

Formation and Destruction Processes of Dust in Supernovae

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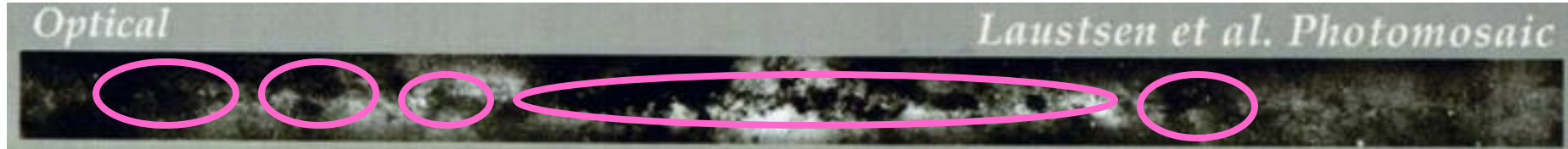
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N. Tominaga (Konan University)

0-1. Sources of dust in our Galaxy

Milky Way (optical)



Milky Way (infrared)



SNe are important sources of interstellar dust?

— number (occurrence) ratio of SNe to AGB stars

$$n(\text{SNe}) / n(\text{AGB stars}) \sim 0.05-0.1$$

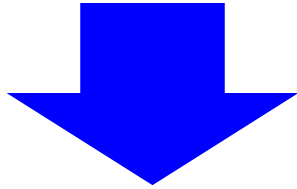
$M_{\text{dust}} = 0.1-1.0 M_{\text{sun}}$ per SN (Nozawa et al. 2003; 2007)

$M_{\text{dust}} = 0.01-0.05 M_{\text{sun}}$ per AGB (Zhukovska & Gail 2008)

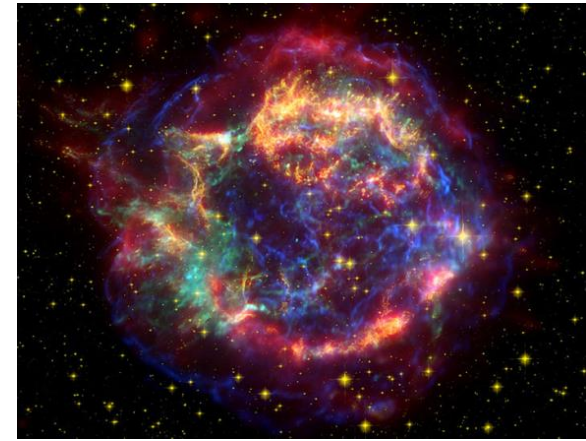
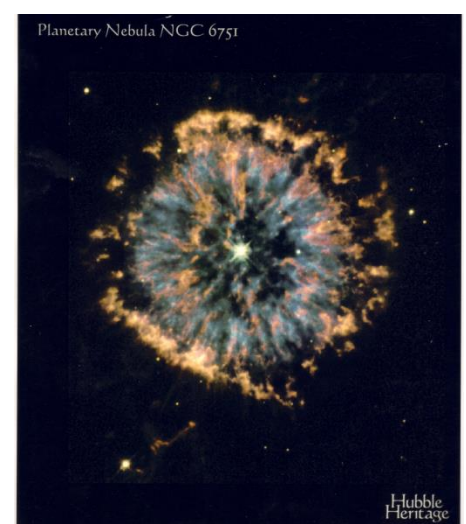
0-2. Formation site of dust

○ Formation sites of dust

- abundant metal (metal : $Z > 5$)
- low gas temperature ($T < \sim 2000$ K)
- high gas density ($n > \sim 10^6$ cm $^{-3}$)

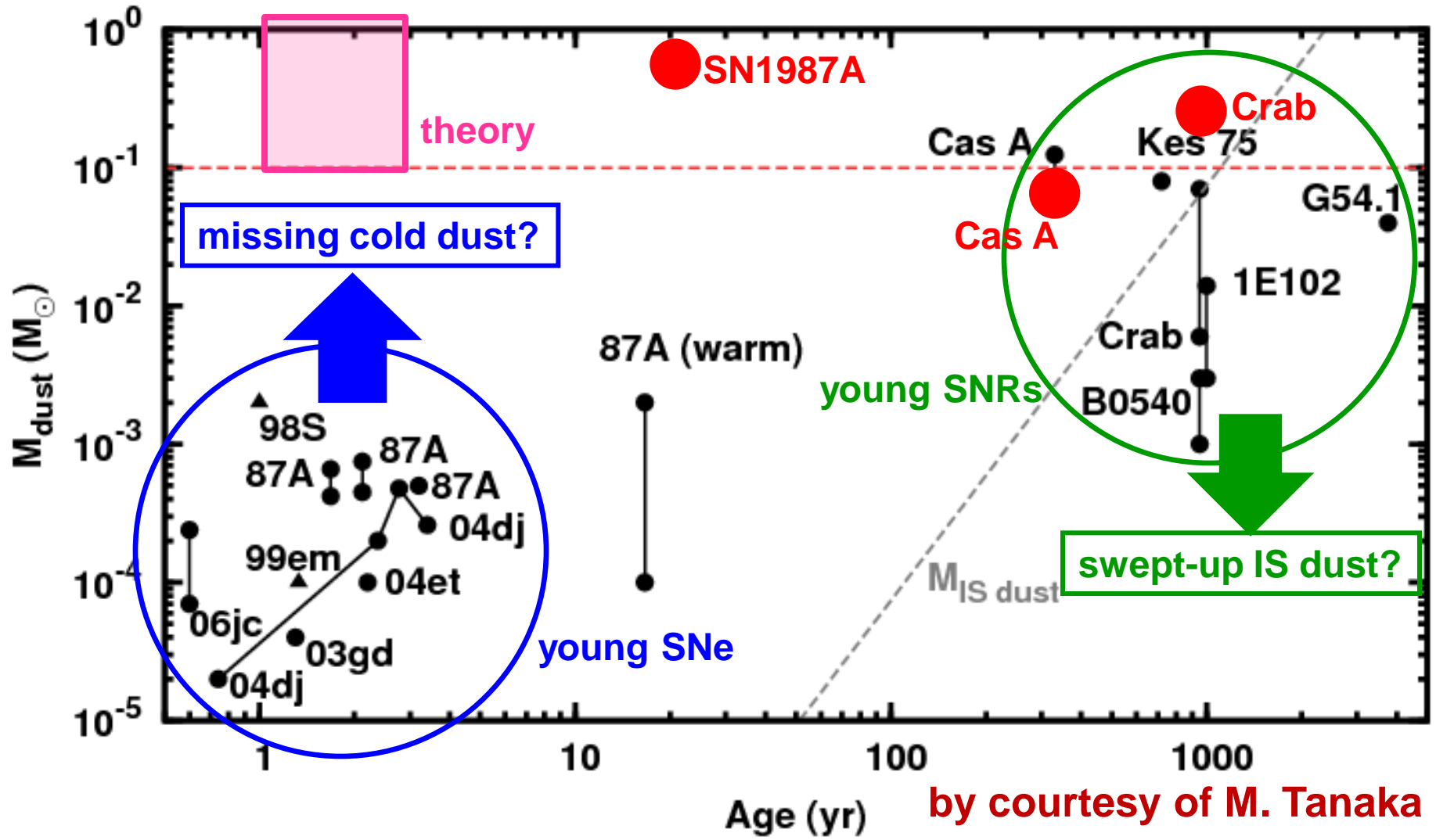


- mass-loss winds of AGB stars
 - expanding ejecta of supernovae
 - molecular clouds (grain growth only)
 - red giant, W-R stars, novae, protoplanetary disk ...
- relative contribution of these sources is unclear!



1. Observations of Dust Formation in SNe (and SNRs)

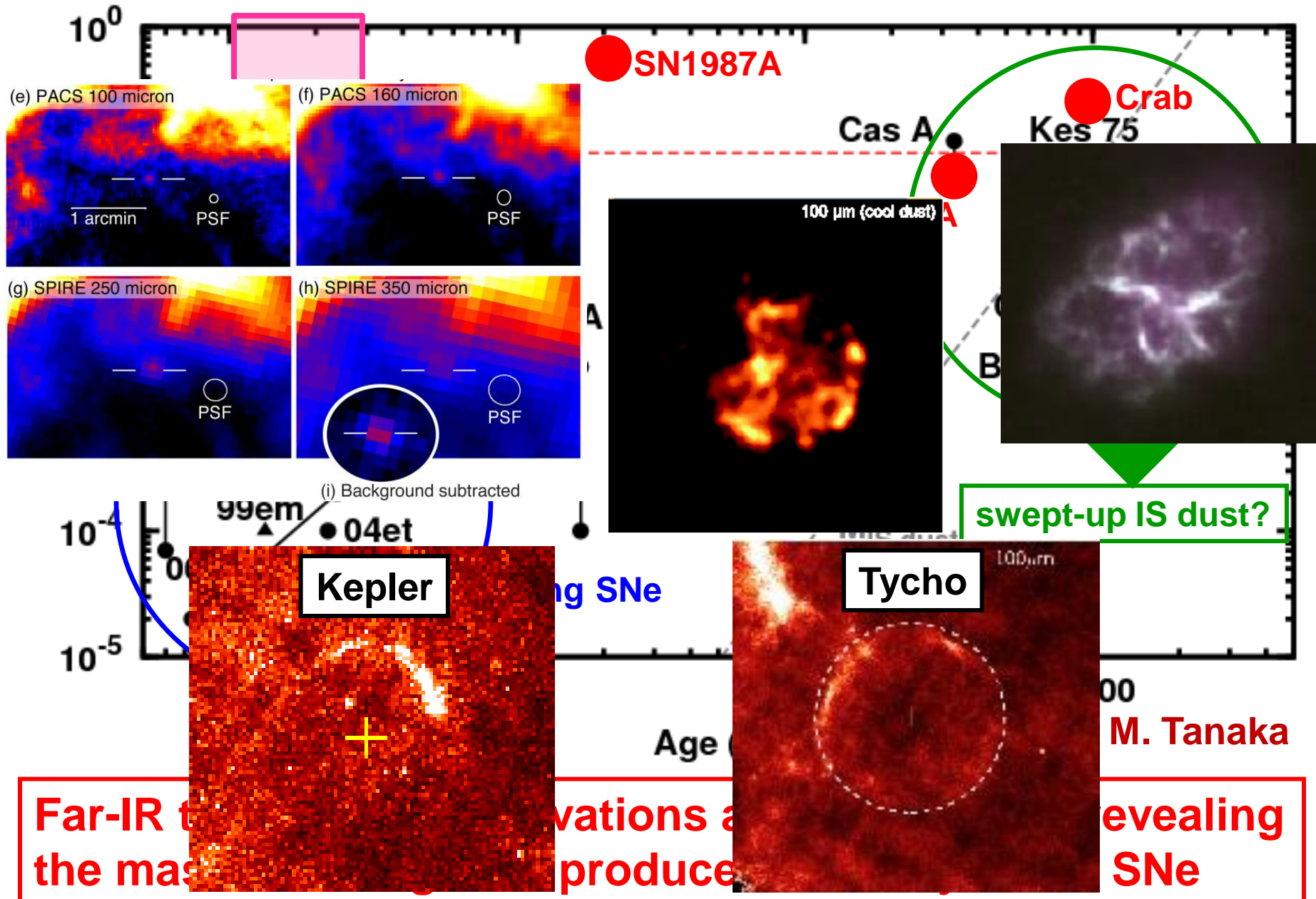
1-1. Summary of observed dust mass in CCSNe



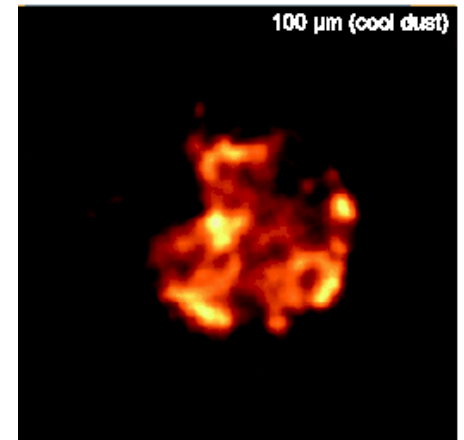
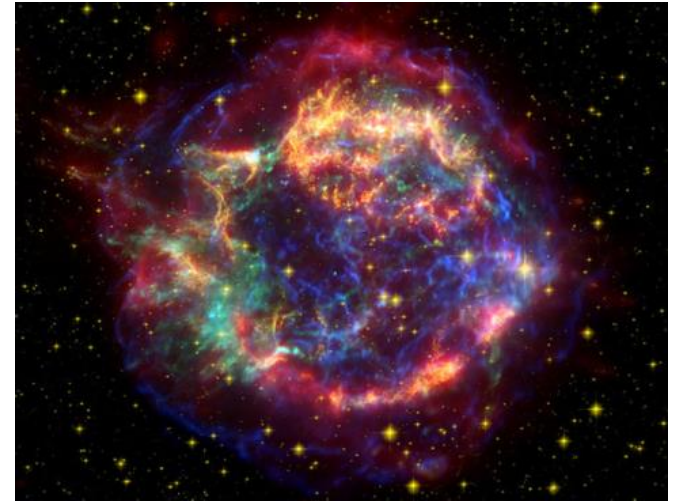
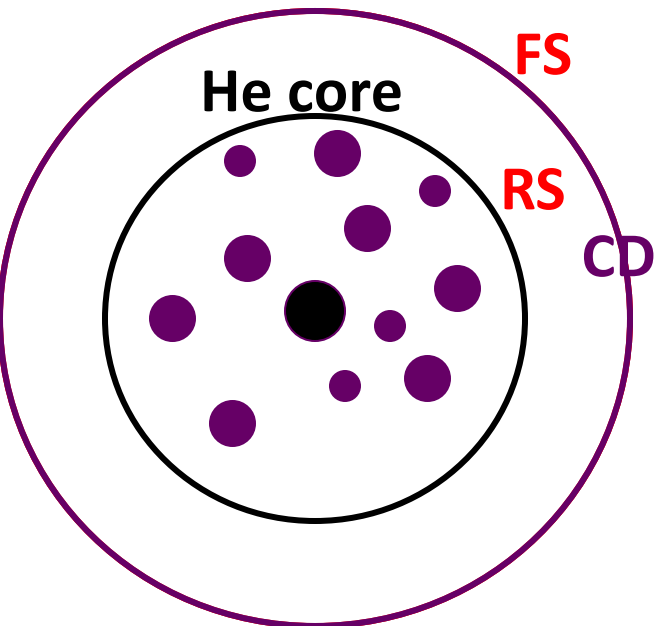
by courtesy of M. Tanaka

Far-IR to sub-mm observations are essential for revealing the mass of dust grains produced in the ejecta of SNe

1-1. Summary of observed dust mass in CCSNe

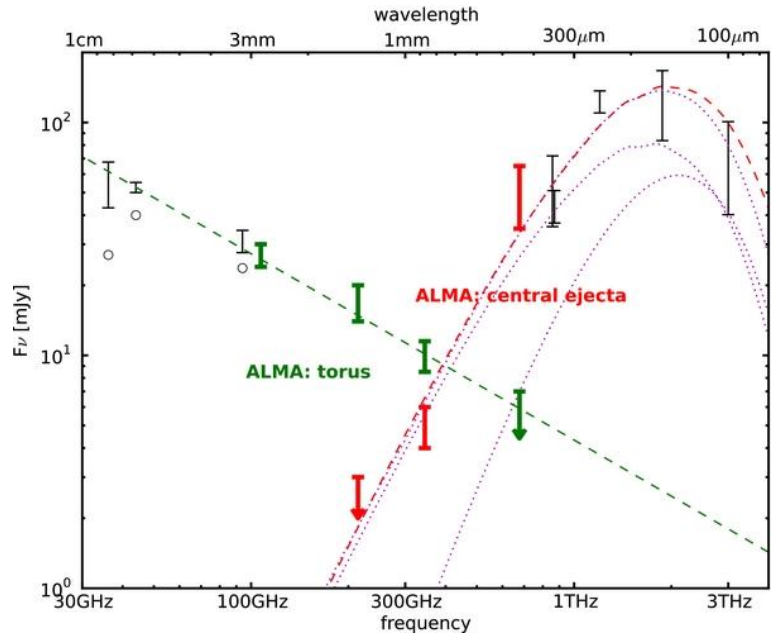


Dust Evolution in SNRs

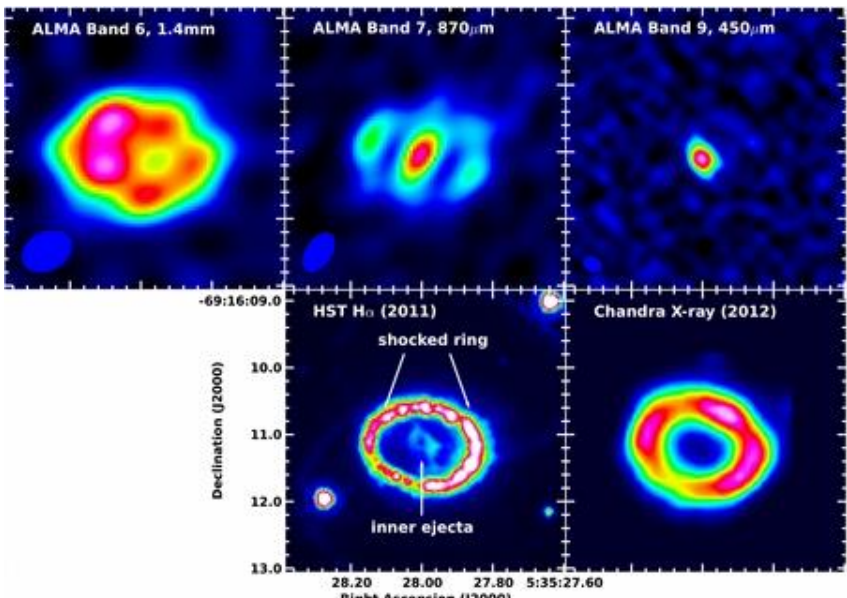


1-2. ALMA reveals dust formed in SN 1987A

SED of 25-years old SN 1987A



Indebetouw+2014

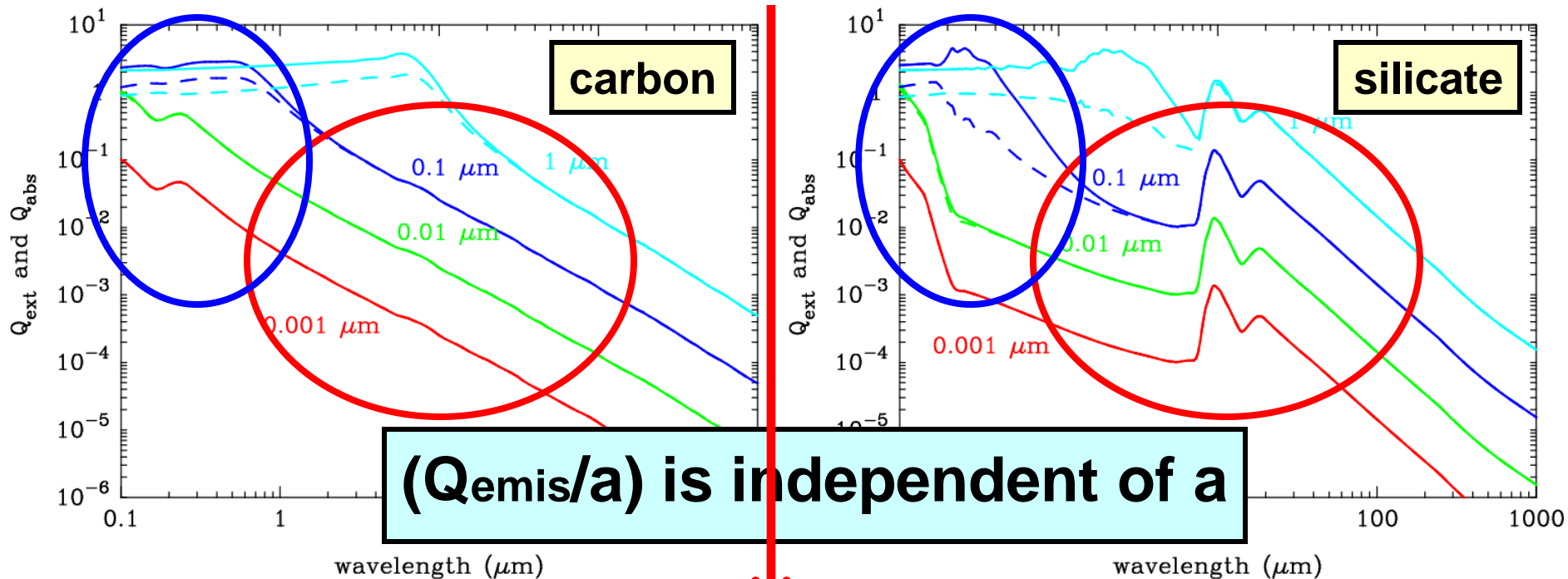


ALMA spatially resolves cool (~20K) dust of ~0.5 Msun formed in the ejecta of SN 1987A
 → SNe could be production factories of dust grains

1-3. Emission and absorption efficiency of dust

○ Thermal radiation from a dust grain

$$F_{\lambda} \propto 4\pi a^2 Q_{\text{emis}}(a, \lambda) \pi B_{\lambda}(T_{\text{dust}}) \quad \# Q_{\text{emis}} = Q_{\text{abs}}$$



(Q_{emis}/a) is independent of a

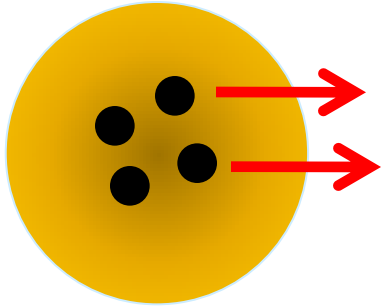
$$F_{\lambda} \propto 4\pi a^3 (Q_{\text{emis}}[a, \lambda]/a) \pi B_{\lambda}(T_{\text{dust}})$$

$$\propto 4 M_{\text{dust}} K_{\text{emis}}(\lambda) \pi B_{\lambda}(T_{\text{dust}})$$

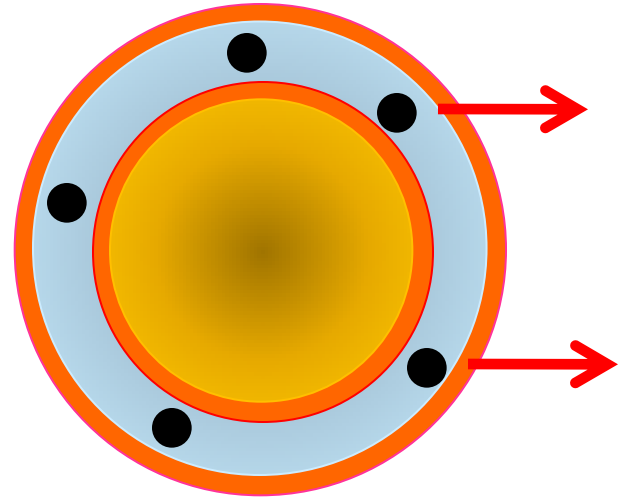
→ IR emission is derived given M_{dust} , K_{abs} , and T_{dust}

1-4. Origin of IR emission from SNe

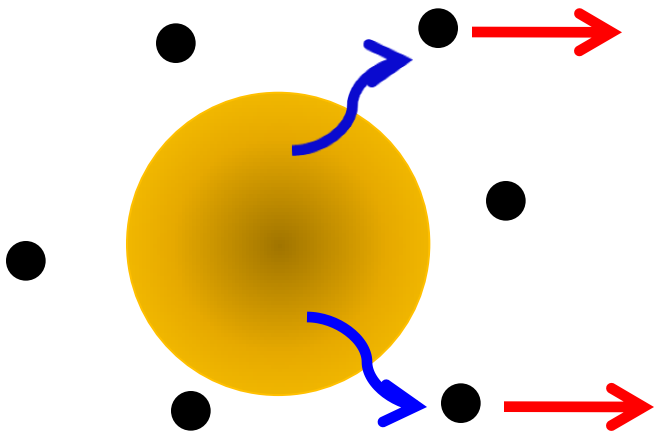
Dust formation in the ejecta



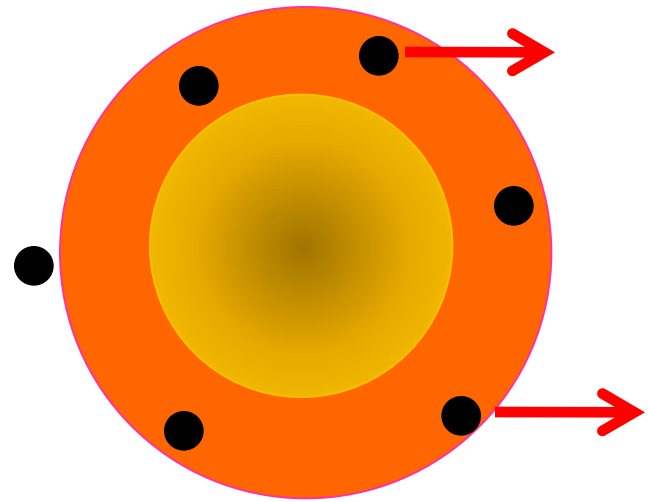
Dust formation in dense shell



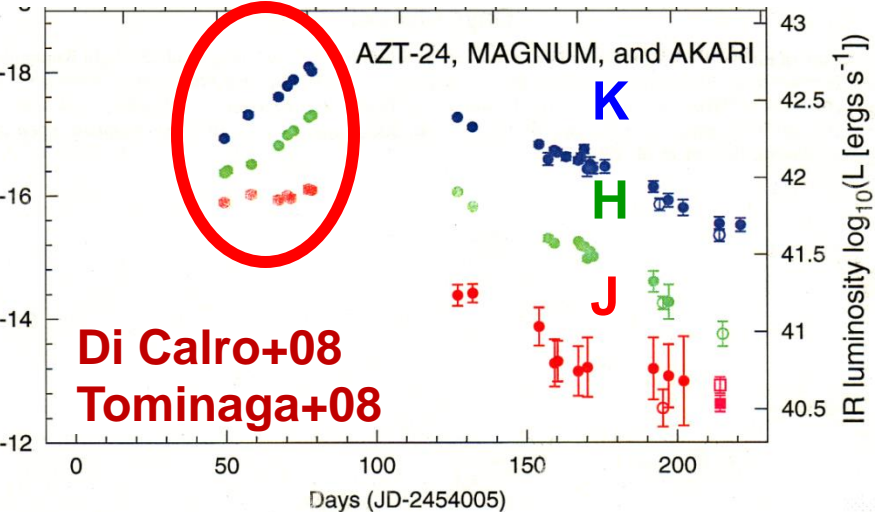
IR echo by CS dust



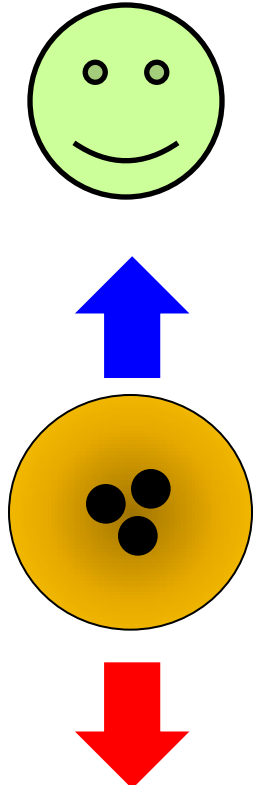
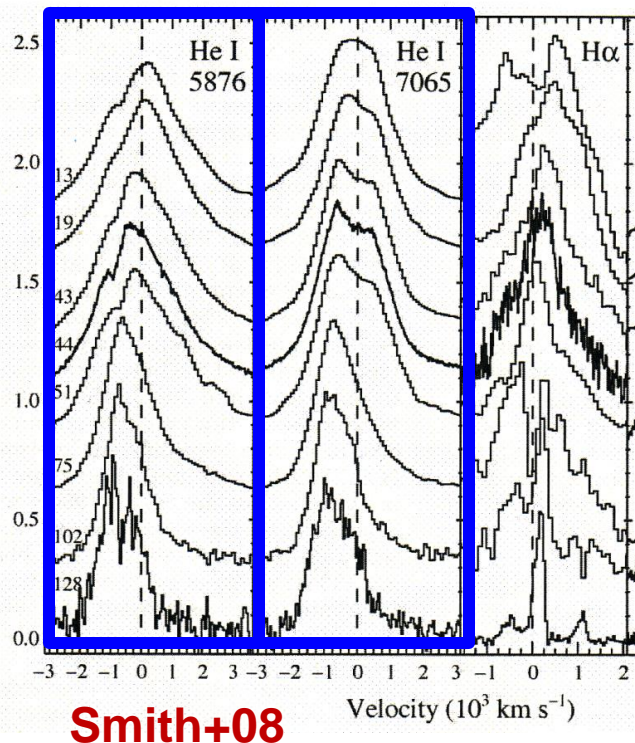
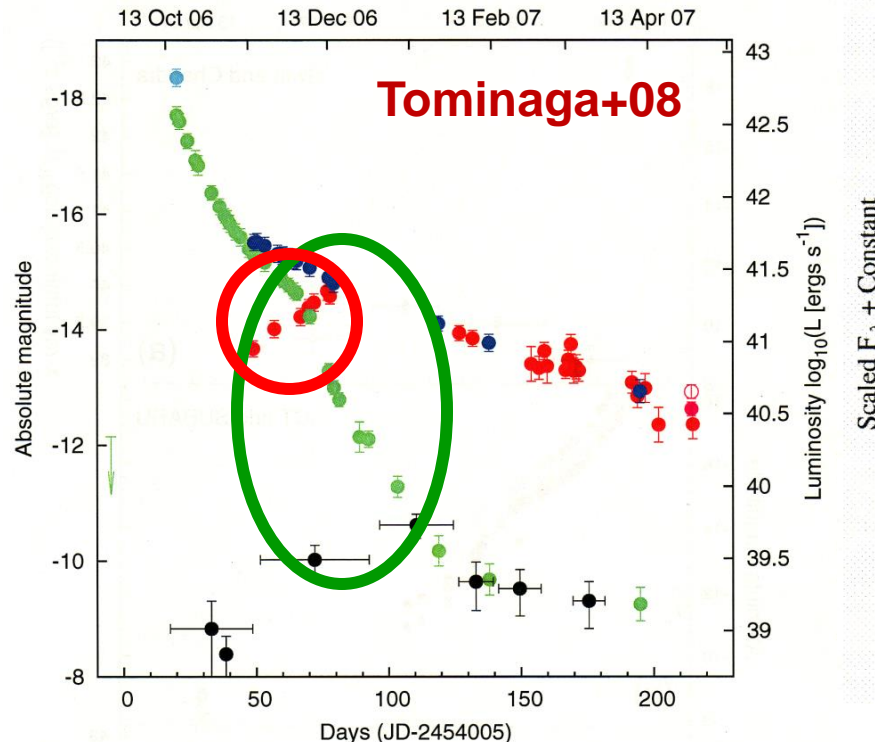
Shock heating of CS dust



1-5. Evidence for dust formation in SN 2006jc

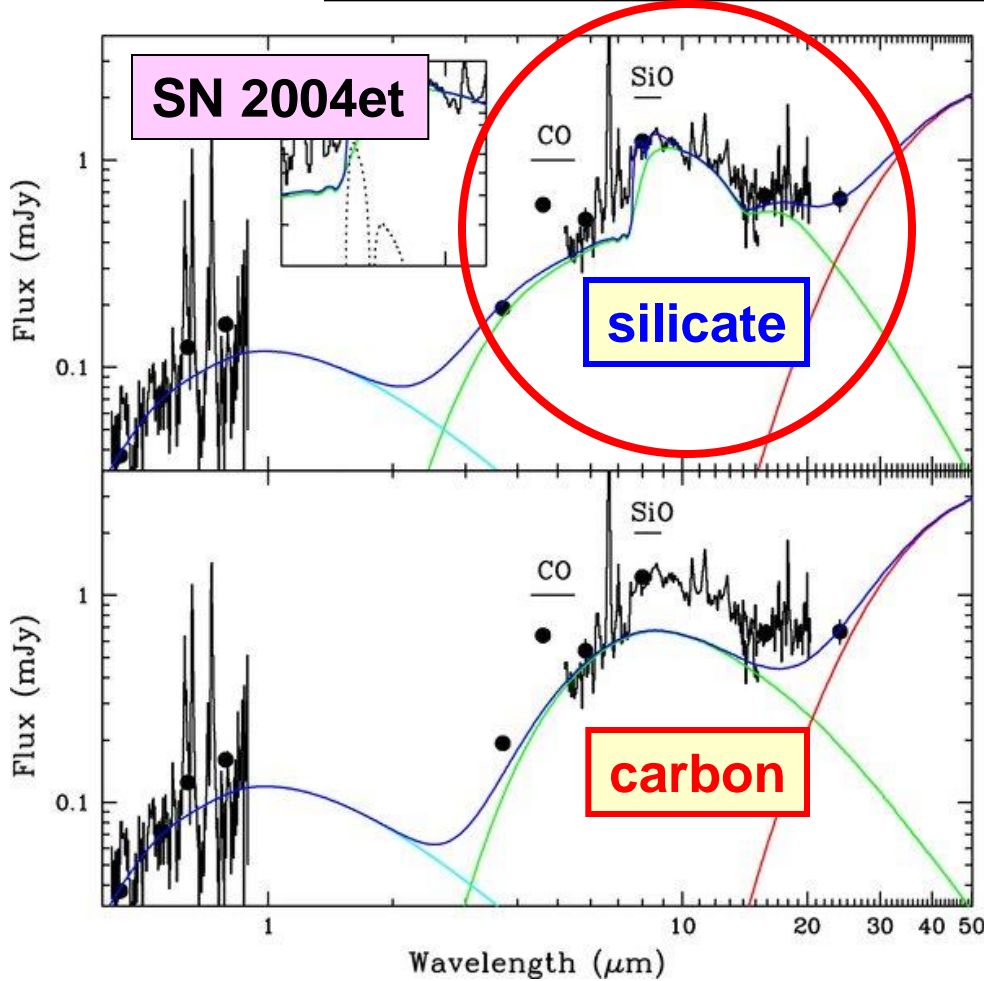


- brightening of IR
 - rapid decline of optical light
 - blueshift of emission lines
- formation of CO and SiO molecules
(more robust if SiO are depleted)

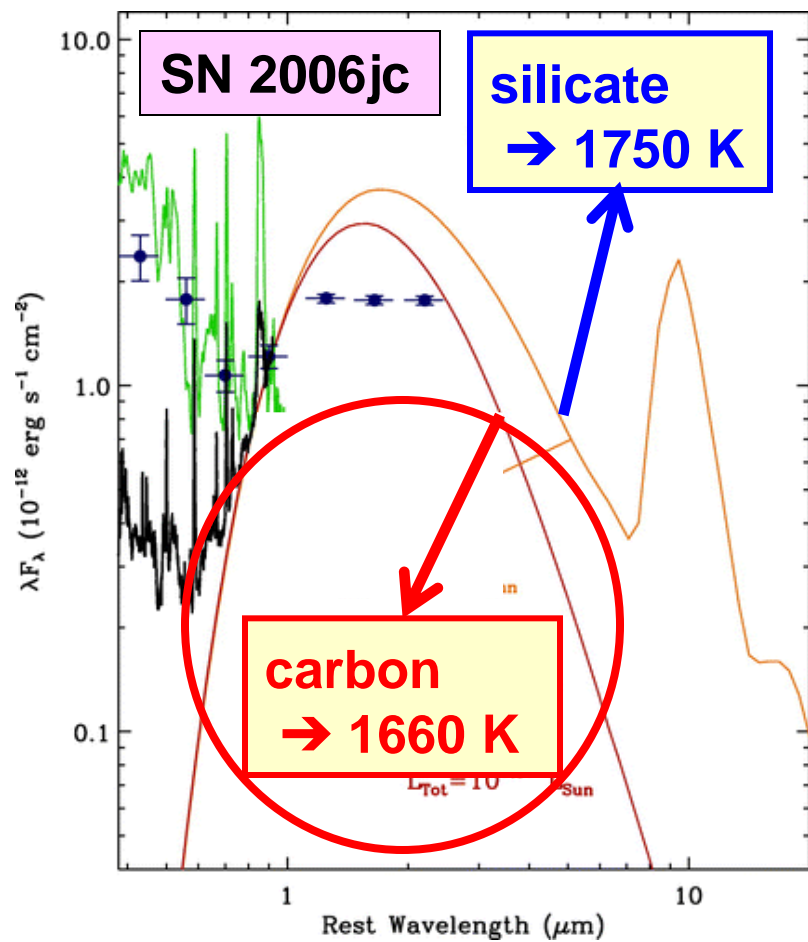


1-6. Composition of dust formed in SNe

IS dust : **carbonaceous grain** and **silicate** (MgSiO_3 , MgFeSiO_4 , ...)

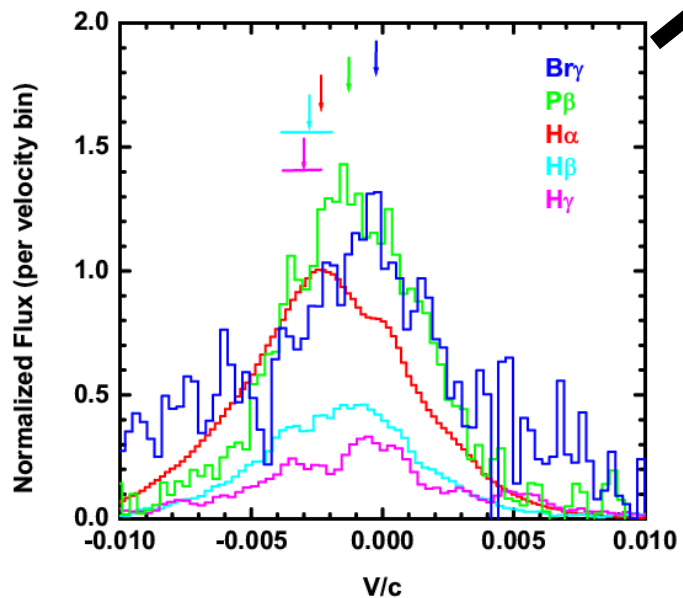
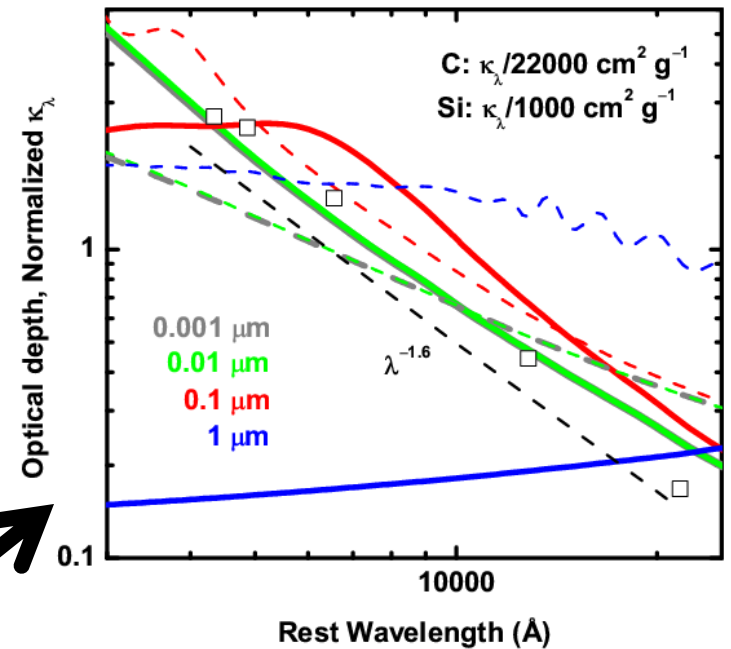
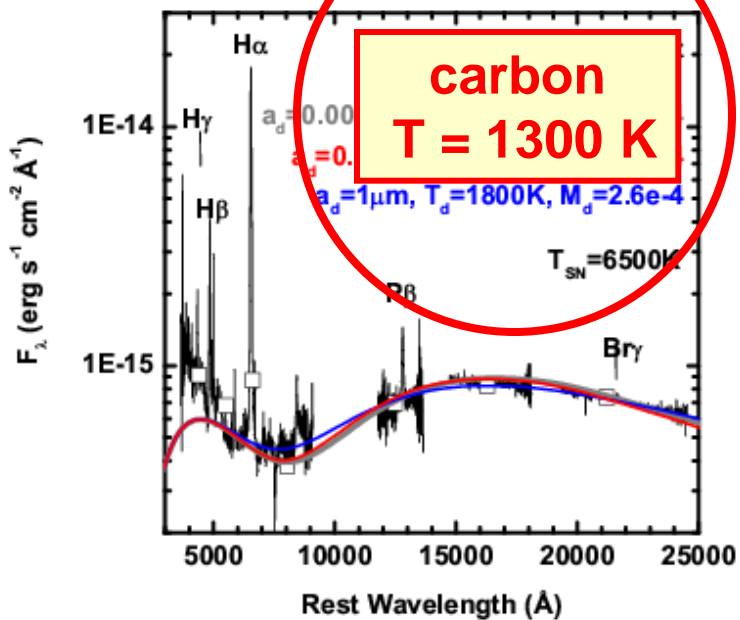


SN 2004et, Kotak+09



SN 2006jc, Smith+08

1-7. Dust formation in Type IIn SN 2010jl



Dust in SN 2010jl

- carbon grains
- grain radius: <0.1 μm
(possibly <0.01 μm)
- dust mass: $\sim 10^{-3} M_{\text{sun}}$

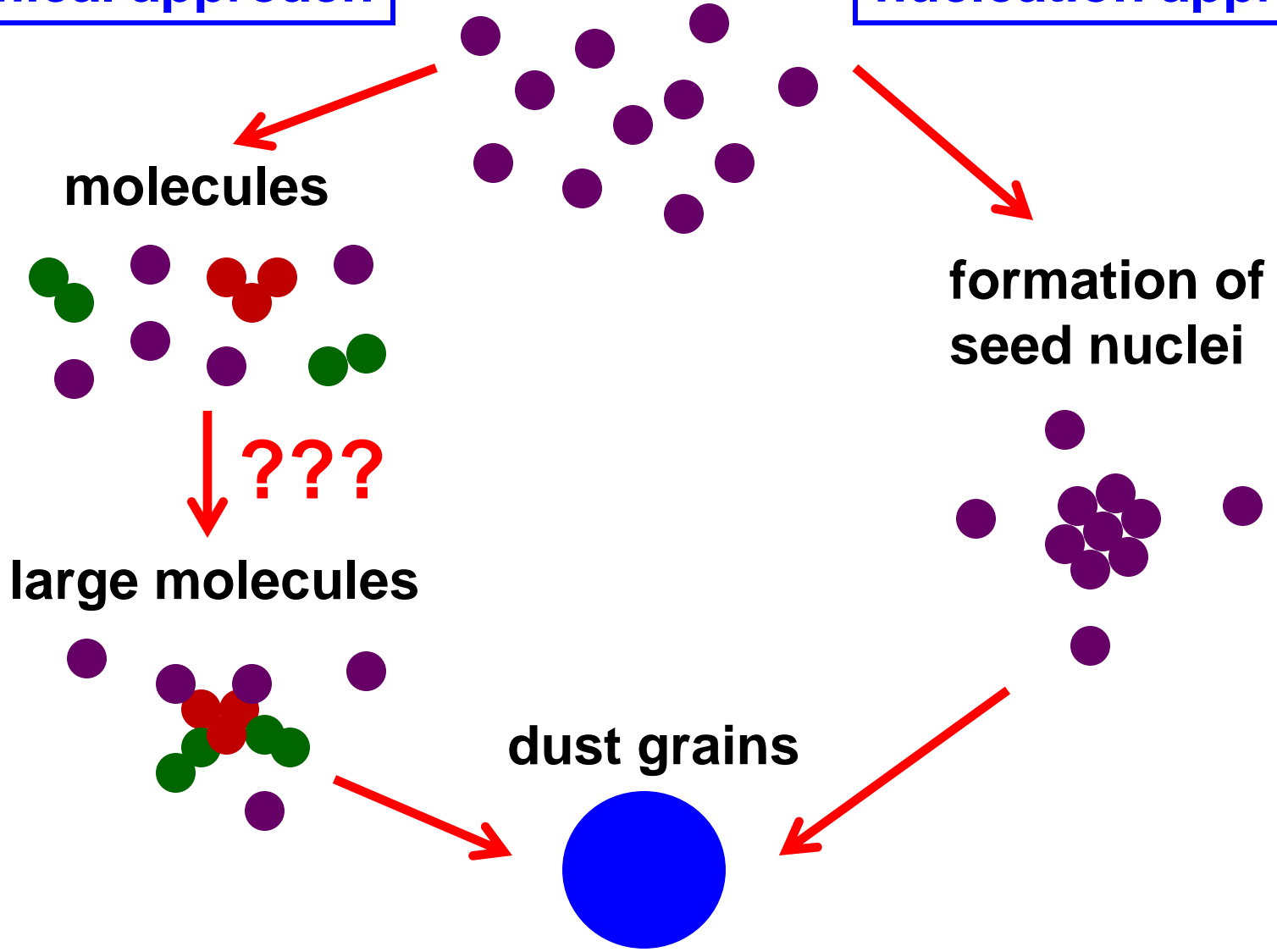
2. Dust Formation in Type IIb SNe

2-0. How do dust grains form?

chemical approach

gaseous atoms

nucleation approach

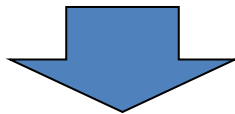


2-1. Calculations of dust formation

- nucleation and grain growth theory taking account of chemical reaction at condensation

(Kozasa & Hasegawa'87)

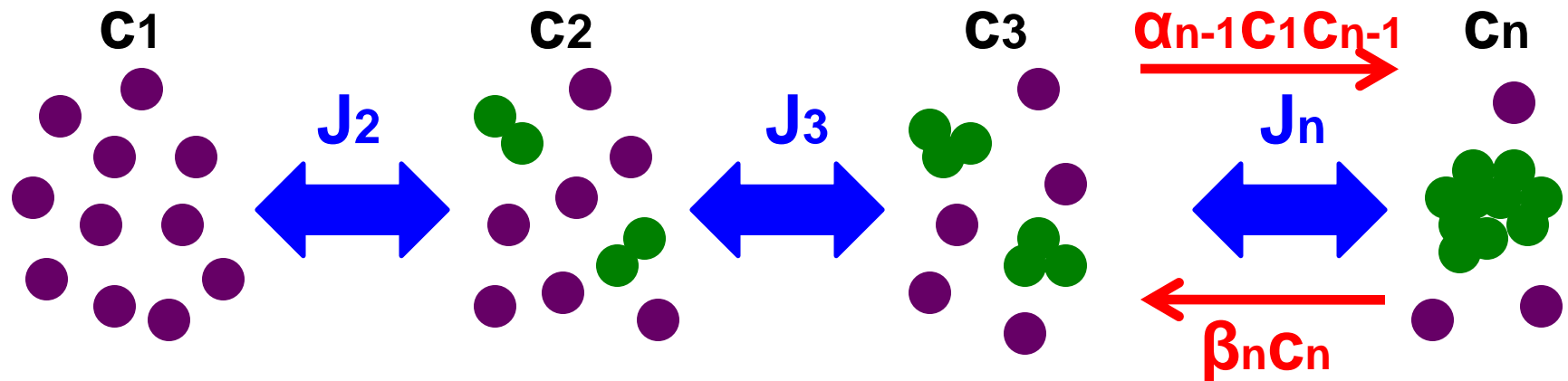
- key species :
gas species with the
least collision frequency
among reactants



key species controls the
kinetics of the nucleation
and grain growth

Dust species	Chemical reactions
Fe _(s)	Fe _(g) → Fe _(s)
FeS _(s)	Fe _(g) + S _(g) → FeS _(s)
Si _(s)	Si _(g) → Si _(s)
Ti _(s)	Ti _(g) → Ti _(s)
V _(s)	V _(g) → V _(s)
Cr _(s)	Cr _(g) → Cr _(s)
Co _(s)	Co _(g) → Co _(s)
Ni _(s)	Ni _(g) → Ni _(s)
Cu _(s)	Cu _(g) → Cu _(s)
C _(s)	C _(g) → C _(s)
SiC _(s)	Si _(g) + C _(g) → SiC _(s)
TiC _(s)	Ti _(g) + C _(g) → TiC _(s)
Al ₂ O _{3(s)}	2Al _(g) + 3O _(g) → Al ₂ O _{3(s)}
MgSiO _{3(s)}	Mg _(g) + SiO _(g) + 2O _(g) → MgSiO _{3(s)}
Mg ₂ SiO _{4(s)}	2Mg _(g) + SiO _(g) + 3O _(g) → Mg ₂ SiO _{4(s)}
SiO _{2(s)}	SiO _(g) + O _(g) → SiO _{2(s)}
MgO _(s)	Mg _(g) + O _(g) → MgO _(s)
Fe ₃ O _{4(s)}	3Fe _(g) + 4O _(g) → Fe ₃ O _{4(s)}
FeO _(s)	Fe _(g) + O _(g) → FeO _(s)

2-2. Formulation of dust formation



▪ master equations

$$\frac{dc_n}{dt} = J_n(t) - J_{n+1}(t) \quad \text{for } 2 \leq n \leq n_*,$$

$$J_n(t) = \alpha_{n-1} c_{n-1} c_1 - \beta_n c_n \quad \text{for } 2 \leq n \leq n_*,$$

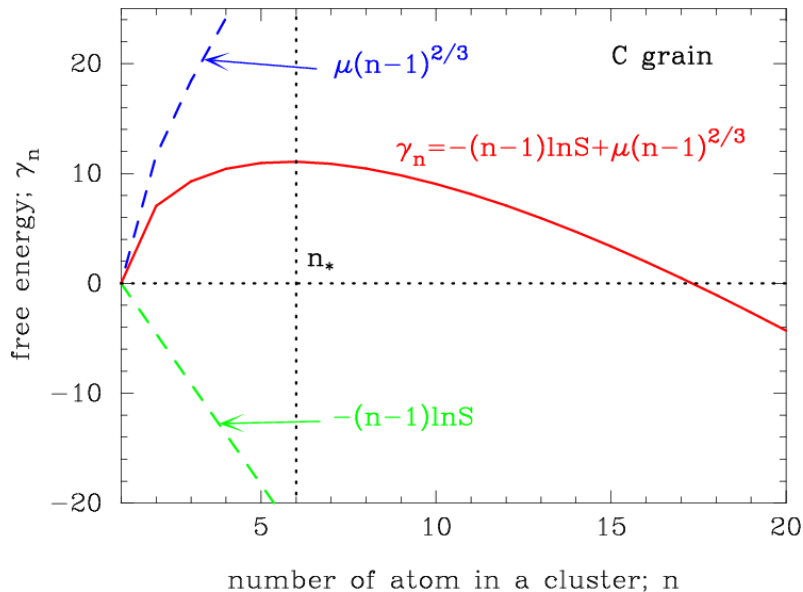
$$\alpha_n = \frac{s_n}{1 + \delta_{1n}} 4\pi a_0^2 n^{\frac{2}{3}} \left(\frac{kT}{2\pi m_n} \right)^{\frac{1}{2}},$$

$$\beta_n = \alpha_{n-1} \frac{\overset{\circ}{c}_{n-1}}{\overset{\circ}{c}_n} \overset{\circ}{c}_1,$$

2-3. Steady-state nucleation rate

steady-state nucleation rate: J_s

→ assuming $J_s = J_2 = J_3 = \dots = J_\infty$



$$(n_c - 1)^{\frac{1}{3}} = \frac{2}{3} \frac{\mu}{\ln S}$$

where

$$\mu = 4\pi a_0^2 \sigma / kT$$

σ : surface tension

S : supersaturation ratio

$$(S = p_1 / p_{1v})$$

$$J_s = s_{\text{crit}} \Omega_0 \left(\frac{2\sigma}{\pi m_1} \right)^{\frac{1}{2}} c_1^2 \Pi \exp \left[-\frac{4}{27} \frac{\mu^3}{(\ln S)^2} \right],$$


2-4. Basic equations for dust formation

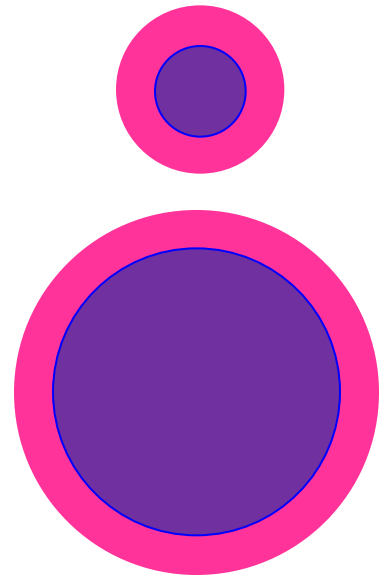
▪ Equation of mass conservation

$$c_{10} - c_1 = \int_{t_0}^t J_{n_s}(t') \frac{a^3(t, t')}{a_0^3} dt',$$

▪ Equation of grain growth

$$\frac{da}{dt} = s\Omega_0 \left(\frac{kT}{2\pi m_1} \right)^{\frac{1}{2}} c_1 \left(1 - \frac{1}{S} \right),$$


$$\frac{dV}{dt} = s\Omega_0 4\pi a^2 \left(\frac{kT}{2\pi m_1} \right)^{\frac{1}{2}} c_1 \left(1 - \frac{1}{S} \right),$$



Growth rate is independent of grain radius

2-5. Dust formation calculation in the ejecta

○ Dust formation calculation

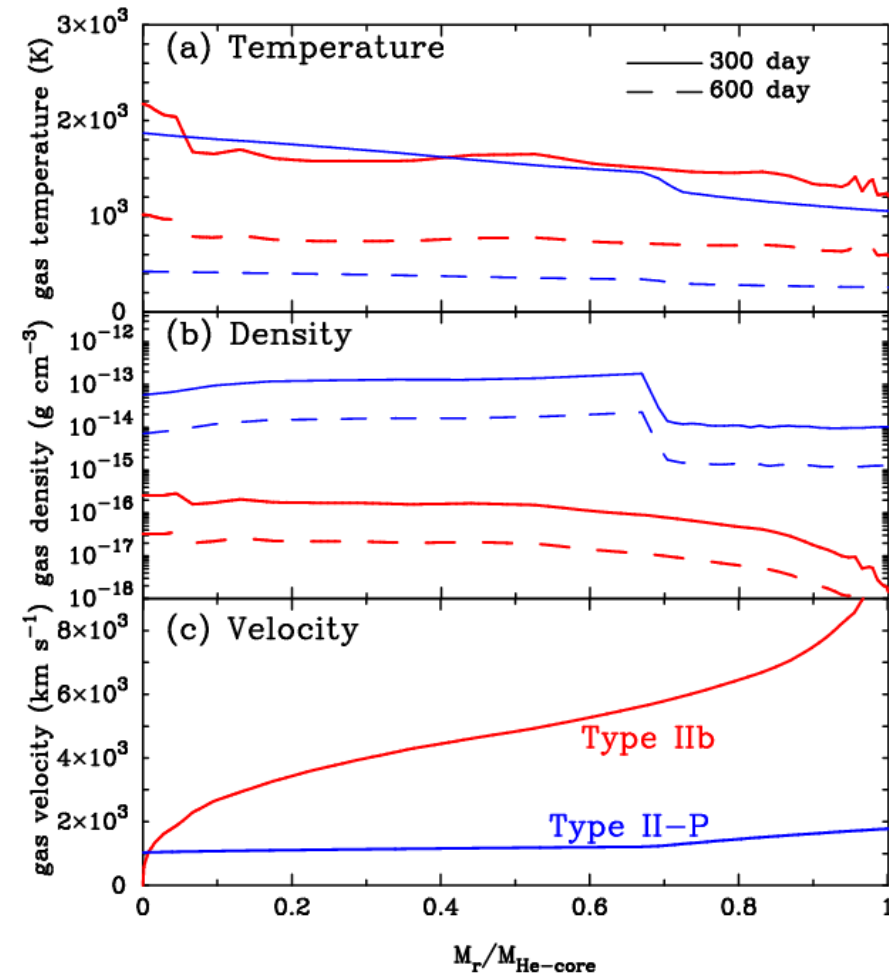
- non-steady nucleation and grain growth theory

(Nozawa et al. 2003)

○ SN IIb model

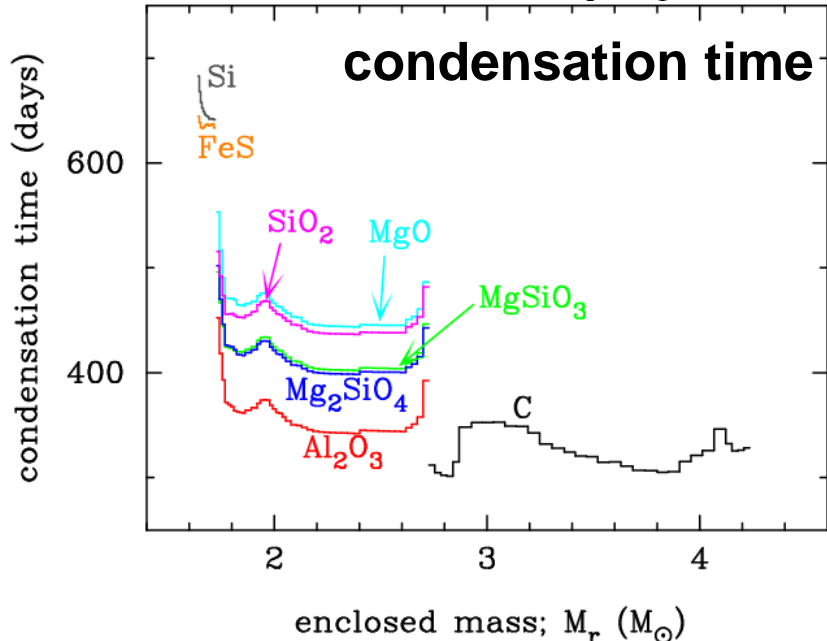
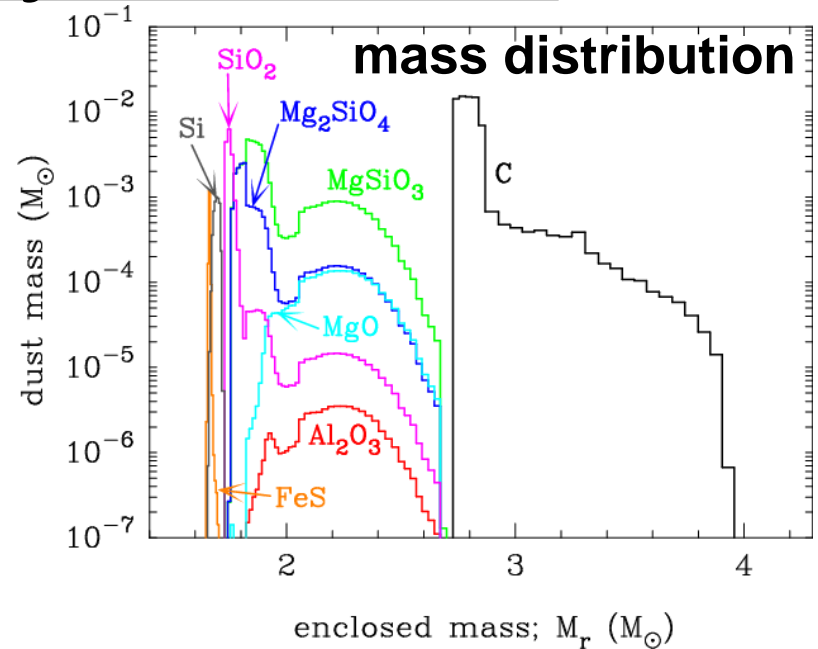
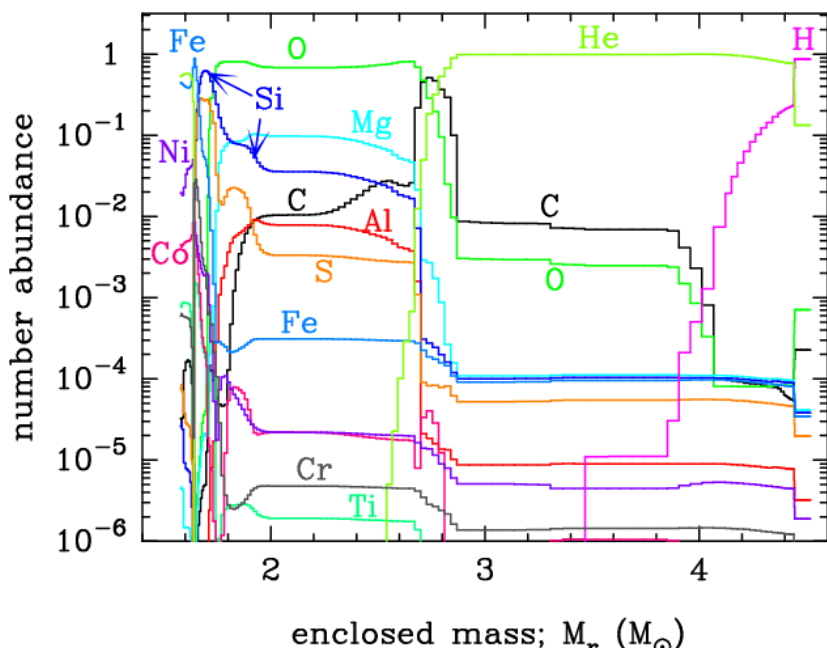
(SN1993J-like model)

- **M_{H-env} = 0.08 M_{sun}**
- **M_{ZAMS} = 18 M_{sun}**
- **M_{eje} = 2.94 M_{sun}**
- E₅₁ = 1
- M(⁵⁶Ni) = 0.07 M_{sun}



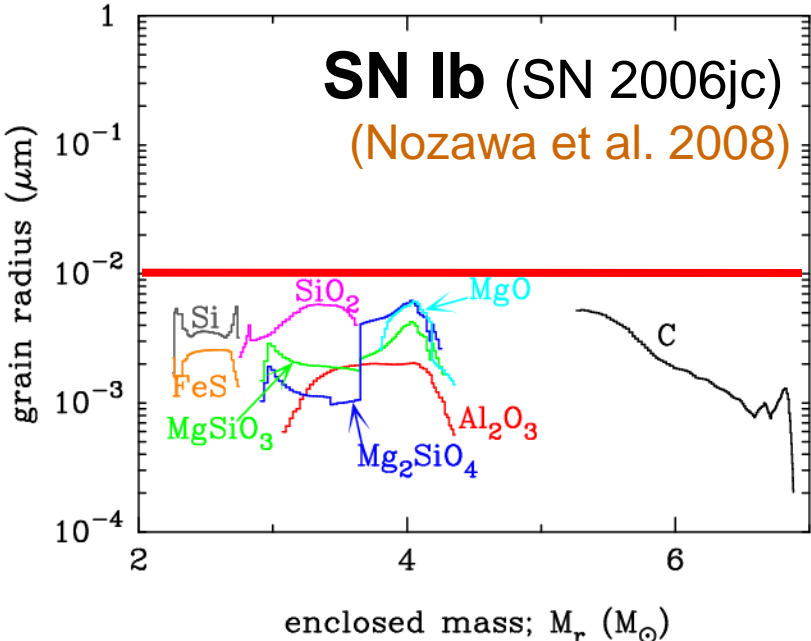
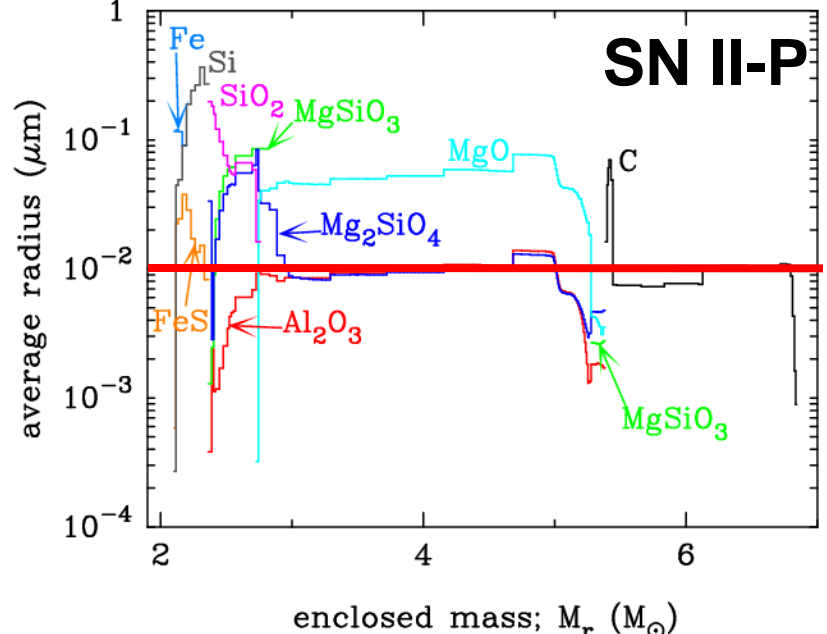
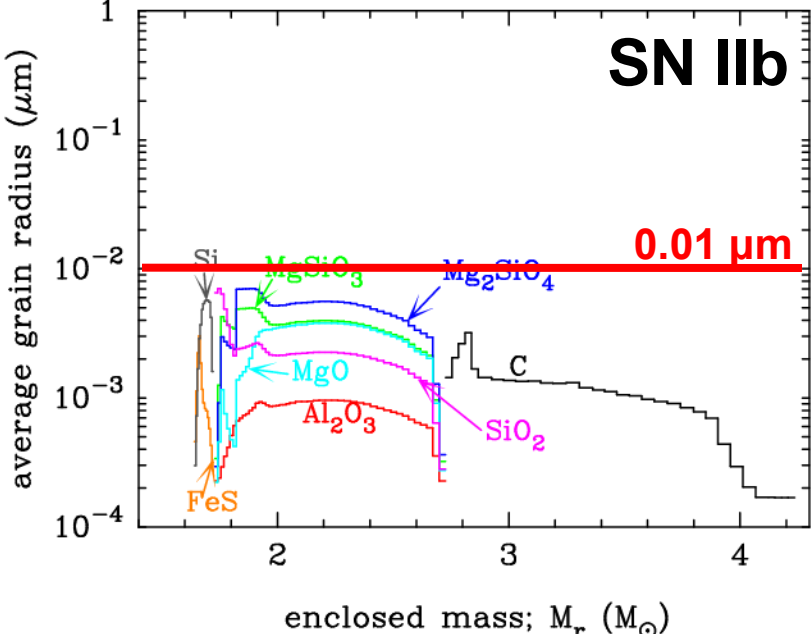
- SN II-P model : **M_{H-env} = 13 M_{sun}**, **M_{ZAMS} = 20 M_{sun}**, **E₅₁ = 1**
(Umeda & Nomoto 2002)

2-6. Birth of dust in the ejecta of Cas A



- condensation time of dust **300-700 d** after explosion
- total mass of dust formed
 - **0.167 M_{sun} in SN IIb**
 - $M_c = 0.07 M_{\text{sun}}$**
 - $M_{\text{silicate}} = 0.08 M_{\text{sun}}$**
 - **0.1-1 M_{sun} in SN II-P**

2-7. Dependence of dust radii on SN type



The radius of dust formed in H-stripped SNe is small

- SN IIb and SN Ib/Ic without massive H-env
→ $a_{\text{dust}} < 0.01 \mu\text{m}$
- SN II-P with massive H-env
→ $a_{\text{dust}} > 0.01 \mu\text{m}$

3. Dust Destruction in Cas A

3-1. Time evolution of SNRs

- Basic equations (spherical symmetry)

$$\frac{\partial \rho}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \rho v) = 0$$

$$\frac{\partial}{\partial t} (\rho v) + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \rho v^2) = -\frac{\partial P}{\partial r}$$

$$\begin{aligned} \frac{\partial}{\partial t} \left(\frac{\rho v^2}{2} + \frac{P}{\gamma - 1} \right) + \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \left[\frac{\rho v^2}{2} + \frac{\gamma P}{\gamma - 1} \right] v \right) \\ = -(n_e n_H \Lambda_{\text{gas}}(T) + \Lambda_{\text{ic}}(T) + \Lambda_{\text{d}}(n_H, T)) \end{aligned}$$

$\Lambda_{\text{gas}}(T)$: cooling function of gas by the atomic process

(Sutherland & Dopita 1993; Smith et al. 2001)

$\Lambda_{\text{ic}}(T)$: inverse Compton cooling (Ikeuchi & Ostriker 1986)

$$\Lambda_{\text{ic}}(T) = 5.41 \times 10^{-32} (1+z)^4 n_e (T/10^4 \text{ K}) \text{ (we adopt } z = 20)$$

$\Lambda_{\text{d}}(n_H, T)$: cooling of gas through thermal emission of dust

- numerical code : flux splitting method (van Albada et al. 1982)

3-2. Dynamics of dust

- deceleration of dust due to drag force (Baines et al. 1965)

$$\frac{dw_d}{dt} = \frac{F_{\text{drag}}}{m_d} = -\frac{3n_H kT}{2a\rho_d} \sum_i A_i G_i(s_i) \quad (w_d : \text{relative velocity})$$

ρ_d ; mass density of a grain

A_i ; the number abundance of gas species i normalized by n_H

$$G_i(s_i) = \left(s_i^2 + 1 - \frac{1}{4s_i^2} \right) \text{erf}(s_i) + \left(s_i + \frac{1}{2s_i} \right) \frac{e^{-s_i^2}}{\sqrt{\pi}}$$

↓

$$G_i(s_i) \approx \frac{8s_i}{3\sqrt{\pi}} \left(1 + \frac{9\pi}{64}s_i^2 \right)^{\frac{1}{2}} \quad (\text{Draine \& Salpeter 1979})$$

where $s_i^2 = m_i w_d^2 / 2kT$

3-3. Erosion rate of dust by sputtering

- dust destruction by sputtering (e.g., Dwek, Foster & Vancura 1996)

$$\frac{da}{dt} = -\frac{m_{\text{sp}}}{4\pi a^2 \rho_d} \sum_i \mathcal{R}(Y_i(E))$$

$Y_i(E) = 2Y_i^0(E)$; the angle-averaged sputtering yield

m_{sp} ; average mass of the sputtered atoms

- rate equation over a modified Maxwellian distribution of gas taken account of relative velocity of dust to gas (e.g., Shull 1978)

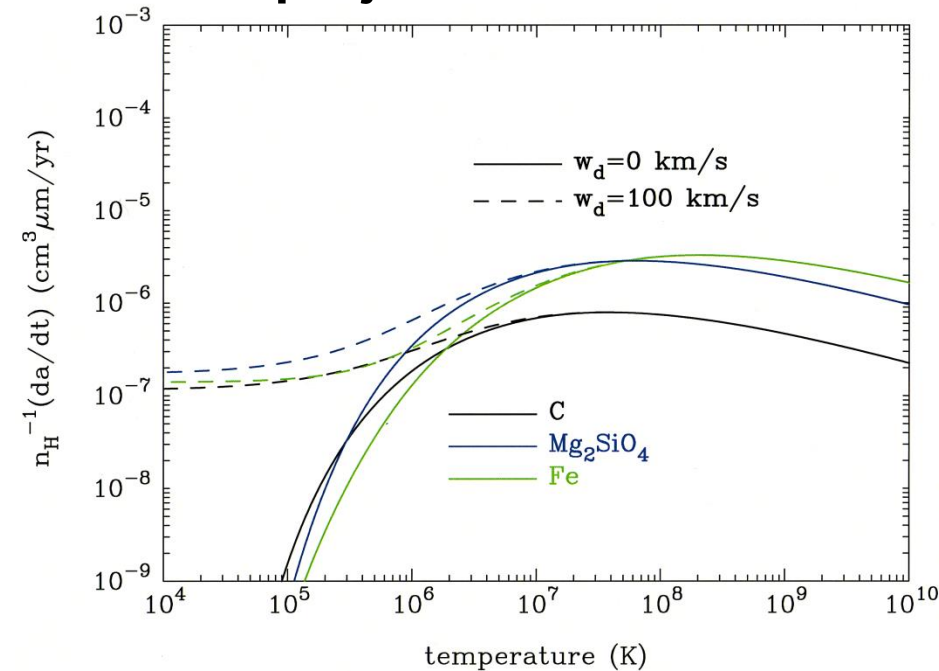
$$\mathcal{R}(X_i(\epsilon)) = n_{\text{H}} A_i \pi a^2 \left(\frac{8kT}{\pi m_i} \right)^{\frac{1}{2}} \frac{e^{-s_i^2}}{2s_i} \int \sqrt{\epsilon} e^{-\epsilon} \sinh(2s_i \sqrt{\epsilon}) X_i(\epsilon) d\epsilon$$

where $\epsilon = E/kT$

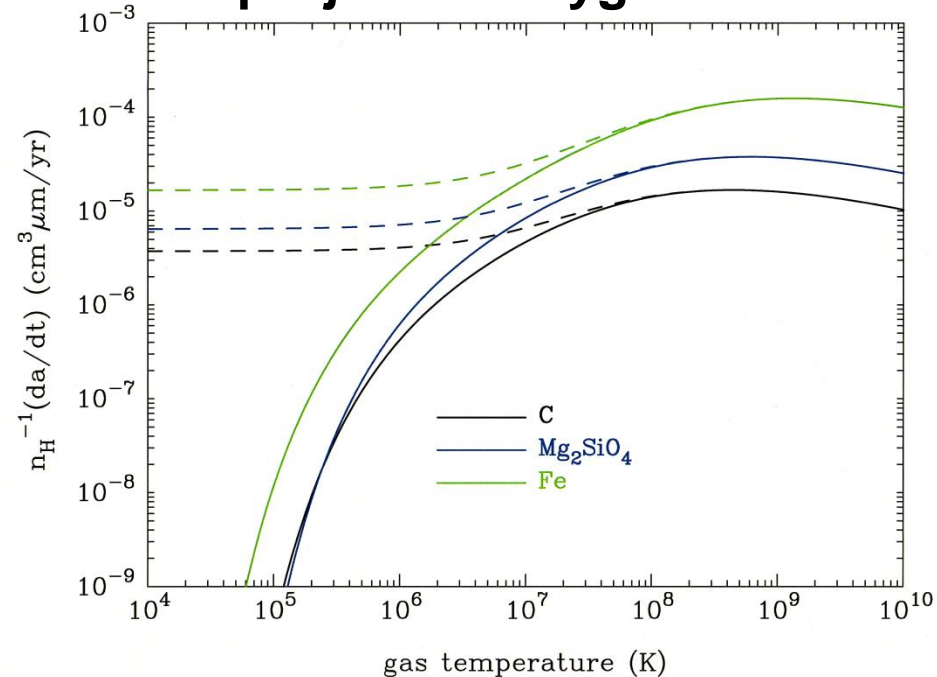
3-4. Erosion rate of dust by sputtering

Nozawa+2006, ApJ, 648, 435

projectile: H and He



projectile: oxygen ions



- erosion rate by sputtering quickly increases above 10^5 K and peaks at 10^7 - 10^8 K
- erosion rate : $da / dt \sim 10^{-6} n_H \mu\text{m yr}^{-1} \text{cm}^3$
for the primordial gas (H and He) at $T > 10^6$ K

3-5. Calculation of dust evolution in SNRs

Dust evolution calculations (Nozawa et al. 2006, 2007)

- spherical symmetric hydrodynamic calculation based on the ejecta model of the SN IIb
- treating dust as a test particle
 - erosion by sputtering
 - deceleration by gas drag
 - collisional stochastic heating

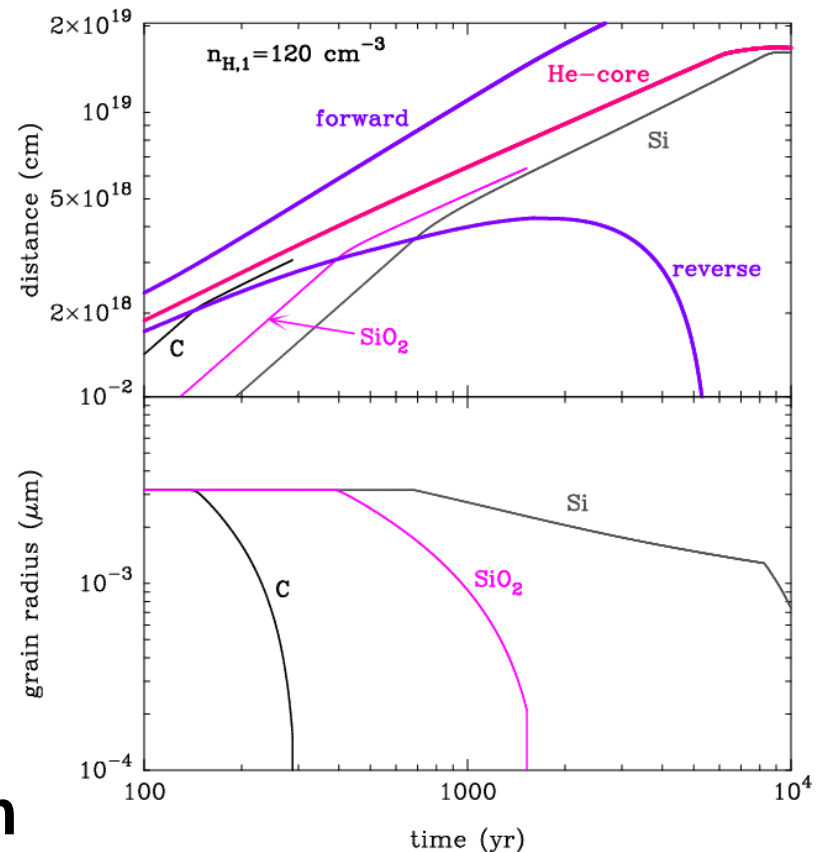
— density profile of CSM

$$\begin{aligned} n_H(r) &= n_{H,1} (r / r_1)^{-2} / \text{cc} \\ &= 1 / \text{cc} \quad \text{for } n_H < 1 / \text{cc} \end{aligned}$$

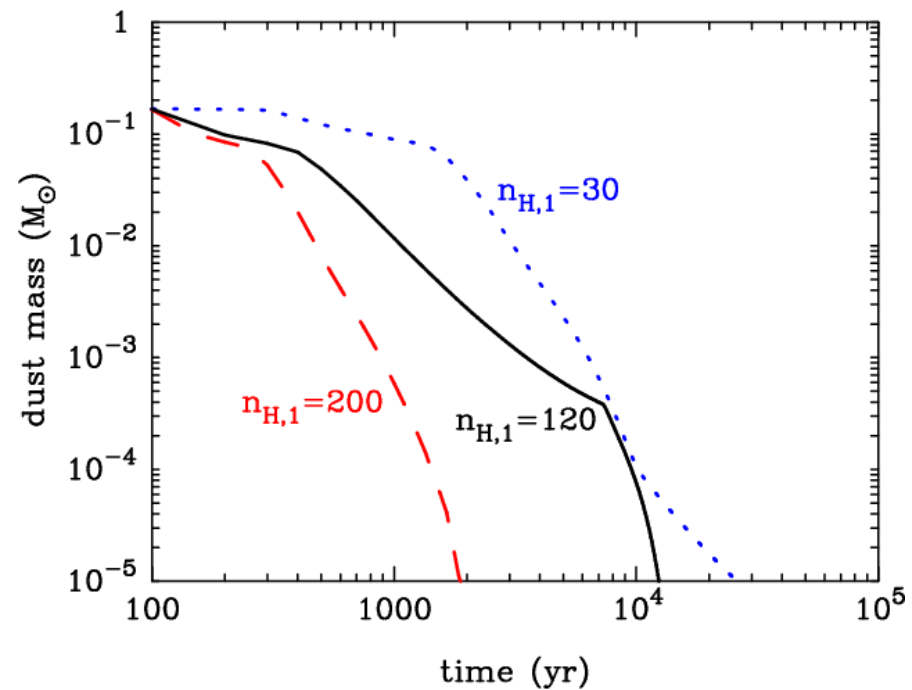
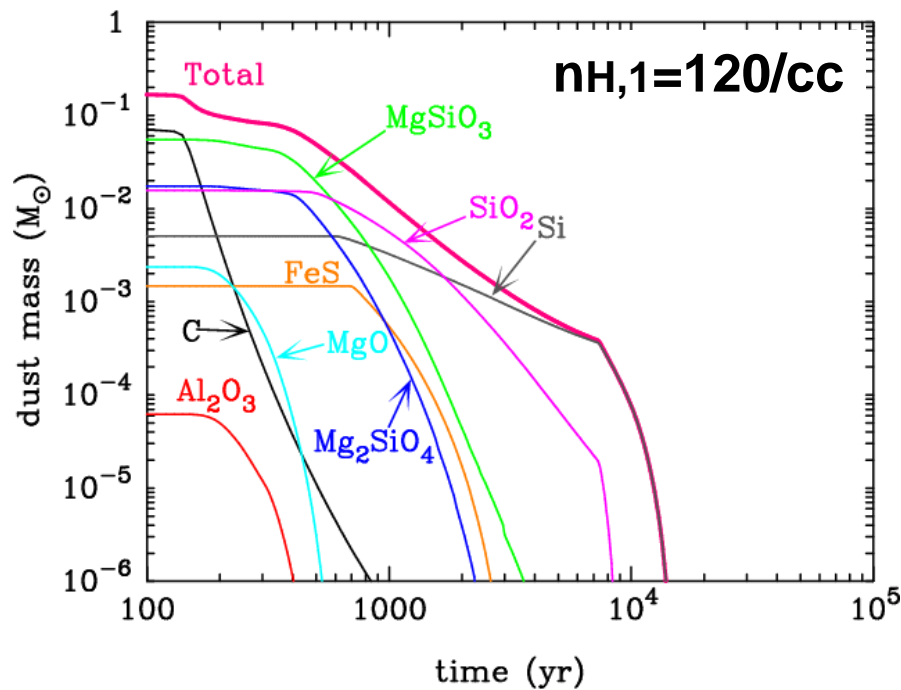
$$r_1 = r(\text{at } 10 \text{ yr}) = 1.2 \times 10^{18} \text{ cm}$$

$$n_{H,1} = 30, 120, 200 / \text{cc}$$

$$\left(\rightarrow dM/dt = 2.0, 8.0, 13 \times 10^{-5} M_{\text{sun}}/\text{yr} \text{ for } v_w = 10 \text{ km/s} \right)$$

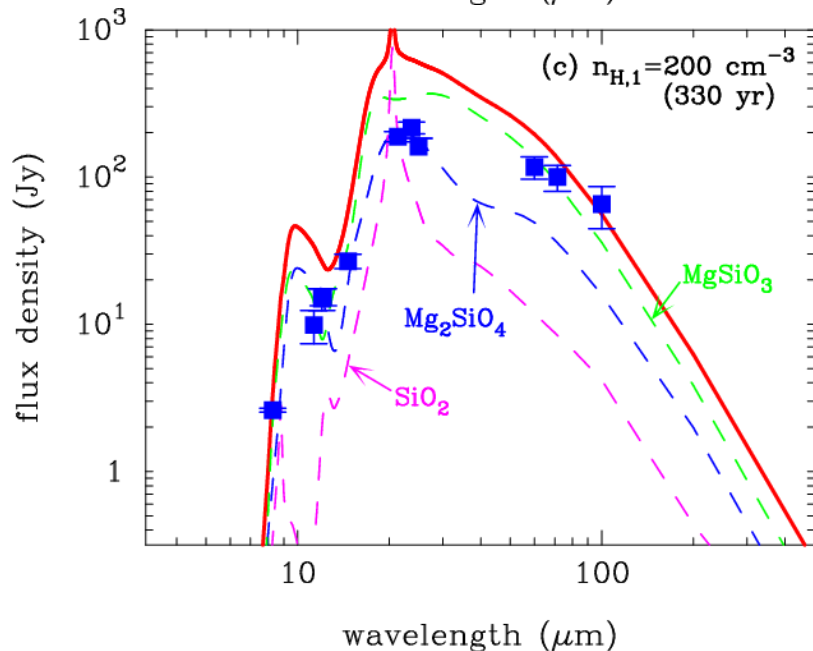
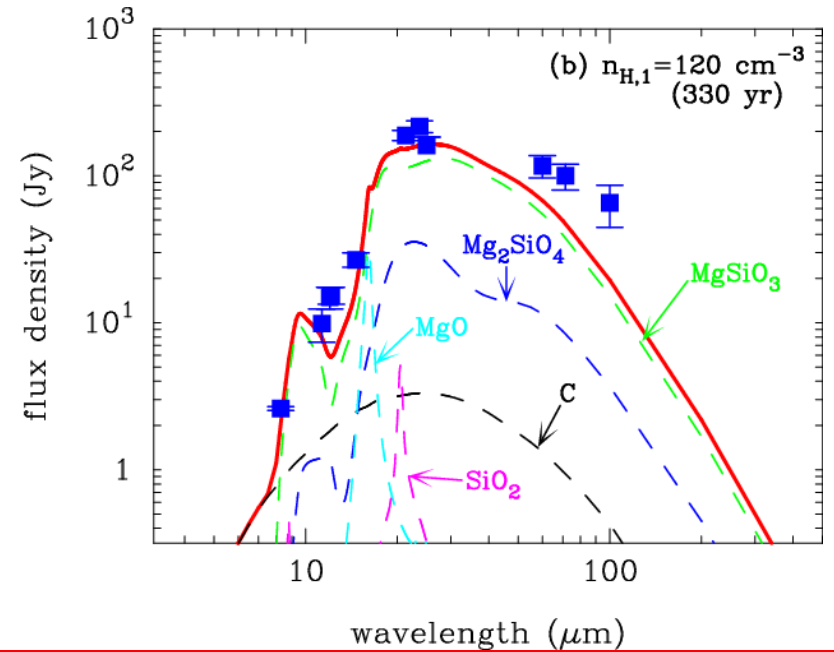
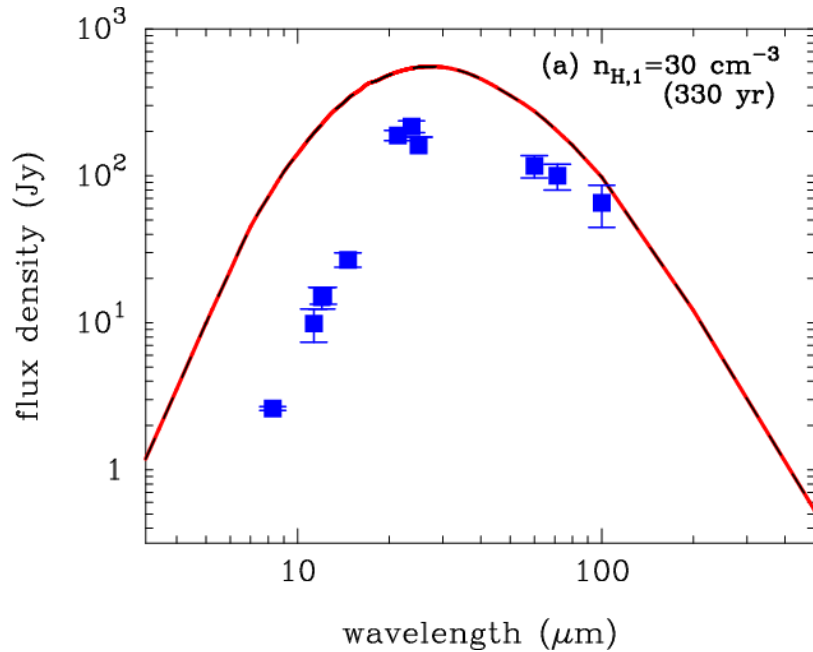


3-6. Fate of dust in Cas A SNR



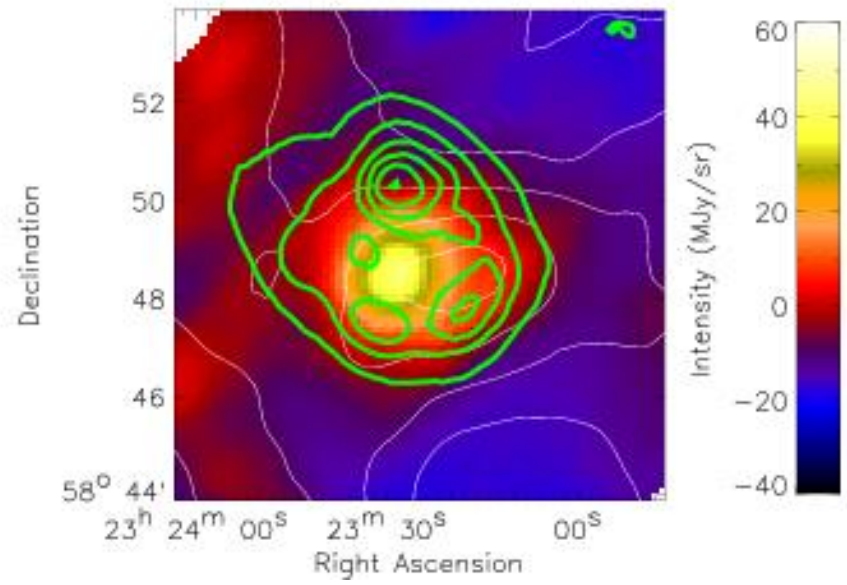
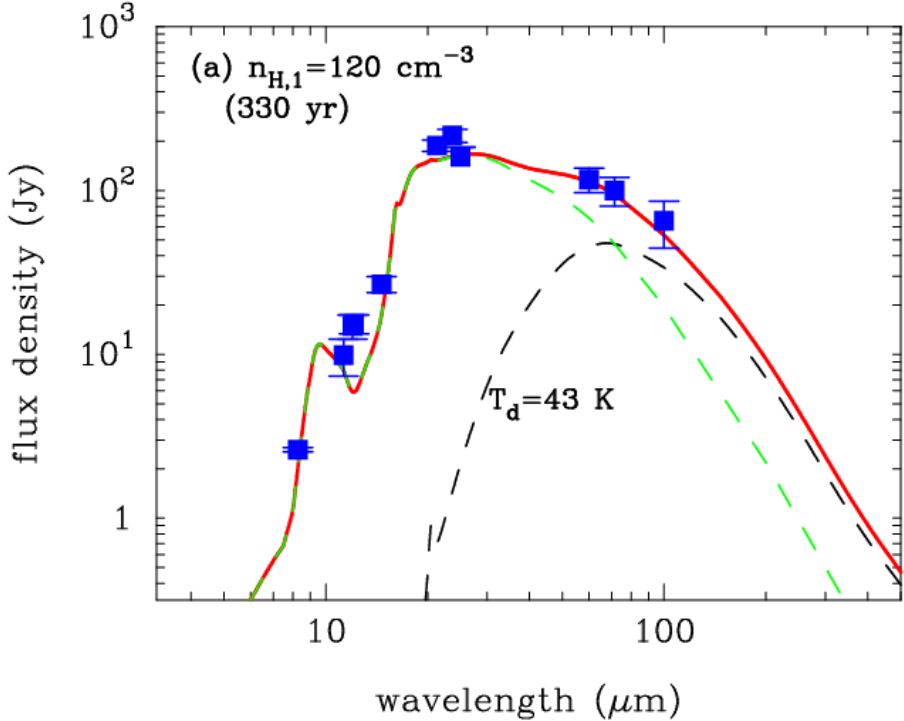
- All of the dust grains in Cas A would be destroyed in the shocked gas within the SNR before $\sim 2 \times 10^4$ yr
 - small grain size of newly formed dust
 - early arrival of the reverse shock at the He core
- **H-deficient SNe may not be major contributors of dust**
- **0.01-0.8 M_{sun} of dust survive for SNe II-P (Nozawa+2007)**

3-7. Comparison with observations of Cas A



- **MIR, $d = 0.008 \text{ Msun}$**
(Mshocked, $d \sim 0.1 \text{ Msun}$)
- **$dM/dt = 8 \times 10^{-5} \text{ Msun/yr}$**
→ $dM/dt \sim 2 \times 10^{-5} \text{ Msun/yr}$ for
Cas A (Chevalier & Oishi 2003)
→ $dM/dt = (3-4) \times 10^{-5} \text{ Msun/yr}$
for **93J** (Suzuki & Nomoto 1995)

3-8. Contribution from unshocked dust



Sibthorpe et al. 2009

observed IR SED can be well reproduced !

↑

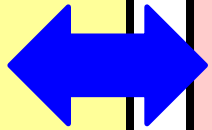
- $M_{d,warm} \sim 0.008 M_{sun}$
- $M_{d,cool} \sim 0.07 M_{sun}$ with $T_{dust} \sim 40 \text{ K}$

AKARI reduced 90 μm image

→ **centrally peaked cool dust component**

↓

$M_{d,cool} = 0.03-0.06 M_{sun}$ with $T_{dust} = 33-41 \text{ K}$



Summary

1) Birth of Dust in the ejecta of Cas A

Dust formed in Cas A was formed at 300-700 days after the explosion with $a_{\text{dust}} < 0.01 \mu\text{m}$ and $M_{\text{dust}} = 0.167 M_{\text{sun}}$

2) Brightening of dust in the shocked hot gas

Model of dust destruction and heating in Type IIb SNR can reasonably reproduce the observed SED of Cas A;

$$M_{\text{d,warm}} = 0.008 M_{\text{sun}}, M_{\text{d,cool}} = 0.07 M_{\text{sun}}$$

$$dM/dt = \sim 8 \times 10^{-5} M_{\text{sun}}/\text{yr}$$

3) Fate of dust in Cas A SNR

Small dust grains in Cas A will be completely destroyed in the shocked gas without being injected into the ISM