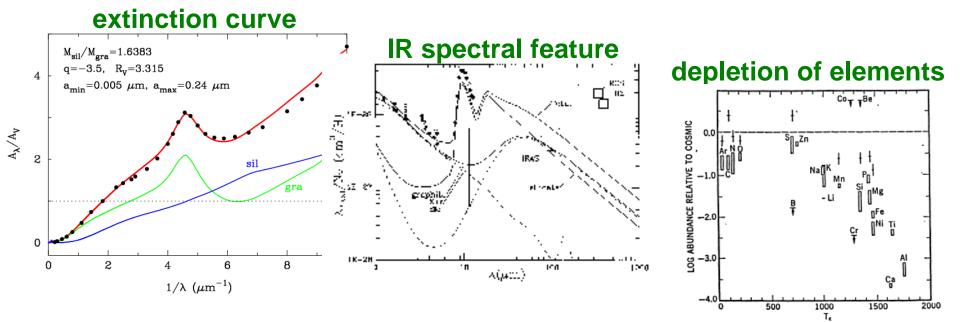
#### **1-1. Introduction**

Cosmic dust universally exits in space

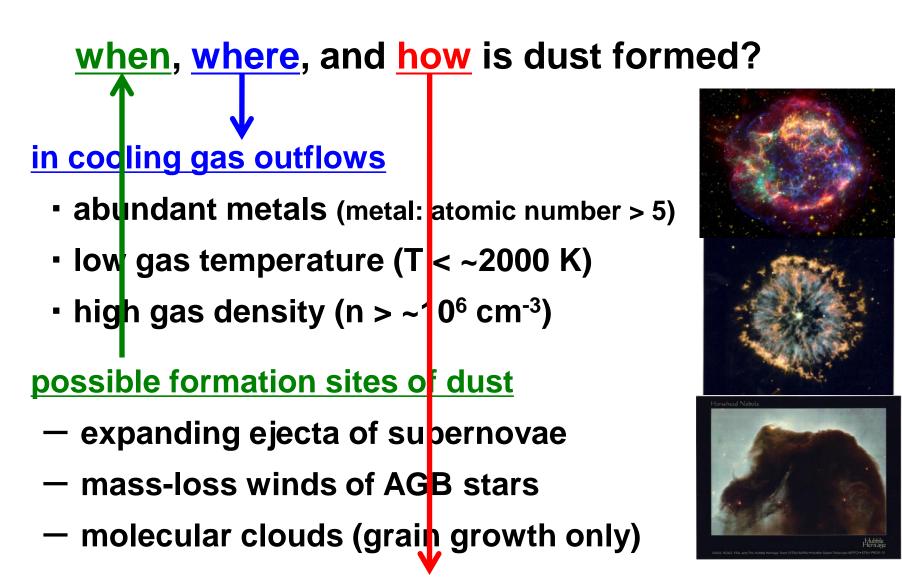
when, where, and how is dust formed?

Properties of dust evolves through the processing in the ISM (sputtering, shattering, coagulation, growth ..)

composition, size, and amount of newly formed dust

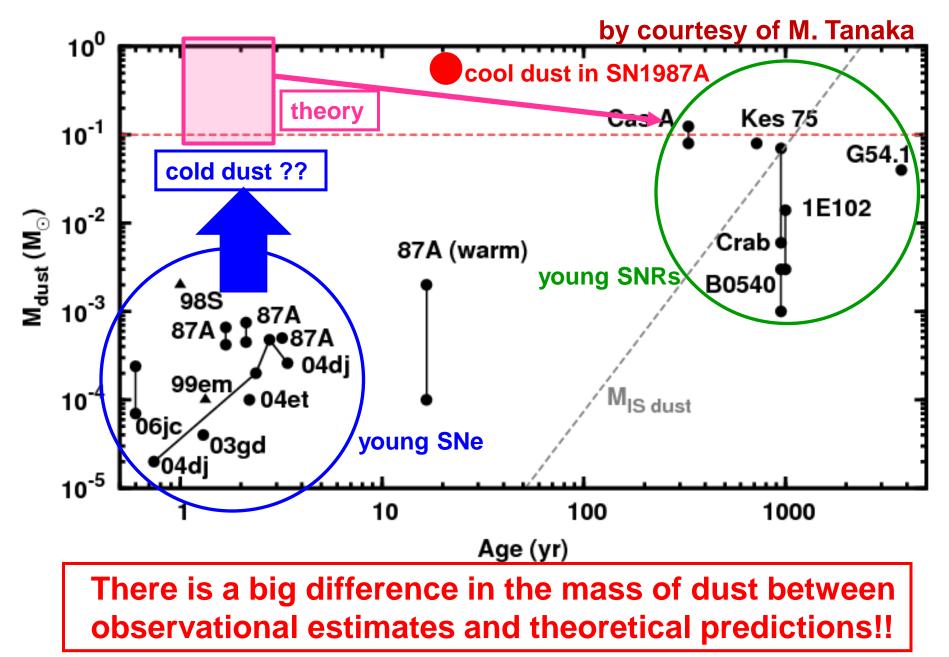


## **1-2. Formation sites of dust**

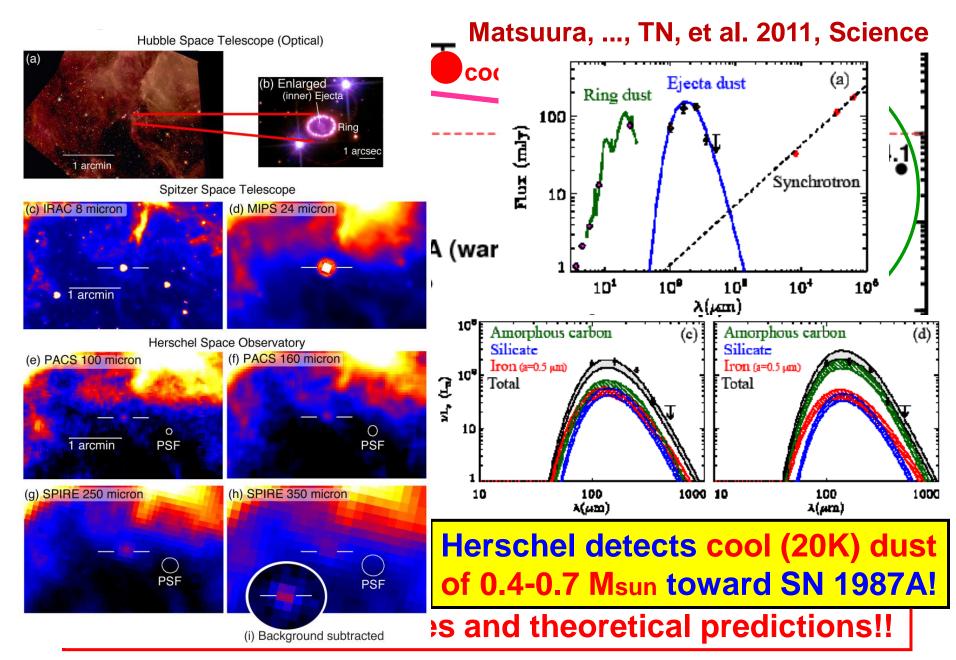


what kinds of, what size of, how much dust is formed

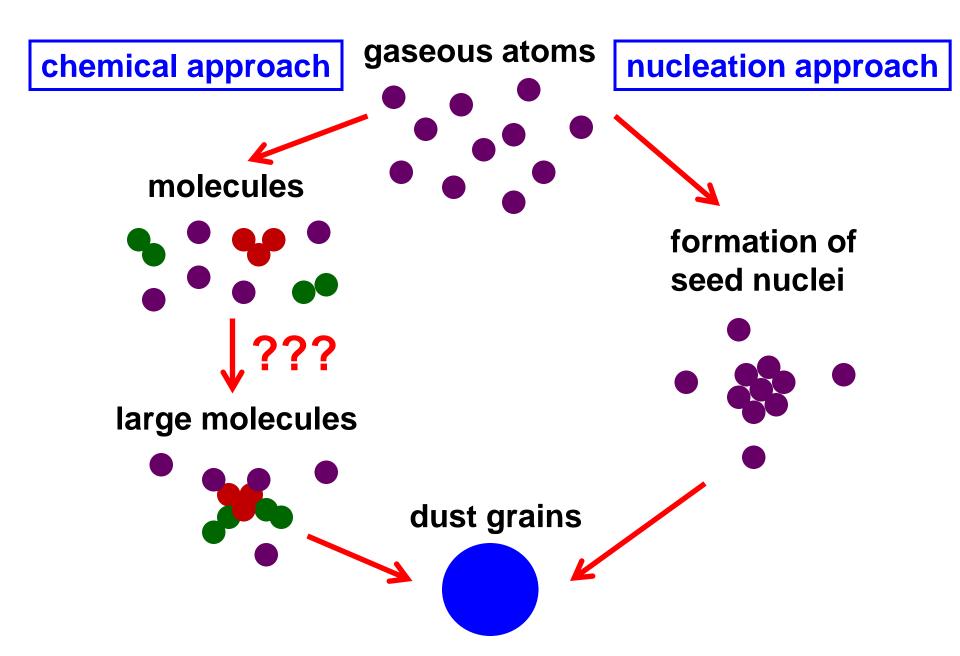
#### **1-3. Missing-dust problem in CCSNe**

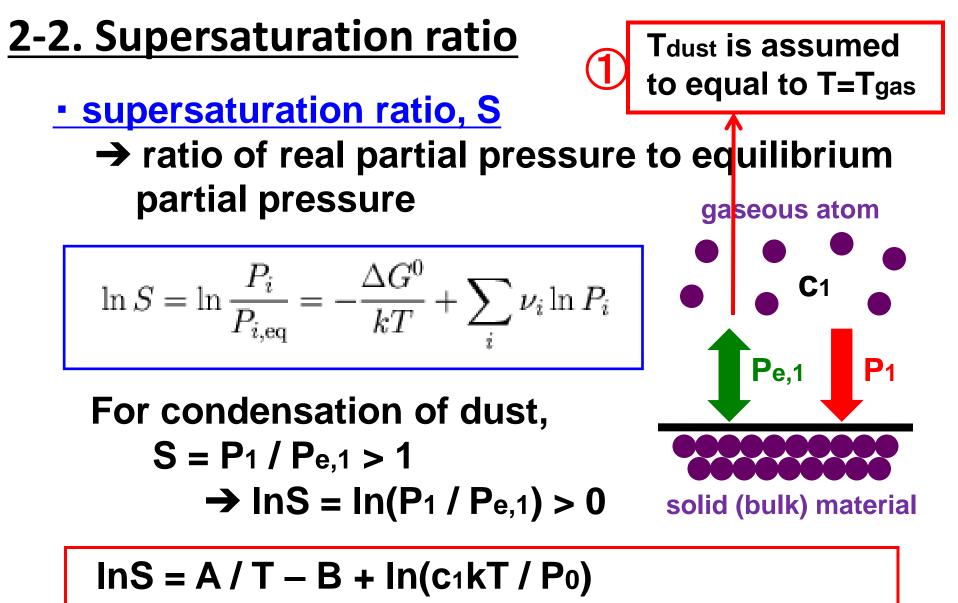


#### **1-3. Missing-dust problem in CCSNe**



#### **2-1. How do dust grains form?**

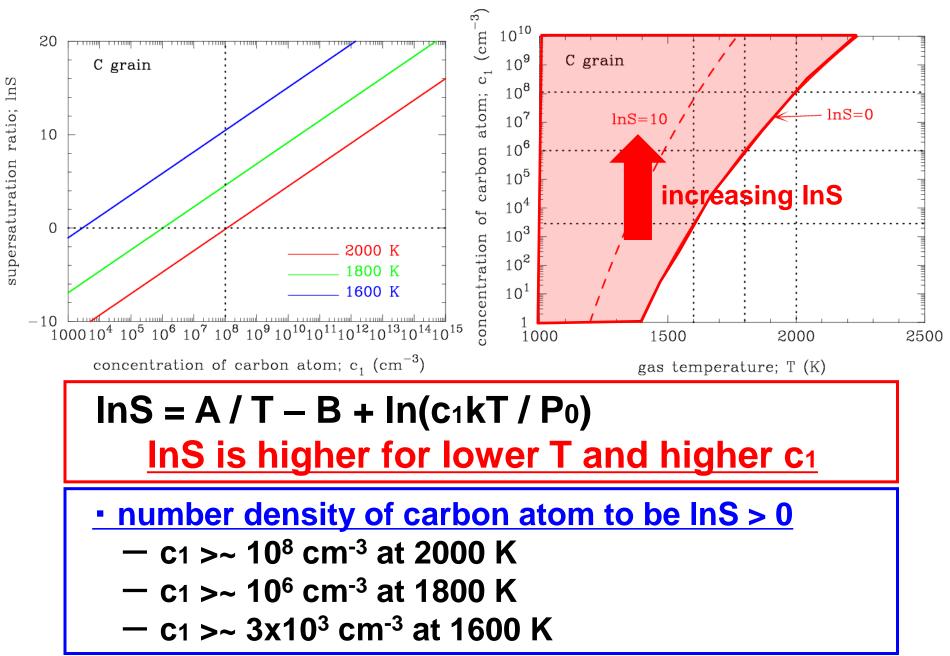




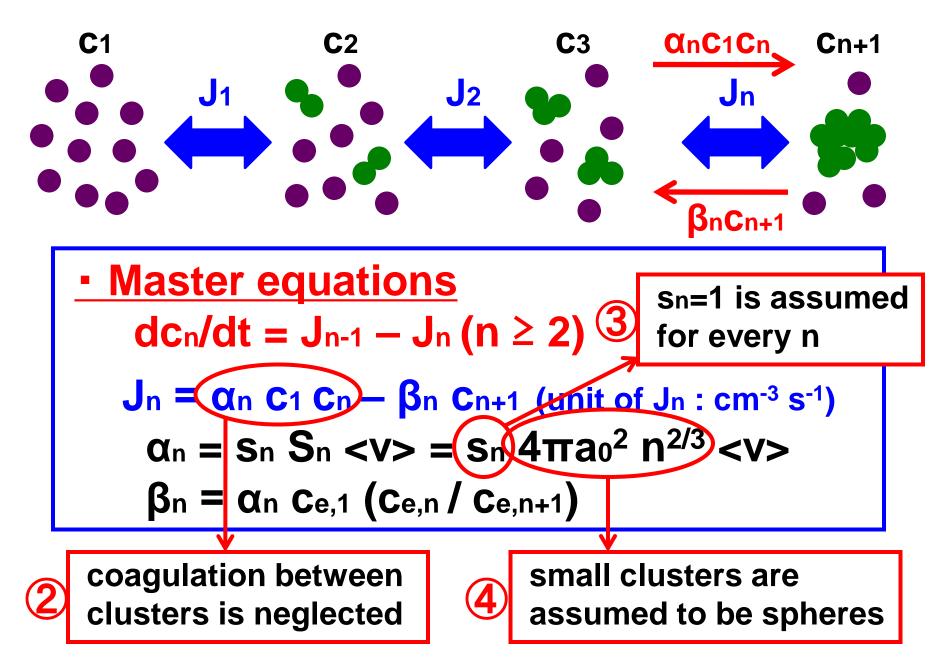
where  $-\Delta G^0/kT = A/T - B$  (A=8.64x10<sup>4</sup>, B=19 for C grains)

InS is higher for lower T and higher c1

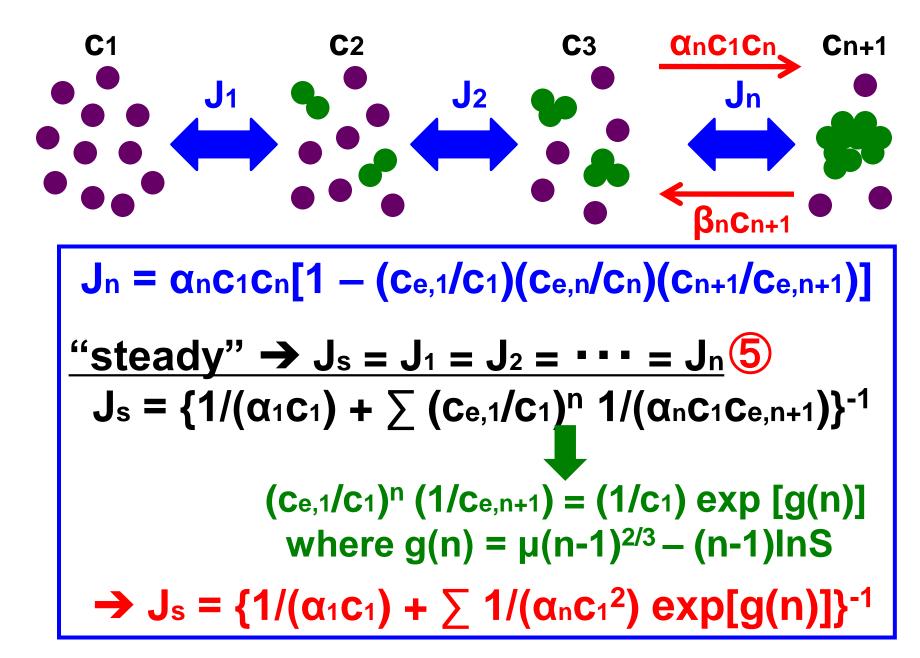
#### **2-3. Behavior of supersaturation ratio**



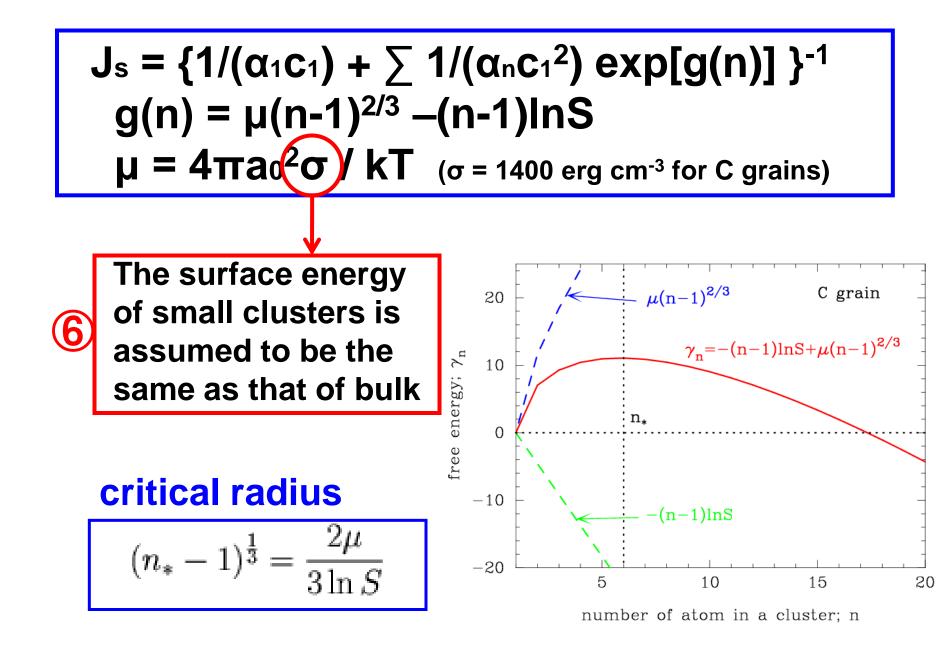
### **3-1. Concept of nucleation**



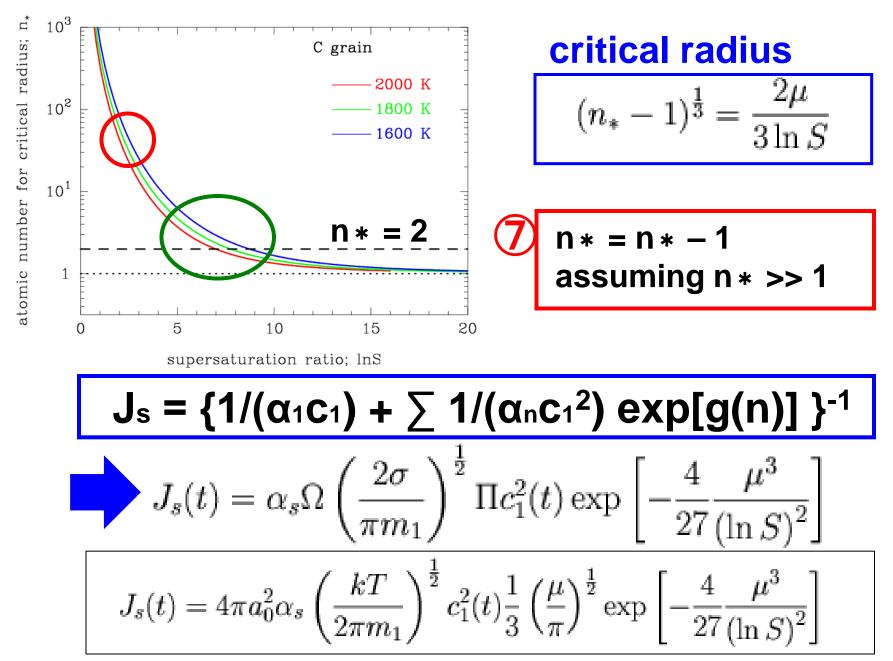
#### **3-2. Steady-state nucleation rate**



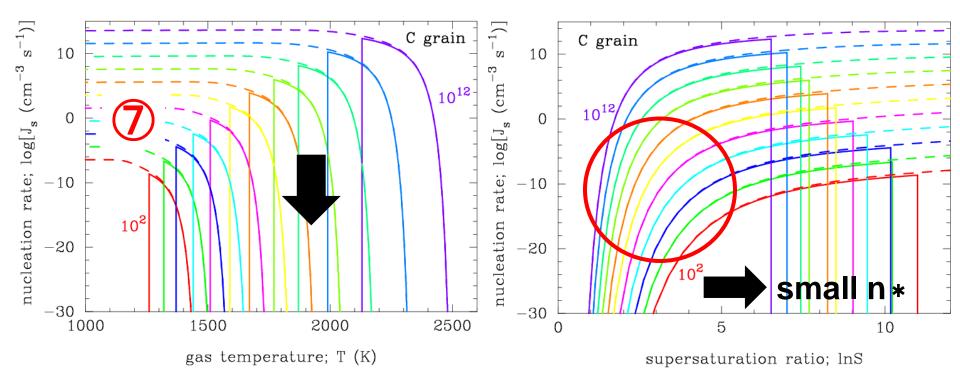
#### **3-3. Critical radius**



#### **3-4. Critical radius of nucleation**



#### **3-5. Comparison of steady-state nucleation**

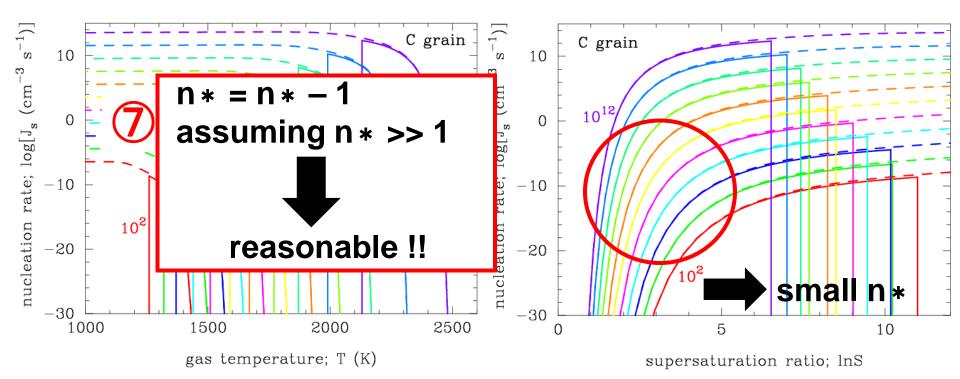


solid line : approximation formula for nucleation rate

$$J_s(t) = \alpha_s \Omega \left(\frac{2\sigma}{\pi m_1}\right)^{\frac{1}{2}} \Pi c_1^2(t) \exp\left[-\frac{4}{27} \frac{\mu^3}{(\ln S)^2}\right]$$

• dashed line : summation form for nucleation rate  $J_s = \{1/(\alpha_1c_1) + \sum 1/(\alpha_nc_1^2) \exp[g(n)] \}^{-1}$ 

#### **3-5. Comparison of steady-state nucleation**



solid line : approximation formula for nucleation rate

$$J_s(t) = \alpha_s \Omega \left(\frac{2\sigma}{\pi m_1}\right)^{\frac{1}{2}} \Pi c_1^2(t) \exp\left[-\frac{4}{27} \frac{\mu^3}{(\ln S)^2}\right]$$

• dashed line : summation form for nucleation rate  $J_s = \{1/(\alpha_1c_1) + \sum 1/(\alpha_nc_1^2) \exp[g(n)] \}^{-1}$ 

#### **<u>4-1. Non-steady nucleation rate</u>**

$$J_{s} = \{1/(\alpha_{1}c_{1}) + \sum 1/(\alpha_{n}c_{1}^{2}) \exp[g(n)] \}^{-1}$$

$$\stackrel{"steady" \rightarrow J_{s} = J_{1} = J_{2} = \cdots = J_{n} (5)$$

$$J_{n} = \alpha_{n}c_{1}c_{n}[1 - (c_{e,1}/c_{1})(c_{e,n}/c_{n})(c_{n+1}/c_{e,n+1})]$$

$$\rightarrow J_{n} = \alpha_{n}c_{1} \{c_{n} - c_{n+1} \exp[g'(n)]\}$$

$$g'(n) = \mu [(n-1)^{2/3} - (n-2)^{2/3}] - \ln S$$

$$\cdot Master equations$$

$$dc_{n}/dt = J_{n-1} - J_{n} (2 \le n \le 100)$$

$$T = T_{0} (t / t_{0})^{-3/4} (T_{0} = 3000 \text{ K}, t_{0} = 150 \text{ day})$$

$$C_1 = C_{10} (t / t_0)^{-3} (C_{10} = 10^5 - 10^8 \text{ cm}^{-3})$$

#### **4-2. Basic equations of dust formation**

#### Equation of conservation for atoms

$$1 - \frac{c_1(t)}{\tilde{c}_1(t)} = \int_{t_0}^t \frac{J(t')}{\tilde{c}_1(t')} \frac{4\pi}{3\Omega} r^3(t,t') dt'$$

#### Equation of grain growth

$$\frac{\partial r}{\partial t} = \alpha_s \frac{4\pi a_0^3}{3} \left(\frac{kT}{2\pi m_1}\right)^{\frac{1}{2}} c_1(t) = \frac{1}{3} a_0 \tau_{\rm col}^{-1}$$

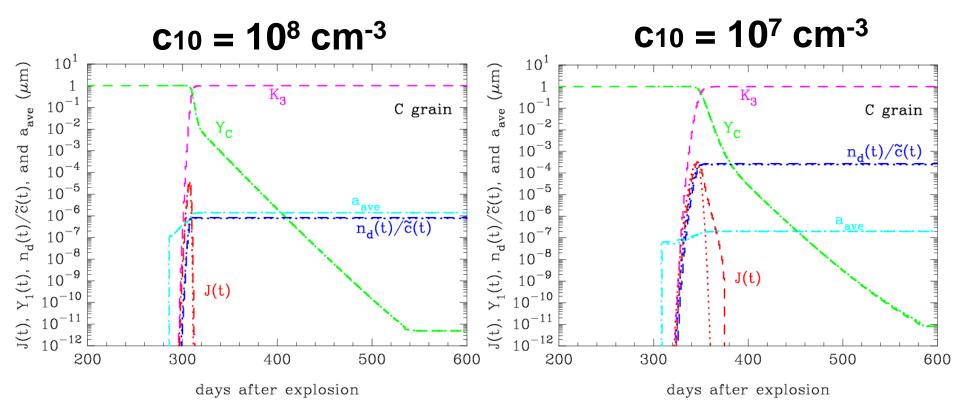
 $\cdot$  number density of dust grain,  $n_{\rm gr}$ 

$$\frac{n_{\rm gr}}{\tilde{c}_1(t)} = \int_{t_0}^t \frac{J(t')}{\tilde{c}_1(t')} dt'$$

 $\cdot$  radius of grain nucleated at  $t_0$  and measured at  $t, r(t, t_0)$ 

$$r(t, t_0) = r_* + \int_{t_0}^t \frac{1}{3} a_0 \tau_{\text{coll}}^{-1}(t') dt'$$

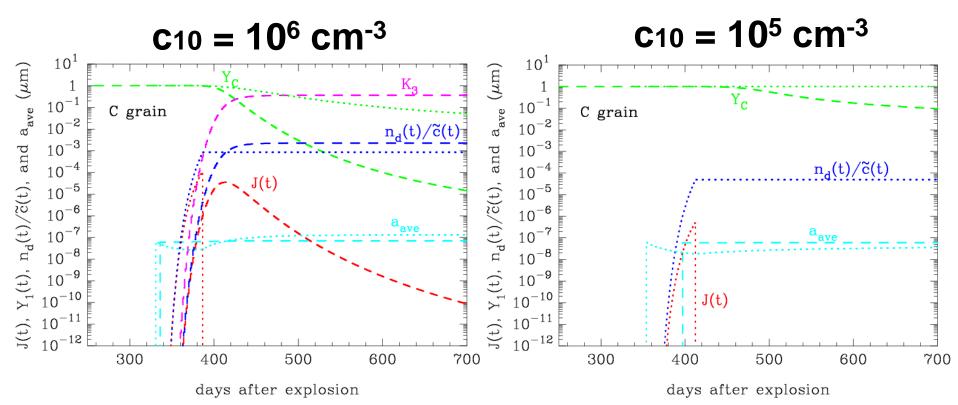
#### 4-3. Steady vs. Non-steady (1)



- dashed line : steady-state nucleation rate
- dotted line : non-steady-state nucleation rate

The difference between steady and non-steady nucleation is small for higher initial densities

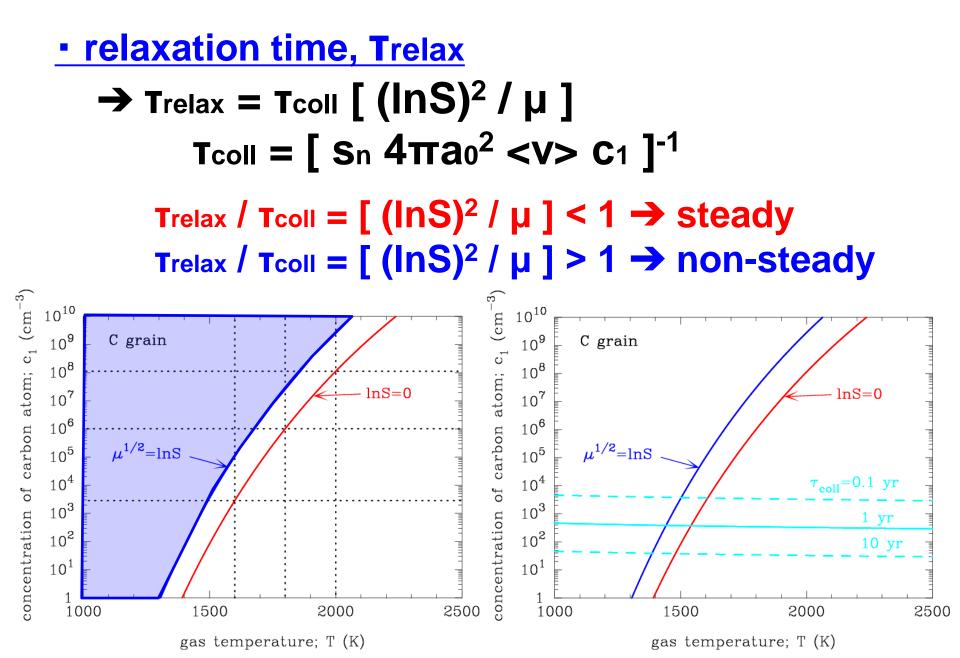
#### 4-4. Steady vs. Non-steady (2)



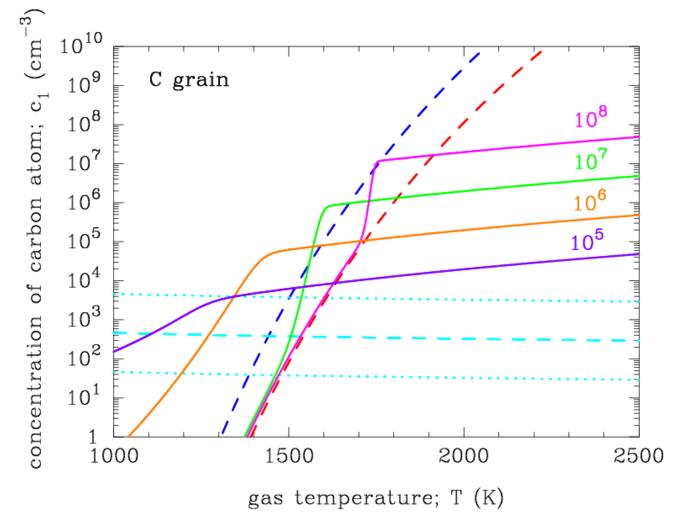
- dotted line : steady-state nucleation rate
- dashed line : non-steady-state nucleation rate

The difference between steady and non-steady nucleation is significant for lower densities

#### 5-1. Relaxation time



#### 5-2. Trajectories on T-c1 plot for dust formation



- higher  $c_1 \rightarrow$  dust condenses at lower  $lnS \rightarrow$  steady
- lower  $c_1 \rightarrow$  dust condenses at higher InS  $\rightarrow$  non-steady

#### 6. Current problems in dust formation theory

- Dust temperature is assumed to be equivalent to gas temperature
- **②** The coagulation between clusters is neglected
- **③** The sticking probability is assumed to be one
- **④** Small clusters are assumed to be spherical
- **(5)**  $J_s = J_1 = J_2 = \cdots = J_{n*}$  for steady-state nucleation
- 6 The surface energy of bulk material is used as that of small clusters
- ⑦ n \* >> 1 is assumed for classical nucleation rate
   → this assumption is valid