EARLY FORMATION OF DUST IN THE EJECTA OF TYPE Ib SN 2006jc
AND TEMPERATURE AND MASS OF THE DUST

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Received 2008 January 13; accepted 2008 May 8

ABSTRACT
SN 2006jc is a peculiar supernova (SN), in which the formation of dust has been confirmed at an early epoch of ~50 days after the explosion. We investigate the possibility of such an early formation of dust grains in the expanding ejecta of SN 2006jc, applying the Type Ib SN model that is developed to reproduce the observed light curve. We find that the rapid increase of the gas temperature in SN 2006jc enables the condensation of C grains in the C-rich layer at 40–60 days after the explosion, which is followed by the condensation of silicate and oxide grains until ~200 days. The average radius of each grain species is confined to be less than 0.01 μm due to the low gas density at the condensation time. The calculated total dust mass reaches ~1.5 M⊙, of which C dust shares 0.7 M⊙. On the other hand, based on the calculated dust temperature, we show that the dust species and mass evaluated to reproduce the spectral energy distribution observed by AKARI and MAGNUM at day 200 are different from those obtained by the dust formation calculations; the dust species contributing to the observed flux are hot C and FeS grains with masses of 5.6 × 10^{-4} and 2.0 × 10^{-3} M⊙, respectively, although we cannot deny the presence of a large amount of cold dust such as silicate and oxide grains up to 0.5 M⊙. One of the physical processes responsible for the difference between calculated and evaluated masses of C and FeS grains could be considered to be the destruction of small-sized clusters by energetic photons and electrons prevailing within the ejecta at the earlier epoch.

Subject headings: dust, extinction — supernovae: general — supernovae: individual (SN 2006jc)

1. INTRODUCTION
Supernova (SN) 2006jc is a peculiar Type Ib SN (SN Ib) in which the formation of dust has been observationally confirmed at a very early time of ~50 days after the peak brightness (Smith et al. 2008), which is more than a few hundred days earlier than those for the dust-forming SNe observed so far. Evidence for dust formation in SN 2006jc comes from an increase of the red to near-infrared (NIR) continuum (Di Carlo et al. 2008) and the simultaneous emergence of blueshifted narrow He i emission lines (Smith et al. 2008). Smith et al. (2008) have proposed that the detected dust does not condense in the ejecta but forms in the dense postshock gas swept up by the forward and reverse shocks. Although X-ray observations of Swift and Chandra (Immler et al. 2008) suggested the presence of a dense circumstellar (CS) shell ejected by the outburst similar to those seen in luminous blue variables (LBVs) 2 yr prior to the explosion (Nakano et al. 2006; Pastorello et al. 2007), the postshock CS gas density estimated from the X-ray light curve (Tominaga et al. 2008) is not high enough for dust grains to condense. Thus, it is reasonable to consider that the appearance of dust toward SN 2006jc should be the outcome of ongoing dust formation in the expanding ejecta of the SN.

Several pieces of evidence for dust formation in the SN ejecta have been reported for Type II SNe (SNe II): SN 1987A (Lucy et al. 1989; Whitelock et al. 1989; Meikle et al. 1993; Wooden et al. 1993; Colgan et al. 1994), SN 1998S (Gerardy et al. 2000; Pozzo et al. 2004), SN 1999em (Elhamdhi et al. 2003), and SN 2003gd (Sugetman et al. 2006; Meikle et al. 2007). For these SNe II except for SN 1998S, the onset of dust formation is estimated to be later than 400 days after explosion. The Type IIn SN 1999BS with the relatively low-mass hydrogen envelope (e.g., Liu et al. 2000; Fransson et al. 2005) exhibits signatures of dust condensation at around 230 days (Gerardy et al. 2000). In addition, SN 1990I is the first SN Ib signifying the ongoing dust formation, in which dust formation is observed at ~230 days (Elhamdhi et al. 2004). On the other hand, the signature of dust formation in SN Ib/c has not been recorded so far. Although theoretical studies have shown the feasibility of dust formation in SNe Ib/c (Kozasa et al. 1989, 1991; Todini & Ferrara 2001; Nozawa et al. 2003), the possibility of dust formation in SNe Ib/c has never been explored to date. Hence, how the formation process of dust in the ejecta depends on the type of SNe is an important subject to be pursued.

Since the progenitor stars of SNe Ib/c have lost most of the hydrogen/helium envelopes before the explosion, their ejected masses are smaller, and the expansion velocities are significantly higher than SNe II. This leads to a lower density of gas in the ejecta, and the gas temperature drops down more quickly than those in typical SNe II. This allows us to expect earlier dust formation in SNe Ib/c than SNe II. On the other hand, the lower gas density may even result in unsuccessful dust formation. Furthermore, in the early epoch, energetic photons and electrons generated by the Compton degradation of γ-rays from the decay of radioactive elements such as 56Ni and 56Co prevail throughout the ejecta, and may affect the formation process of dust grains. SN 2006jc is an
ideal laboratory for examining the process of dust formation in SNe Ib because a copious amount of observational data enable us to compare with theoretical models. In this paper we investigate, for the first time, the possibility of dust formation in the expanding ejecta of a SN Ib, based on the SN model that can well reproduce the light curve of SN 2006jc (Tominaga et al. 2008).

The paper is organized as follows. In § 2 we summarize the observational evidence for dust formation in SN 2006jc and its interpretation, which are compared with the calculations of dust formation in the later sections. In § 3 we investigate the dust formation in the ejecta and show that it is possible for dust grains to condense in the ejecta of SN 2006jc at very early times of about 50 days after explosion. In § 4 we calculate the temperature of possible condensates obtained in § 3 and evaluate the amount of dust grains contributing to the spectral energy distribution observed with AKARI and MAGNUM at day 200. Formation processes of dust grains in SN 2006jc are discussed in § 5, focusing on the interpretation of the difference between dust mass obtained by the dust formation calculation and that evaluated from the spectral fitting. The summary is presented in § 6. In this paper we assume that the explosion of SN 2006jc has occurred at 15 days before its discovery.

2. OBSERVATIONS OF DUST FORMATION IN SN 2006jc AND ITS INTERPRETATION

2.1. Evidence for Dust Formation

The first verification of the presence of dust in SN 2006jc comes from the rebrightening at J, H, and K bands around day 50 (Arkharov et al. 2006; Di Carlo et al. 2008). In addition, Di Carlo et al. (2008) have noted a concomitant steep drop of the light curve in the optical bands starting from 70 days, suggestive of strong extinction by the newly formed dust. It is also shown that this rapid decline of the optical light curve continues up to ~120 days (Tominaga et al. 2008; G. C. Anupama et al. 2008, in preparation; K. S. Kawabata et al. 2008, in preparation; Mattila et al. 2008).

Definitive evidence for dust formation has been reported by Smith et al. (2008); the asymmetry of narrow He i emission lines increased concurrently with an increase in the red-to-NIR continuum between 65 and 120 days. The increasing red/NIR continuum is interpreted as the thermal radiation from the newly formed carbonaceous dust with a temperature of ~1600 K, considering its high temperature. At day 140, the excess of this continuum disappeared, which indicates that the dust grains were completely destroyed or the dust temperature became so low that its thermal emission was shifted to longer wavelengths. The increasing asymmetry of narrow He i emission lines tracing the shocked CS gas was caused by the dust obscuration of the redshifted side, whereas broad emission lines tracing the SN ejecta such as Ca ii and O i faded entirely. The blueshifts of He i emission lines persisted up to day 180 (Mattila et al. 2008), asserting that the newly formed carbon grains were not destroyed but cooled down, which is supported by the NIR observations with AKARI (Sakon et al. 2007) and MAGNUM (Minezaki et al. 2007) showing that the temperature of the carbon grains dropped down to ~800 K at day 215.

The time evolution of the optical light curve and the He i emission-line profile during 50–140 days strongly suggests the ongoing formation of dust in SN 2006jc and reliably rules out as origins of the red/NIR continuum the scenarios involving pre-existing dust in the CS medium (CSM), such as the IR light echo (Smith et al. 2008; Mattila et al. 2008) and the heating of the CS dust through the collision with the forward shock. However, as suggested by Sakon et al. (2007) and Mattila et al. (2008), the mid-IR spectrum observed at a later epoch (>200 days) can be attributed to the low-temperature CS dust, which is discussed in § 4.2.

2.2. The Site of Dust Formation

Smith et al. (2008) have supposed that dust grains are formed in the dense shell swept up by shocks but not in the freely expanding ejecta, based on (1) the geometrical considerations for explaining the blueshifts of narrow He i lines and the overall fading of broad Ca ii and O i lines and (2) the time evolution of dust temperature that remains nearly constant for about a month and decreases after then; they considered that dust can continuously form at a temperature of ~1600 K in the rapidly cooling regions behind the forward shock rather than the reverse shock, in the course of the passage of the forward shock through the dense CS shell created by the LBV-like eruption 2 yr prior to the SN explosion. This scenario is supported by a flux ratio of He i λ7065/λ5876 close to unity and the He ii λ4686 emission feature that appeared during the putative time of dust formation. The detection of these He lines is expected to indicate the presence of the postshock gas of ~3 × 10^{-14} g cm^{-3} that is comparable to the critical density for carbon grain condensation (e.g., Clayton 1979), although Mattila et al. (2008) cannot find the sign of the He ii line in their spectrum during 88–132 days.

Here we investigate whether dust formation in the postshock gas around SN 2006jc is possible or not, referring to the X-ray observations and the hydrodynamical calculations for the ejecta-CSM interaction. Observations with the Swift and Chandra satellites (Immler et al. 2008) have shown that the X-ray luminosity is in the range of 10^{39}–10^{40} ergs s^{-1} from day 36 through day 180, with a gentle rise of the X-ray emission until 110 days. Immler et al. (2008) have estimated the density of the postshock gas shell to be ~4 × 10^{-17} g cm^{-3}, assuming that all of the measured X-rays at peak are emitted from the dense shocked shell. However, the time evolution of the X-ray luminosity indicates that the medium around SN 2006jc has a quite smooth density profile. Tominaga et al. (2008) have performed the hydrodynamical calculations to reproduce the observed X-ray light curve and found that the density profile of the preshock CSM should be \rho_0 = 2.75 \times 10^{-19} g cm^{-3} for r < 2.2 \times 10^{16} cm and \rho = \rho_0(r/2.2 \times 10^{16} cm)^{-6} g cm^{-3} for r \geq 2.2 \times 10^{16} cm. Their result has shown that the gas density swept up by the forward and reverse shocks is \leq 10^{-17} g cm^{-3} at 50 days (see Fig. 11 in Tominaga et al. 2008), which is too low for dust grains to nucleate. Thus, on the basis of the hydrodynamical simulations, we conclude that dust grains are not likely to be formed in the postshock CS gas.

On the other hand, it should be addressed that there are some studies that advocate the formation of dust in the dense CS shell produced by the LBV-like outburst before 2 yr (Di Carlo et al. 2008; Mattila et al. 2008). Mattila et al. (2008) have shown that the observed X-ray luminosity is produced by the CS shell with a preshock density of (2.5–4) \times 10^{-14} g cm^{-3} in aid of their calculations of shock evolution, and that the NIR light curve is reproduced by the IR light echo of the dust newly formed in the dense, cooling CS shell. However, the formation process of dust heavily depends on the cooling history of the gas, and whether dust formation can be realized in the rapidly cooling postshock gas should be fully explored in future work. In the following sections we pursue the possibility of dust formation in the expanding ejecta of SN 2006jc.

3. DUST FORMATION IN THE EJECTA OF SN 2006jc

3.1. Model of SN 2006jc and Calculation of Dust Formation

The time at which dust condenses in the SN ejecta and the size and number density of the newly formed dust are sensitive to the
time evolution of the gas temperature and density (Kozasa et al. 1989; Todini & Ferrara 2001; Nozawa et al. 2003), given the elemental composition. In the calculation of dust formation, we apply the results of hydrodynamics and nucleosynthesis calculations for the SN Ib model well reproducing the observed bolometric light curve of SN 2006jc (Tominaga et al. 2008); the ejecta mass is 4.9 \( M_{\odot} \) with the explosion energy of \( E_{51} = 10 \) and the ejected \( ^{56}\text{Ni} \) mass of 0.22 \( M_{\odot} \), where \( ^{56}\text{Ni} \) is uniformly distributed in mass within the He core. The preexplosion mass of the progenitor is 6.9 \( M_{\odot} \). The elemental composition in the ejecta has an original onion-like composition, except for \( ^{56}\text{Ni} \). The time evolution of the gas temperature in the freely expanding ejecta was calculated by solving the radiative transfer and the energy equations, taking account of the energy deposition from \( ^{56}\text{Ni} \) and \( ^{56}\text{Co} \).

Figure 1 shows the structures of the gas temperature (Fig. 1a) and density (Fig. 1b) within the He core of the SN 2006jc model at 50 days (red solid lines) and day 200 (red dashed lines) after the explosion. For comparison, also shown are those for the SN II model (blue lines) with \( M_{\text{pr}} = 25 M_{\odot} \) and \( E_{51} = 1 \) (Umeda & Nomoto 2002), which has a He core of 5.5 \( M_{\odot} \), comparable to that of SN 2006jc. The mass coordinate is normalized by the mass of the He core.

The dust formation calculation is performed by applying a theory of nonsteady state nucleation and grain growth described in Nozawa et al. (2003). In the calculations, we assume the sticking probability of \( c^1_{1j} = 1 \), and that the temperature of a small cluster consisting of up to a few tens of atoms is the same as the gas temperature.\(^9\)

3.2. Results of Dust Formation Calculations

Figures 2a and 2b show the results of calculation. Figure 2a indicates the condensation time of the newly formed dust, defined as the time when the nucleation rate reaches the maximum (see Nozawa et al. 2003). It can be seen that in the outermost C-rich layer of the ejecta (see Fig. 8c in Tominaga et al. 2008), C grains condense at very early times of 40–60 days. This is due to the rapid decrease of the gas temperature in the ejecta, as well as the relatively high condensation temperature of C grains. It should be emphasized that the condensation times of C grains are in good agreement with the onset time of dust formation observed in SN 2006jc. Furthermore, the condensation of C grains can explain both the blueshift of He i lines and the entire fading.

\(^9\) There is a typographical error in eq. (3) for the nucleation rate in Nozawa et al. (2003); replace \( c^1_{ij} \) with \( c^2_{ij} \).
of Ca II and O I lines because the formation site is in the region between the He-rich CSM and the O-rich layer in the ejecta, although they cannot absorb the zero-velocity component of narrow He I emission lines efficiently.

After C grains are formed, Al2O3, Mg2SiO4, MgSiO3, SiO2, Fe2O3, MgO, and FeO grains form in the O-rich layer at 90–150 days in this order, and FeS and Si grains condense in the Si-I-rich layer at ~200 days. Since 56Ni is uniformly mixed throughout the ejecta, Fe2O3 and FeO grains are produced instead of Fe grains; Fe grains are expected to form in the innermost Fe-Ni core unless 56Ni intrudes into the outer layers (Nozawa et al. 2003). However, the mixing of elements is likely to be at the knotty level rather than at the microscopic atomic level, as suggested by the observations of the Cas A supernova remnant (Douvion et al. 2001; Ennis et al. 2006; Rho et al. 2008). If 56Ni is not mixed at the atomic level, the formation of Fe grains is expected as well. Nevertheless, Fe grains, which have a high-energy barrier for nucleation and a resulting low condensation temperature (~800 K), cannot form in the ejecta considered here because the gas density is too low at the time when the gas cools down to 800 K (~250 days). Also, Fe atoms originally existing in the O-rich layer are not locked into grains significantly (condensation efficiency of ~10^{-5}) owing to their small abundances. Considering these uncertainties, we rule out Fe2O3 and FeO grains as the newly formed dust species.

As is expected from the low gas density, as well as the rapid cooling of gas in the ejecta, the average radius of each dust species given in Figure 2b is considerably small, being less than 0.01 µm for all grain species. On the other hand, the condensation efficiency of dust is almost unity, and the amount of dust formed is relatively large. The total mass of newly formed dust is 1.45 M⊙, and the mass of C grains (0.7 M⊙) accounts for about a half of the total mass. The mass of each dust species M_{i,j} obtained by the dust formation calculation is summarized in Table 1. Other major grain species in mass are SiO2 (0.23 M⊙), Si (0.2 M⊙), and MgSiO3 (0.16 M⊙).

It should be noted here that the dust formation process as demonstrated above is not influenced by the interaction between the ejecta and the CSM. Our results show that dust grains cannot condense in the region of 0.005 M⊙ from the outer edge of the ejecta, where the gas density is too low. Although the ejecta-CSM interaction causes the reverse shock penetrating into the ejecta, the hydrodynamic simulation shows that the reverse shock sweeps up only ~0.011 M⊙ of the outermost region in the ejecta by 50 days and ~0.053 M⊙ by 200 days (see Fig. 11 in Tominaga et al. 2008). Thus, the reverse shock sweeps up 0.006 M⊙ from the outer edge of the dust formation region at day 50, and 0.048 M⊙ at day 200. The mass of C grains within the region swept up by 200 days is only 1.3 × 10^{-3} M⊙, which is much smaller than 0.7 M⊙ at the time of formation; thus, almost all of the C grains can form in the freely expanding ejecta. Since the radii of C grains formed in the outermost region are smaller than 10 Å (see Fig. 2b), the timescale of dust destruction by sputtering is estimated to be <~6 hr (Nozawa et al. 2006) in the shocked gas with density of ~10^{-18} g cm^{-3} (Tominaga et al. 2008). Hence, thermal emission from shock-heated grains can be negligible.

### 4. EVALUATION OF DUST TEMPERATURE AND MASS IN THE EJECTA

The NIR to mid-IR (MIR) observations with AKARI (Sakon et al. 2007) and MAGNUM (Minezaki et al. 2007) have detected thermal emission from dust in SN 2006jc at ~200 days. Sakon et al. (2007) have concluded that the obtained NIR spectrum is fitted by amorphous carbon grains of 800 K with a mass of 6.9 × 10^{-5} M⊙, assuming optically thin thermal radiation. They have also shown that the MIR excess emission over the amorphous carbon grains of 800 K can be explained either by silicate and silicic grains of 700–800 K with ~10^{-4} M⊙ or by amorphous carbon grains of 320 K with 2.7 × 10^{-3} M⊙. In this section, referring to the grains species calculated in § 3 as possible condensates in the ejecta and deriving the dust temperature, we evaluate the dust mass by reproducing the spectral energy distribution observed at day 200 with AKARI and MAGNUM.

#### 4.1. Temperature of Dust

The equilibrium temperature of dust in the ejecta is determined by the balance between heating and cooling through radiation and collision with gas. In order to calculate the heating due to the absorption of ambient radiation, we evaluate the flux F_{r}(t,r) at a time t and a position r within the ejecta, assuming that the total flux F_{r}(t) calculated by Tominaga et al. (2008) radiates as a blackbody with temperature T_{BB}(r,t).

Given the gas temperature T_{gas}(r,t) and number density n_{gas}(r,t) in the ejecta, the equilibrium temperature of dust T_{d}(r,t) at a given time and at a given position is determined by implicitly solving the equation

\[
4\pi a^{2} \sigma_{B} T_{d}(r,t) \int_{0}^{\infty} \pi a^{2} Q_{d}(a) B_{i}(T_{BB}) d\lambda + 4\pi a^{2} n_{gas}(c_{s} + \frac{1}{2} k) \left[ T_{gas} \left( \frac{k T_{gas}}{2\pi \mu m_{H}} \right)^{1/2} - T_{d} \left( \frac{k T_{d}}{2\pi \mu m_{H}} \right)^{1/2} \right] = F_{r}(t) / \sigma_{B} T_{BB}^{4},
\]

where a is the radius of dust, \sigma_{B} is the Stefan-Boltzmann constant, (Q_{d}(a,T)) is the Planck-mean of absorption coefficient, B_{i}(T) is the Planck function, k is the Boltzmann constant, c_{s} is the heat capacity of a gas molecule (c_{s} = 3k/2 for a monatomic molecule), \mu is the mean molecular weight, and m_{H} is the atomic mass unit. Here we consider that the gas colliding with dust is completely accommodated and is ejected from the surface with the same temperature as the dust (see Landau & Pitaevski 1981).

In the calculations we assume T_{BB} = 5000 K throughout the ejecta.

### Table 1: Mass of Each Dust Species and References for Optical Constants

<table>
<thead>
<tr>
<th>Dust Species</th>
<th>M_{1,i} (M_{⊙})</th>
<th>M_{2,i} (M_{⊙})</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>0.701</td>
<td>5.6 × 10^{-4}</td>
<td>1</td>
</tr>
<tr>
<td>Al2O3</td>
<td>0.008</td>
<td>≤0.008</td>
<td>2</td>
</tr>
<tr>
<td>Mg2SiO4</td>
<td>0.157</td>
<td>≤0.157</td>
<td>3</td>
</tr>
<tr>
<td>MgSiO3</td>
<td>0.082</td>
<td>≤0.082</td>
<td>4</td>
</tr>
<tr>
<td>SiO2</td>
<td>0.229</td>
<td>≤0.229</td>
<td>5</td>
</tr>
<tr>
<td>MgO</td>
<td>0.010</td>
<td>≤0.010</td>
<td>6</td>
</tr>
<tr>
<td>FeS</td>
<td>0.067</td>
<td>0.002</td>
<td>4</td>
</tr>
<tr>
<td>Si</td>
<td>0.196</td>
<td>.</td>
<td>7</td>
</tr>
<tr>
<td>Total</td>
<td>1.450</td>
<td>≤0.489</td>
<td></td>
</tr>
</tbody>
</table>

Notes:— The mass of grain species i obtained by the dust formation calculation is denoted by M_{i,j}. The mass or upper mass limit of the dust necessary for reproducing the SED observed at 200 days is denoted by M_{2,i,j}, where Si grains are excluded because their condensation time could be much later than 200 days (see text). References for the optical constants used in the calculation are shown in the last column. The optical constants of MgSiO3 at λ ≤ 0.3 μm are replaced by that of Mg2SiO4 (see Hirashita et al. 2008).

regardless of time, and \( a = 0.01 \mu m \). Since in the ejecta considered here the total flux at day 200 is \( F \sim 10^6 \text{ erg s}^{-1} \text{ cm}^{-2} \) almost uniformly over the He core, the energy transferred through the radiative process is much larger than that by collision with gas, and thus we can neglect the collisional heating and cooling. Note that in this case the calculated dust temperature is independent of dust size because \( Q_J(a)/a \) does not depend on the radius for \( a \leq 0.05 \mu m \). The references for the optical constants of each dust species used in the calculations are given in Table 1.

We also note that the effect of stochastic heating can be negligible as long as we assume a blackbody radiation with \( T_{BB} \sim 5000 \text{ K} \) under the given total flux. We have confirmed that for C grains of 10 (20) \( \mu m \), stochastic heating only makes the dust temperature distribute symmetrically around the equilibrium temperature with the temperature width of \( \pm 100 \) (30) K. Accordingly, the resulting emissivity of 10 \( \mu m \)-sized C grains does not change significantly at wavelengths longer than 2 \( \mu m \), compared with that derived for equilibrium temperature; its difference is 10% at 2 \( \mu m \) and less than 2.5% at \( \geq 3 \mu m \). Therefore, stochastic heating does not affect the results of the IR spectrum energy distribution calculated in § 4.2.

Figure 3 shows the temperatures of all dust species at 200 days (solid lines), along with the temperature of C grains at 60 days (dashed lines).\(^{10}\) The temperature of the C grains is 1200–1700 K at 60 days and is higher for those formed in the inner region. Note that this high temperature is in good agreement with the temperature of dust responsible for the red/NIR continuum appearing in SN 2006jc two months after the explosion (Smith et al. 2008). At 200 days, the C grains cool down to 500–600 K, which is also considered to correspond to the temperature of 800 K for amorphous carbon grains suggested by the observations with AKARI and MAGNUM (Sakon et al. 2007), although the calculated temperature is relatively low. Thus, the calculated temperature of C grains can reasonably explain the time evolution of the dust temperature indicated by the observations toward SN 2006jc from day 50 through day 200.

On the other hand, silicate grains have a temperature of only 100–200 K at day 200, reflecting much lower absorption efficiency at optical wavelengths than at IR wavelengths. This low temperature cannot explain the MIR excess emission over the amorphous carbon grains with 800 K observed by AKARI (Sakon et al. 2007), and we can conclude that neither silicate nor silica grains newly formed in the ejecta can be the carriers of the MIR excess emission. In addition, our result shows that the temperature of C grains spans the range from 500 to 600 K. Therefore, if the MIR excess emission were attributed to the amorphous carbon grains with 320 K, they might not be the grains formed in the ejecta but could be the preexisting CS grains heated by the SN outburst, as suggested by Sakon et al. (2007).

In the calculations we assumed the ambient radiation field as a blackbody with \( T_{BB} = 5000 \text{ K} \). The calculated dust temperatures at day 200 is not sensitive to \( T_{BB} \) as long as \( T_{BB} \) is in the range 5000–6000 K; for \( T_{BB} = 6000 \text{ K} \), the temperature of MgSiO\(_3\) and Mg\(_2\)SiO\(_4\) grains increases by \( \sim 50 \) K compared with that for \( T_{BB} = 5000 \text{ K} \), while the increase of temperature of the other grains species is at most 30 K. Here, it should be kept in mind that, being different from normal SNe Ib, SN 2006jc shows the strange optical spectrum in the early times until day 120, with a bright blue continuum whose origin is not clear (Foley et al. 2007; Pastorello et al. 2007). This indicates that the spectrum of radiation at the early epoch within the ejecta of SN 2006jc is not also expected to be approximated by a blackbody radiation. Nevertheless, as shown above, we can reasonably explain the time evolution of temperature of C grains indicated by the observations. Thus, we adopt the results for \( T_{BB} = 5000 \text{ K} \) in the following discussions.

4.2. IR Spectral Energy Distribution and Dust Mass

In this subsection we calculate thermal emission from dust grains based on the dust temperatures presented in Figure 3, and estimate the dust mass necessary for reproducing the spectral energy distribution (SED) at day 200 observed with AKARI and MAGNUM.

Taking into account the self-absorption of dust, the observed flux density \( F_{\nu}^{\text{obs}} \) of thermal emission from dust grains formed in the ejecta is evaluated by

\[
F_{\nu}^{\text{obs}} = \frac{1}{4\pi D^2} \int_0^R 4\pi r^2 m_{d,j}(r) \kappa_{\nu,j} B_\nu(T_J(r)) \exp\{-\tau_{\nu,j}(r) - \tau_{\nu}(r)\} \, dr,
\]

where \( D = 25.8 \) pc is the distance from observers (Pastorello et al. 2007), \( R \) is the outermost radius of the dust-forming region in the ejecta, \( m_{d,j}(r) \) is the mass of dust species \( j \) per volume at the position \( r \), and \( \kappa_{\nu,j} = 3Q_{\nu,j}(a)/4a\rho_j \) is the mass absorption coefficient, and the dust bulk density \( \rho_j \) is taken from Nozawa et al. (2006). Note that \( \kappa_{\nu,j} \) does not depend on the size as long as \( a \leq 0.05 \mu m \). The optical depth \( \tau_{\nu} \) is given by

\[
\tau_{\nu}(r) = \int_0^r \sum_j m_{d,j}(r) \kappa_{\nu,j} \, dr.
\]

The magenta solid line in Figure 4 is the SED calculated by adopting the mass of each dust species \( M_{d,j} \) given in § 3.2, and the SED is dominated by thermal emission from C grains existing in the outermost ejecta as the result of the large optical depth due to their large mass. It is clear that the derived IR spectrum

\[\text{Fig. 3.—Temperature of each dust species formed in the ejecta of SN 2006jc at 200 days after the explosion. The dashed line depicts the temperature of C grains at 60 days.}\]
largely exceeds the observational data at $\gtrsim 3\, \mu m$ and cannot reproduce the observed SED.

The NIR-to-MIR spectrum can be fitted using the derived grain temperatures because dust temperature does not depend on the mass of dust, as can be seen from equation (1), so the dust mass can be used as a free parameter in order to reproduce the observations. We calculate thermal emission from dust grains by taking the mass of each grain species at the position $r$ as $j_i m_i(r)$ and fit the SED to the observational data, where the value of a free parameter $j_i(\leq 1)$ is assumed to be constant for a given dust species. The best-fitted result is displayed by the red solid line in Figure 4 and can well explain the observed NIR-to-MIR spectrum. The contribution of each grain species is depicted by the dashed lines, for which we adopt the masses of C and FeS grains and the upper mass limits of the other dust species given as $M_{d,j}$ in Table 1. Here the mass of C grains is $5.6 \times 10^{-4} M_\odot$, reduced by a factor of 1250 in comparison with the mass obtained by the dust formation calculation. FeS grains can also contribute to the SED spectrum because of its high temperature ($\sim 900$ K), and its mass is reduced to $2 \times 10^{-3} M_\odot$ ($j_f = 0.03$). On the other hand, silicates and oxide grains do not contribute to the SED spectrum because their temperatures are too low ($100-200$ K). Furthermore, the large optical depth of MgSiO$_3$ and Mg$_2$SiO$_4$ at MIR wavelengths prevents us from constraining the mass of these grain species. Thus, we cannot defy the existence of a large amount of cold dust reaching up to $\sim 0.5 M_\odot$ in the ejecta from the spectral fitting, and the dust mass derived under the optically thin assumption should be considered to be the lower limit (see also Meikle et al. 2007).

We also investigate the effect of the presence of amorphous carbon grains in the CSM on the observed spectrum, which have been suggested to contribute to the MIR spectrum at $\gtrsim 200$ days (Sakon et al. 2007; Mattila et al. 2008). In the calculations we take the temperature of CS carbon grains to be 320 K (Sakon et al. 2007). If their mass is smaller than $2.7 \times 10^{-4} M_\odot$, the best-fitted spectrum in Figure 4 is not influenced by the preexisting C grains. A further increase of CS dust mass can also reasonably reproduce the observed IR spectrum as seen from Figure 5, where the mass of newly formed and preexisting C dust is $2.24 \times 10^{-4}$ and $1.4 \times 10^{-3} M_\odot$, respectively (the mass of other newly formed dust is the same as that in Fig. 4). Therefore, the spectral fitting can allow the presence of low-temperature C grains in the CSM.

The emission from CS grains can be the IR light echo but not the thermal radiation from dust heated by the collision with the forward shock. This is readily demonstrated by considering the radius of dust cavity created by the evaporation of preexisting CS grains due to strong radiation from a SN. Taking the evaporation temperature of C grains to be 1800 K and using the SN peak luminosity of $10^{42.7}$ ergs s$^{-1}$ with the blackbody temperature of $\sim 6000$ K (Tominaga et al. 2008), we estimate the radius of the dust cavity to be $\lesssim 3 \times 10^{16}$ cm. Because the estimated radius of the dust cavity is comparable with the radius of the forward shock at $\sim 200$ days, the forward shock could not have swept a significant amount of CS dust. If we consider the radiation from the shock breakout as the heating source, which is expected to be brighter and have a higher blackbody temperature, the dust cavity may be extended so far that any CS dust cannot be swept up by the forward shock at $\sim 200$ days. Note that in this spectral fitting, the mass of newly formed C grains depends on the temperature and mass of CS dust, and in the following discussion we refer to the mass of C grains derived by the spectral fitting without CS dust in Figure 4.

5. DISCUSSION

5.1. Mass of Dust Formed in the Ejecta

As shown in § 4.2, the mass of C grains ($0.7 M_\odot$) obtained by the dust formation calculation is 3 orders of magnitude larger than that ($5.6 \times 10^{-4} M_\odot$) estimated from the spectral fitting to the observations. One of the reasons for this difference is considered to be the clumpy structure in the ejecta. In order to evaluate the dust mass necessary for reproducing the observed spectrum of SN 2003gd, Sugerman et al. (2006) performed the radiative transfer calculation taking account of the clumpy structure and found an increase in the estimated mass of dust in the ejecta by about 1 order of magnitude, compared with the mass derived for the
uniform distribution of dust. Nevertheless, the consideration of dust clumping does not seem to be sufficient to overcome the large gap. Thus, the difference in dust mass should stem from the process of dust formation in the ejecta.

One of the processes influencing dust formation is the non-local thermal equilibrium (non-LTE) effect. As seen from Figures 1 and 3, the dust temperature is not the same as the gas temperature; at 200 days the temperature of C grains (500–600 K) and silicate and oxide grains (100–200 K) is lower than the gas temperature with 700–1000 K. In the ejecta with a strong radiation field, the temperature of small clusters is expected to be higher than the gas temperature depending on the optical property. In this case, the non-LTE effect retards or hinders the formation of dust grains. Assuming that the optical properties of small carbon clusters are the same as those of small C grains, and applying a formula of nucleation rate taking into account the non-LTE effect by Kozasa et al. (1996), we realized that the non-LTE effect does not significantly affect the formation of C grains; the non-LTE effect only retards the formation of C grains by less than 10 days and does not affect the mass of C grains because the temperature of small carbon clusters is only 50 K higher than that of gas. Meanwhile, the non-LTE effect delays the formation of Si grains from ~200 to ~240 days. This is the reason why we exclude Si grains in reproducing the observed SED at day 200 in § 4.2.

Another process affecting the formation of dust in the ejecta is the energy deposition on small-sized clusters through the latent heat deposition at the condensation, as well as the collisions with high-energy photons and electrons. In the ejecta rich in condensable elements, the destruction of small-sized clusters by the deposition of latent heat could be significant unless the deposited energy is released by collisional and/or radiative processes efficiently. Also, at an early epoch after the explosion, energetic photons and electrons generated from the decays of radioactive elements $^{56}$Ni and $^{56}$Co prevail abundantly throughout the ejecta. Since the nucleation rate is determined by the balance between the growth and destruction rate of small-sized clusters, the energy deposition makes small-sized clusters unstable against the growth and as a result reduces the nucleation rate.

Although the nucleation rate can be reduced by increasing the critical cluster size, as demonstrated by Bianchi & Schneider (2007), there is no reason to cut the number of seed nuclei by increasing the critical size arbitrarily, apart from the uncertainty inherent in the standard nucleation theory arising from the evaluation of chemical potential of small-sized clusters. Thus, we examine the effect of energy deposition for dust formation at early times observed in SN 2006jc by reducing the sticking probability $\alpha_s$ for simplicity and comparing with the mass of dust evaluated in § 4.2. If we take $\alpha_s \sim 3 \times 10^{-3}$, we can obtain a mass of C grains of $\sim 5 \times 10^{-5} M_\odot$, while $\alpha_s \approx 0.3$ to produce FeS grains of $2 \times 10^{-5} M_\odot$. In this case, the condensation times of C and FeS grains are 40–67 and 190–200 days, respectively. While the destruction rate of small-sized clusters depends on the properties of materials forming dust grains, the difference in the sticking probability may be caused by the collisions with energetic photons and electrons, reflecting the difference in the condensation time of C and FeS grains; energetic photons and electrons are more abundant at day 50 than at day 200. The details of these microscopic processes are beyond the scope of this paper and will be investigated in the future study on the dust formation in SNe.

5.2. Early Condensation of Dust in SNe Ib

In § 3.2 we showed that the early formation of dust around 50 days is possible in SN 2006jc, whose progenitor has lost most of its He envelope (Foley et al. 2007; Tominaga et al. 2008). However, other dust-forming SNe Ib had not shown such an early formation of dust; SN 1990I displayed the diagnostics of dust formation around 230 days (Elmhamdi et al. 2004), although the condensation time is relatively earlier than that of SNe II. The peculiar Type Ib SN 2005bf shows a rapid decline of the light curve from 50 days after the explosion, but does not exhibit NIR brightening, in contrast to the case of SN 2006jc (Tominaga et al. 2005). Maeda et al. (2007) have shown that the quickly faded light curve of SN 2005bf can be explained by the newly born magnetized neutron star at the center. On the other hand, they have demonstrated that the blueshifted profiles of O I and Ca II observed at ~270 days can be explained by the obscuration of dust in the ejecta. If the blueshift of emission lines in SN 2005bf is attributed to the newly formed dust grains, the time of dust formation is considered to be later than 100 days and not to be so early as in SN 2006jc, although the epoch of dust formation in SN 2005bf was not specified by the observations.

The results of calculations revealed that the early formation of dust in SN 2006jc can be realized by the rapid decline of gas temperature, reflecting the large ratio of the explosion energy ($E_{51} = 10$) to the ejected mass ($M_{ej} = 4.9 M_\odot$); the ratio $E_{51}/(M_{ej}/M_\odot) \approx 2$ is much greater than $0.125–0.25$ for SN 2005bf (Tominaga et al. 2005) and $\approx 0.3$ for SN 1990I (Elmhamdi et al. 2004). Unfortunately, no literature has reported the explosion energy of the Type IIn SN 1998S, which had a time of dust condensation of ~230 days (Gerardy et al. 2000). Using the ejecta mass estimated from the He core of $4–6 M_\odot$ (Fassia et al. 2001; Pooley et al. 2002) and hydrogen envelope of $0.1–2 M_\odot$ (Fassia et al. 2000; Anupama et al. 2001) and taking $E_{51} = 1$ as the typical explosion energy, we can, however, deduce the ratio to be $E_{51}/(M_{ej}/M_\odot)$ = $0.125–0.25$ for SN 1998S, which is similar to or slightly less than those for SN 2005bf and SN 1990I. On the other hand, the ratio for the dust-forming SNe II is of order $0.1:0.1–0.2$ for SN 1987A (Shigeyama et al. 1988; Woosley 1988), 0.05–0.1 for SN 1999em (Elmhamdi et al. 2003), and $\approx 0.12$ for SN 2003gd (Hendry et al. 2005). Dust formation has not been yet observed on SNe Ic. However, the early dust formation in SNe Ic is also expected, because SNe Ic may well have $M_{ej}$ similar to SNe Ib.

In conclusion, we can speculate that as the envelope of a star at explosion is smaller and the explosion energy is higher, the condensation time of dust tends to be earlier. In order to prove these hypotheses and to investigate the formation process of dust in SNe, we need further observational and theoretical studies on dust formation in various types of SNe. In particular, the UV-to-MIR observations at early times for SNe Ib/c are promising to clarify the formation process of dust because its condensation time is much earlier than that for SNe II, as is shown above.

6. SUMMARY

We investigate the formation of dust grains in the ejecta of SN 2006jc by applying the SN model that can nicely reproduce its light curve. We find that the formation of dust in SN 2006jc is possible at early times, thanks to the rapid decrease of the gas temperature in the ejecta. The condensation of C grains is realized in the C-rich layer at very early times of ~50 days after the explosion. This is in good agreement with the time of the onset of dust formation indicated by the observations. In addition to C grains, the other grain species such as silicate and oxide grains are formed until ~200 days, with the average radii less than 0.01 $\mu$m. We suppose that the formation of dust earlier than SNe II is common to the hydrogen-deficient SNe and that SN 2006jc is its extreme case.
Furthermore, we calculate the dust temperature by considering the radiation field in the ejecta at the early epoch as a blackbody with $T_{BB} = 5000 \, K$. C grains have a temperature of $\sim 1600 \, K$ at 60 days and cool down to $\sim 600 \, K$ at 200 days. This temperature of C grains can reasonably explain the time evolution of the dust temperature suggested by the observations toward SN 2006jc from day 50 through day 200. The temperatures of silicates and oxide grains are 100–200 K at day 200 and are too low to contribute to the MIR spectrum observed with AKARI.

The comparison of the calculated SED with the observations of AKARI and MAGNUM shows that dust grains contributing to NIR/MIR flux are C and FeS grains whose masses are $5.6 \times 10^{-4}$ and $2 \times 10^{-3} \, M_{\odot}$, respectively. The masses of hot C and FeS grains obtained by the dust formation calculation are considerably larger than those estimated from the observations. This difference in dust mass may be explained by the destruction of small-sized clusters by the collisions with energetic photons and electrons. On the other hand, we cannot constrain the mass of low-temperature silicate and oxide grains in the ejecta from the spectral fitting. The spectrum fitting also shows that the observed MIR spectrum can be attributed to preexisting CS carbon grains with the mass up to $\sim 10^{-3} \, M_{\odot}$. In order to reveal the process of dust formation in the SN ejecta, it is essential to carry out UV-to-IR observations of various types of SNe. In particular, SNe Ib/c are the objects suitable for detecting signatures of dust formation by the optical to NIR observations because the condensation time of dust is much earlier than SNe II.

The authors are grateful to the anonymous referee for critical comments that were useful for improving the manuscript. The authors thank H. Hirashita, T. T. Takeuchi, and A. K. Inoue for their useful comments. This research has been supported in part by World Premier International Research Center Initiative (WPI Initiative), MEXT, Japan, and by the Grant-in-Aid for Scientific Research of the Japan Society for the Promotion of Science (18104003, 18540231, 19740094, 20340038, 20540226, and 20540227) and MEXT (19047004 and 20040004). These grants support T. N., T. K., N. T., M. T., S. K., K. M., H. U., and M. L.’s visit.

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