

"How equation of state affects explosions of core-collapse supernovae"

Tomoya Takiwaki
(RIKEN)

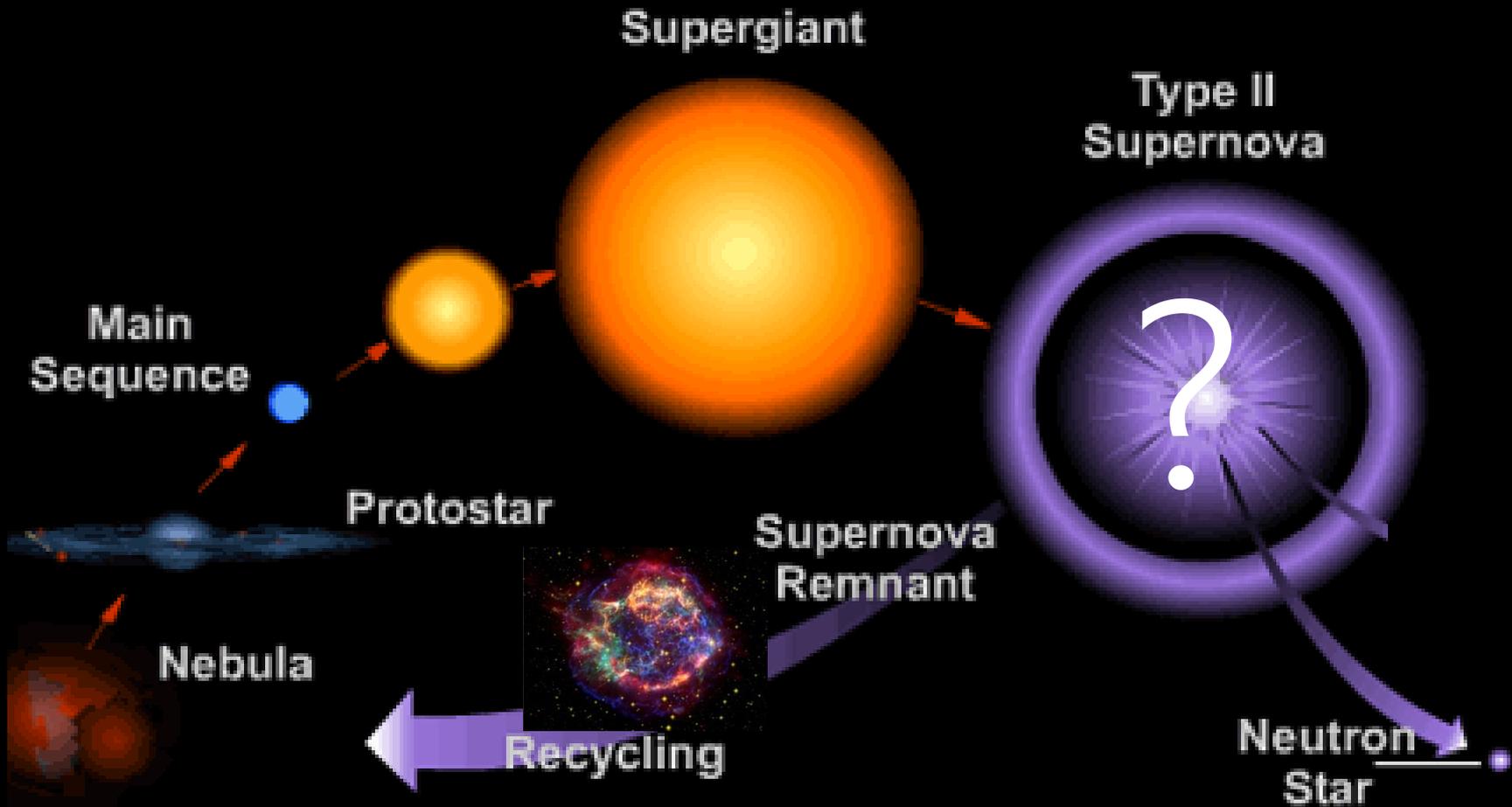
Collaborator:

Kei Kotake, Yudai Suwa and Takami Kuroda

Plan

- Recent status of SN simulations
- Our efforts for making sophisticated model
- How EOS affects the explosion
- Systematic studies of EOS(in progress)

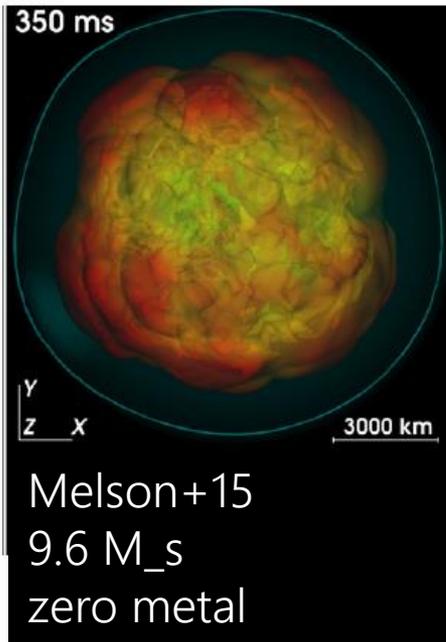
Supernovae: the death of the star



Q:How does the explosion occur?

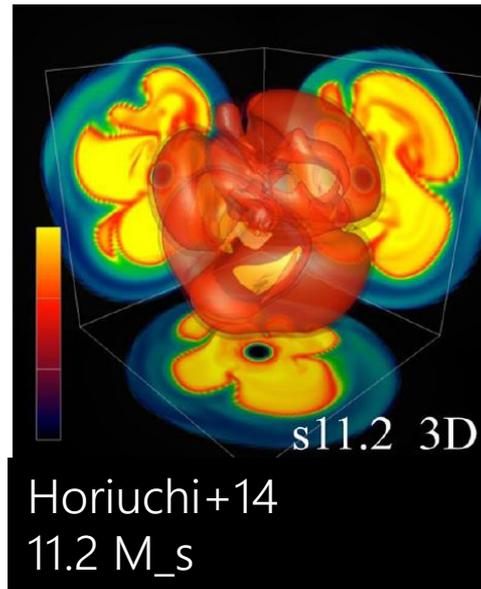
Current Status of SNe Mechanism

$M < 10M_s$



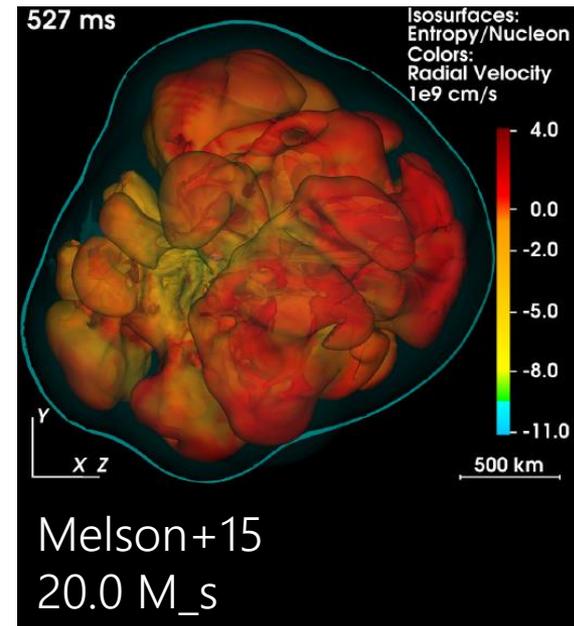
Dilute outer layer
Only ν -heating

$M < 15M_s$



ν -heating and
convection

$M < 40M_s$



ν -heating, convection
and SASI

Self-consistent 3D simulations with MG ν -transport
are available.

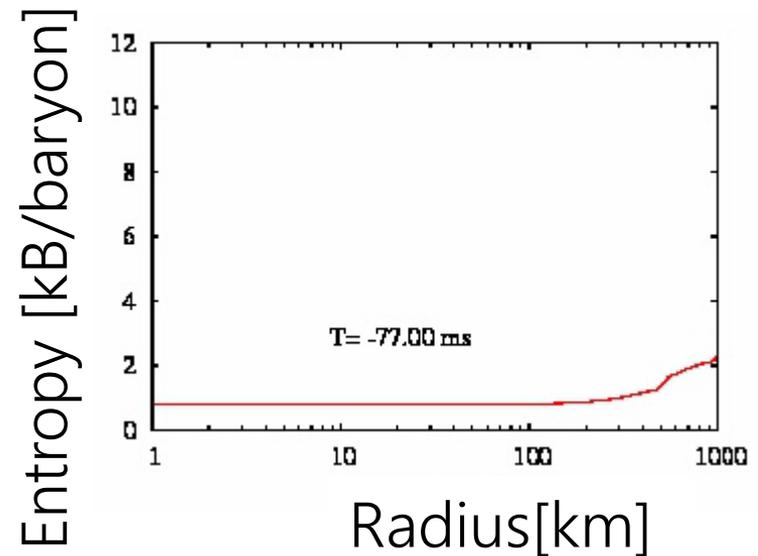
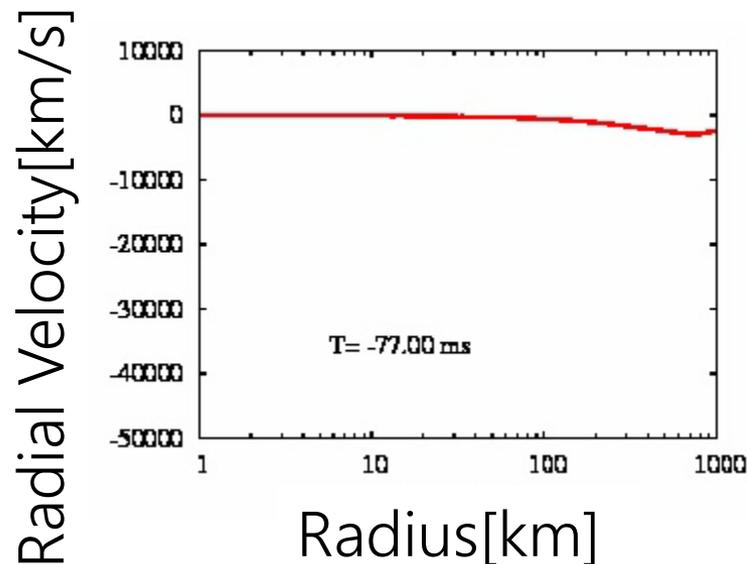
Typical 1D simulation

Velocity and Entropy profile in 1D

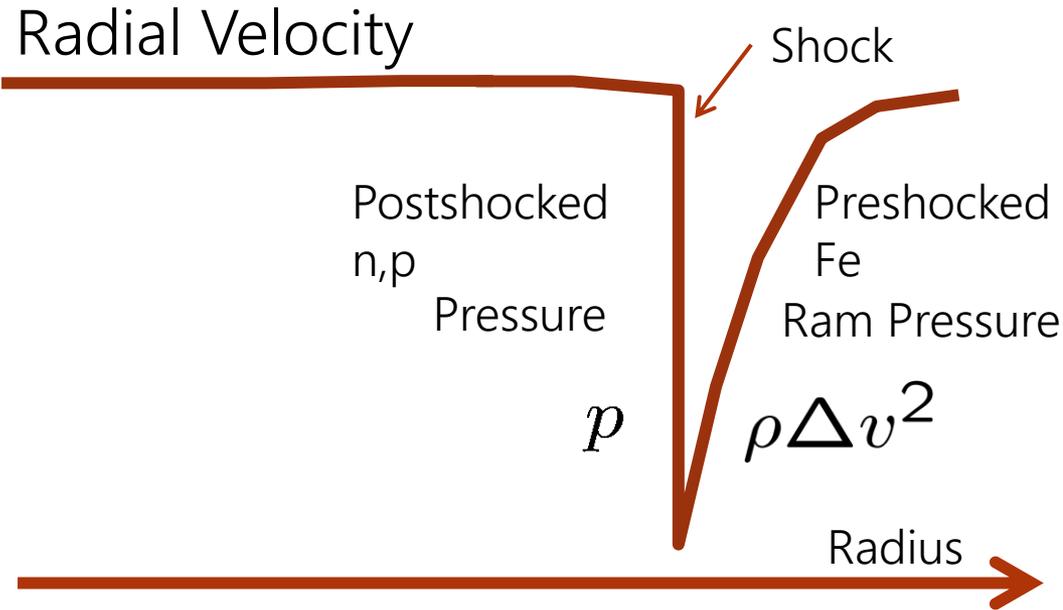
Entropy: T^3 / ρ

It's a good measure for the shock.

At the shock, kinetic energy is converted to heat and temperature increases (i.e. entropy also increases.)



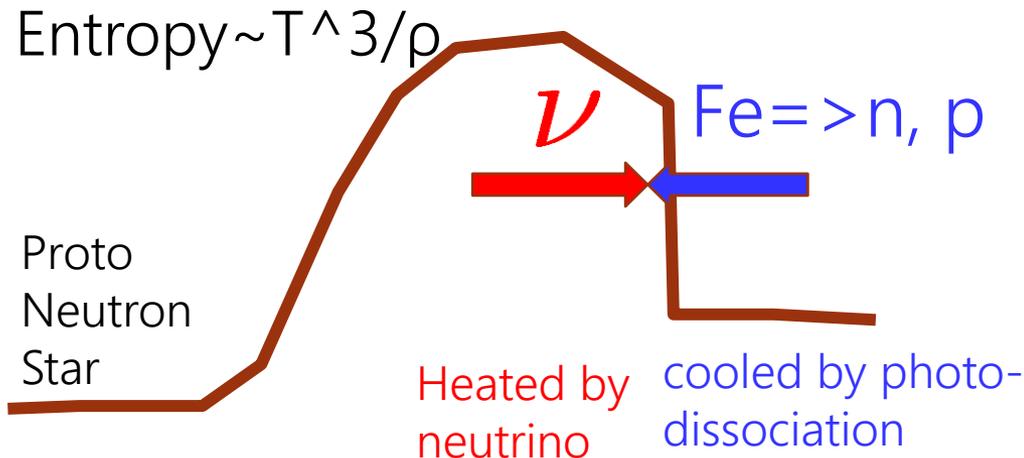
Key aspects of Neutrino Mechanism



When the shock is stalling, Pressure inside and ram pressure outside balances.

$$p \sim \rho \Delta v^2$$

RHS is determined by stellar structure (density profile).



LHS is determined by two ingredients.

(1) Photo-dissociation



(2) Neutrino Heating



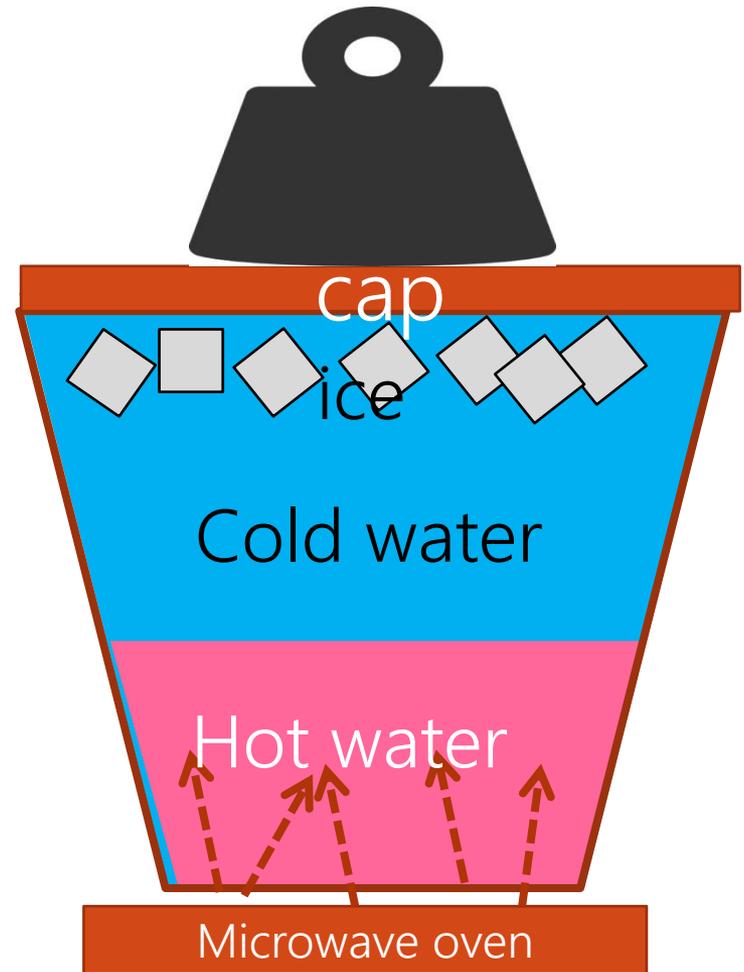
Problem

Supernova shock in simulation tends to stall and does NOT explode.

Long-lasting Problem ~1980.
In 2000-2005, state-of-the-art simulations with detailed neutrino transport confirm that!

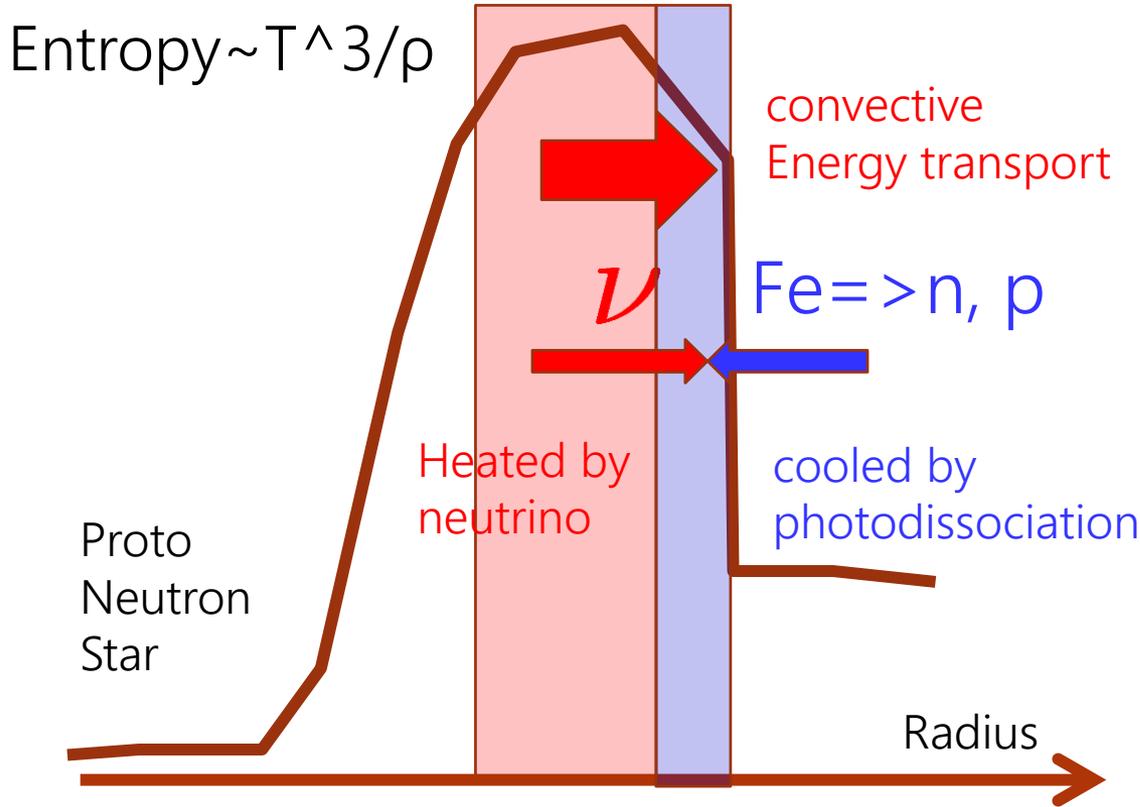
(Liebendoerfer+2001, Rampp+2002, Thompson+2003 and Sumiyoshi+2005)

(in 1D) Neutrino heating $<$ ram pressure
 \Rightarrow fails to explode!



From 1D to 3D

Key aspects of Neutrino Mechanism

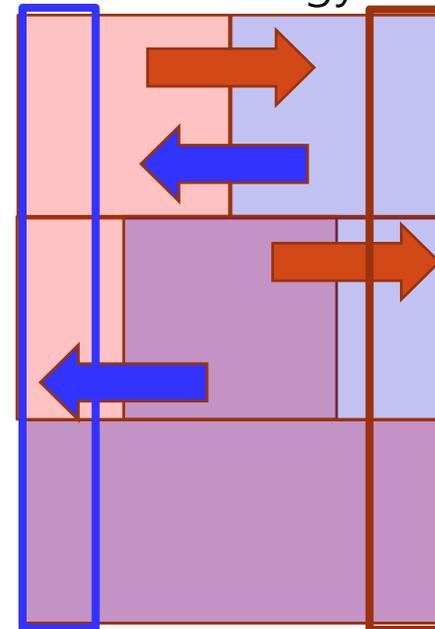


Cooler than the initial state but ν heat is active

Negative entropy gradient leads Rayleigh-Taylor instability

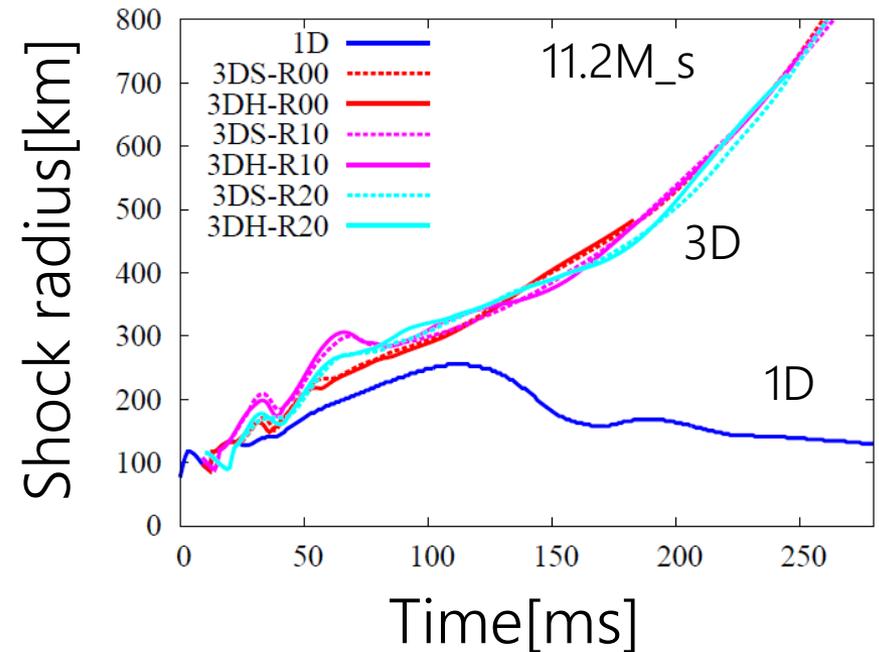
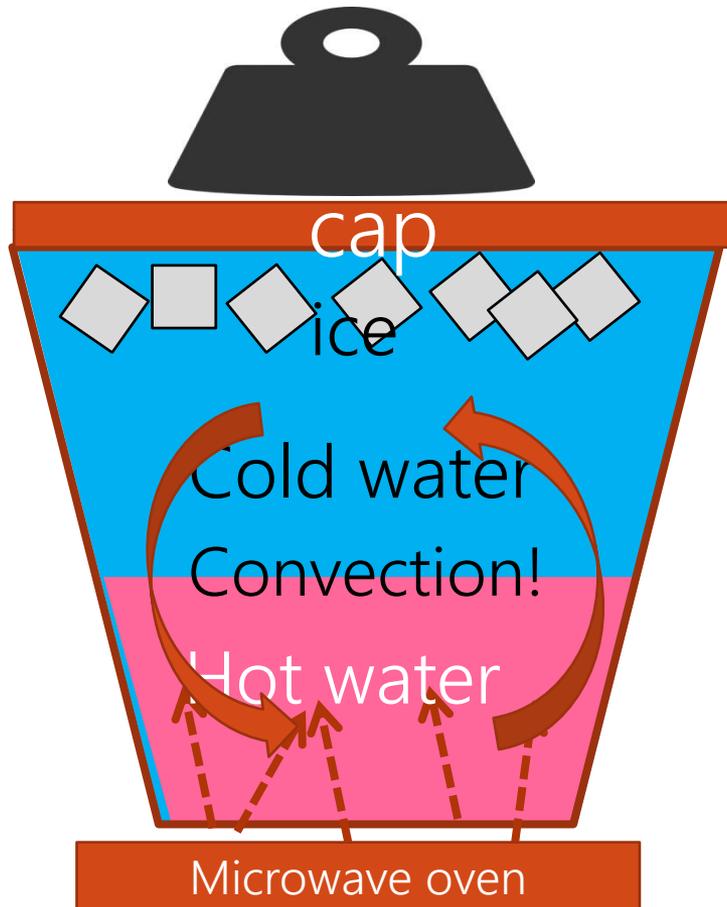
(Cold heavy matter is put over Hot light matter)

Rayleigh-Taylor convection transfer energy outward.



Hotter than the initial state

Successful 3D simulation



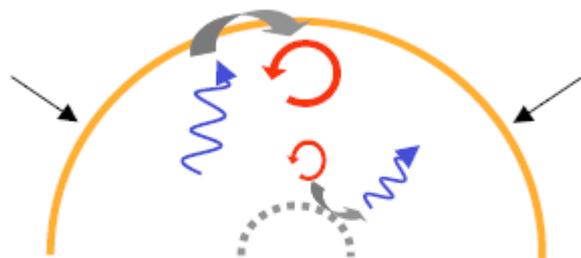
2 month times 16,000 cores are used in K computer

With convection hot water at the bottom is transported near the cap. The pressure at the cap become higher. Explosion occurs with the process.

S A S I

(Standing Accretion Shock Instability)

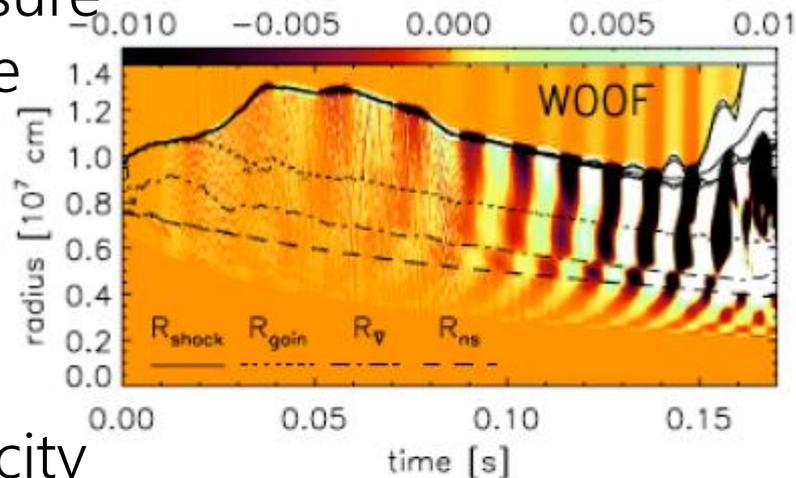
Scheck+ 2008



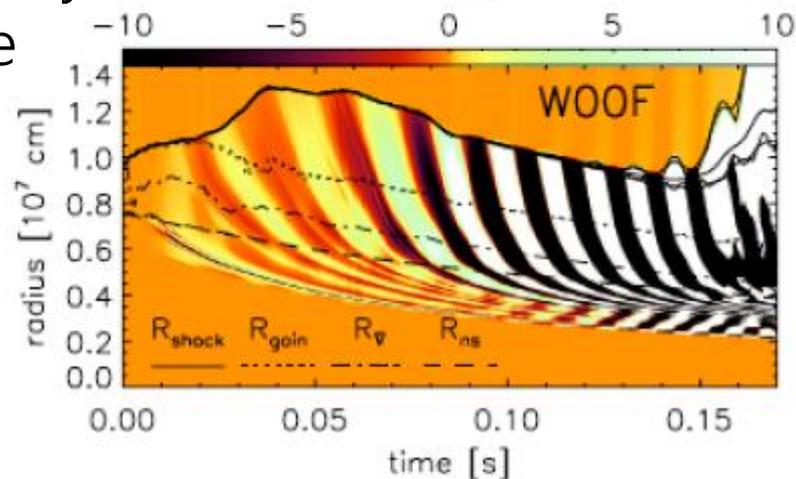
Advective-acoustic
cycle

From Foglizzo's slides
Standing Accretion Shock Instability(SASI)

Pressure
Wave



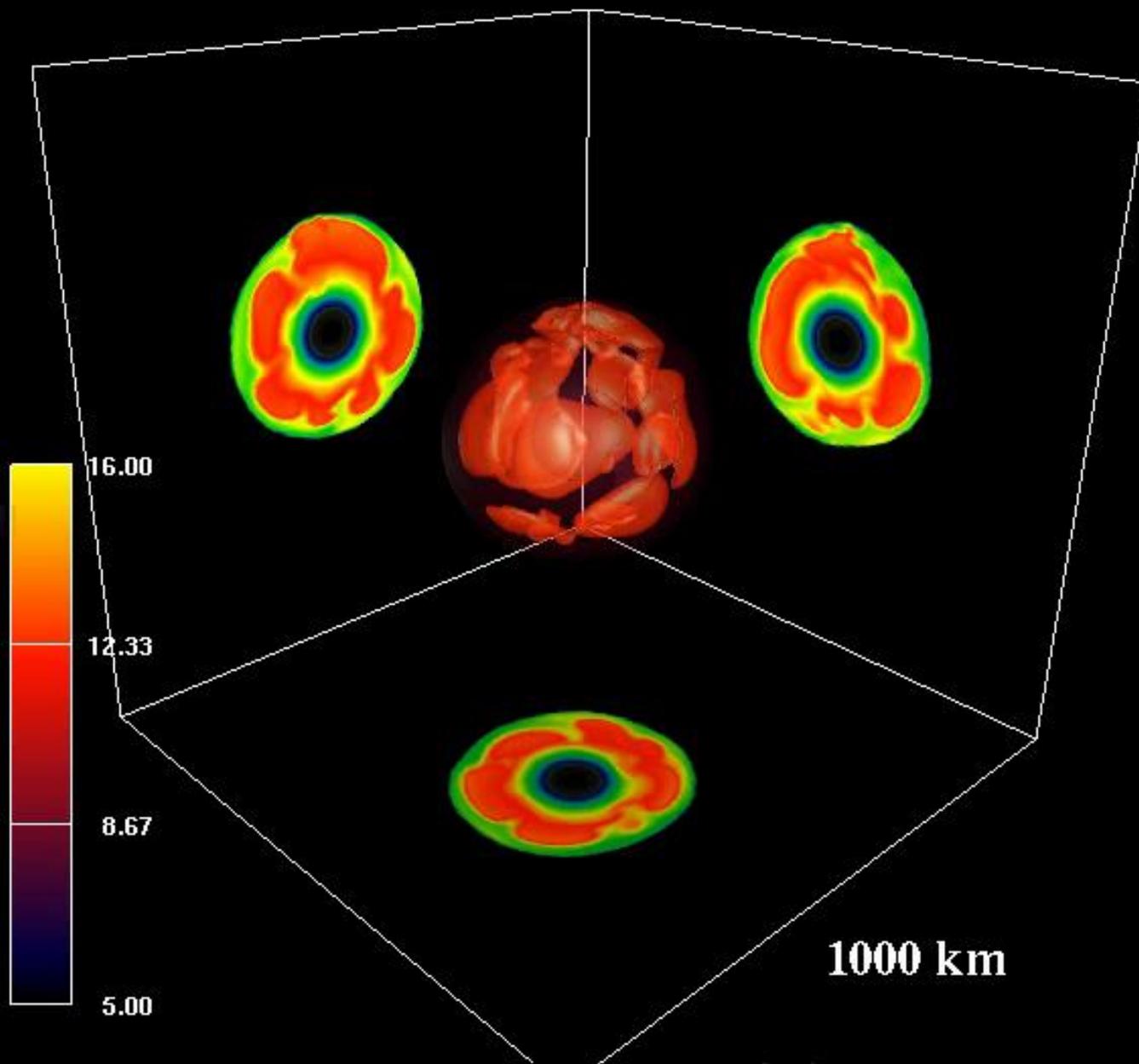
Vorticity
Wave



Entropy

27.0M_s R0.0

t= 0150 ms



Recent Problem of CC SNe

Results in multi-D models significantly depend on input physics and numerical methods!

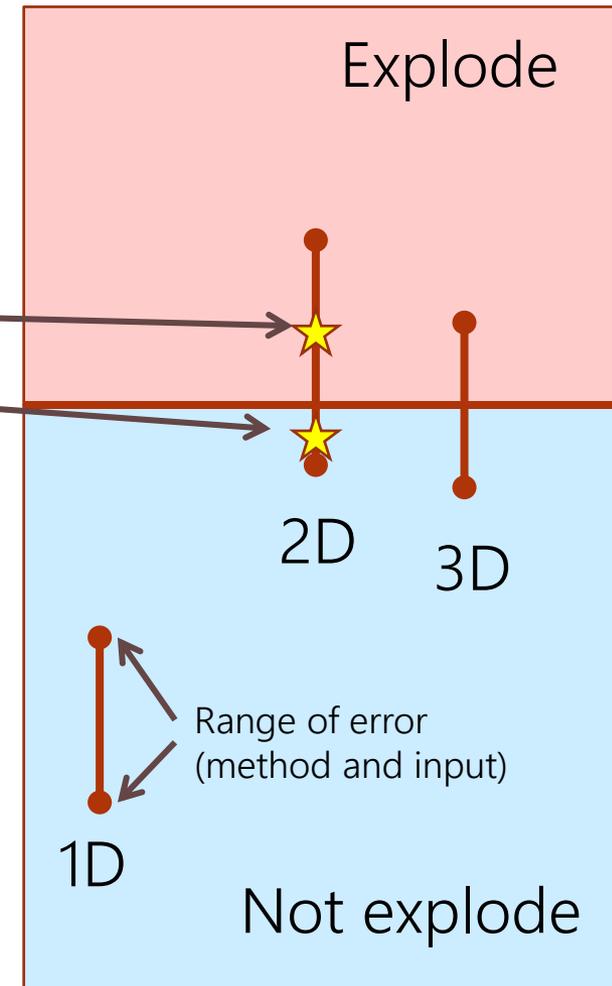
2D models for multiple progenitors

- Bruenn+12: all explode
- **Mueller+13: almost all explode**
- Dolence+14: not explode
- Nakamura+14: all explode
- Suwa +14: half of them explode
- Hanke's setup: almost all explode

3D models for multiple progenitors

- Hanke et al+13: not explode(3model)
Melason+15 , Mueller+15: explode
- Takiwaki in prep: half of them explode
- Bruenn: a explosion model

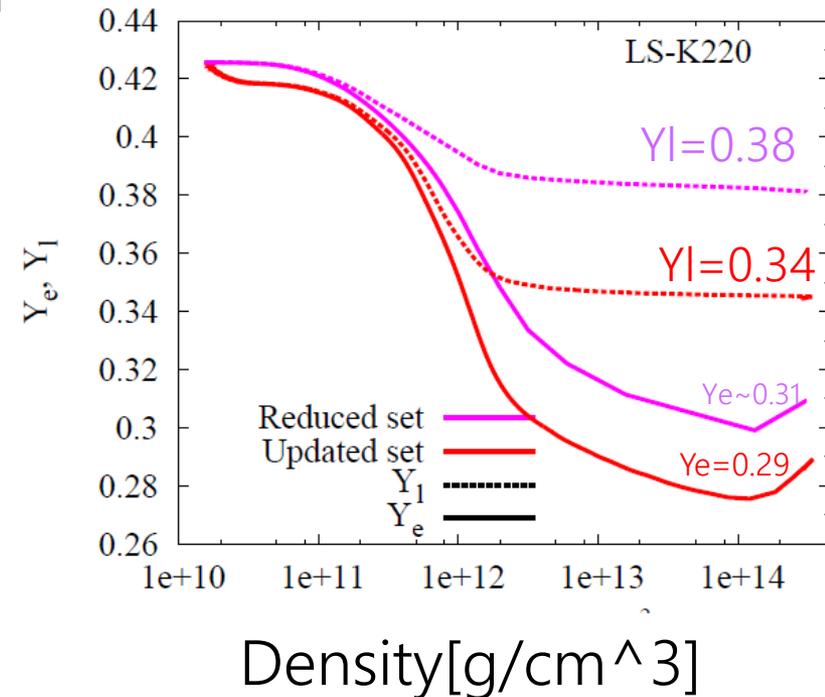
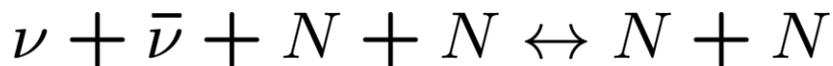
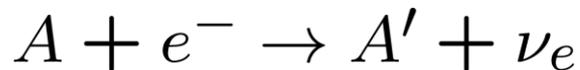
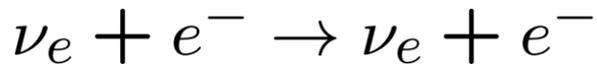
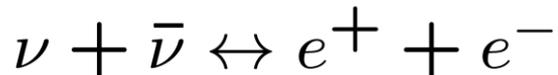
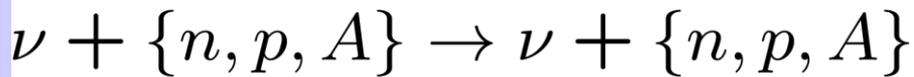
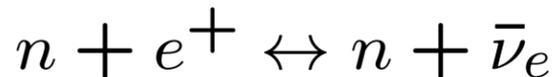
We have to update the input physics.



Plan

- Recent status of SN simulations
- Our efforts for making sophisticated model
- How EOS affects the explosion
- Systematic studies(in progress)

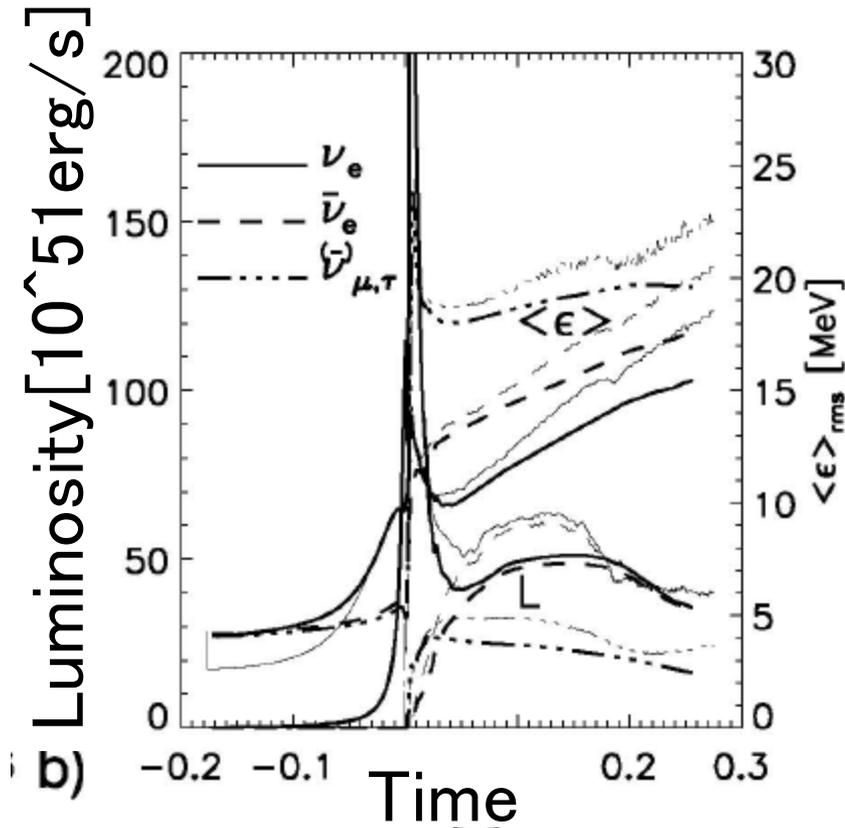
Towards further sophistications



There are still several minor points that are remaining to be updated.

Updated set is roughly consistent with the more sophisticated works(e.g. Mueller+2010).

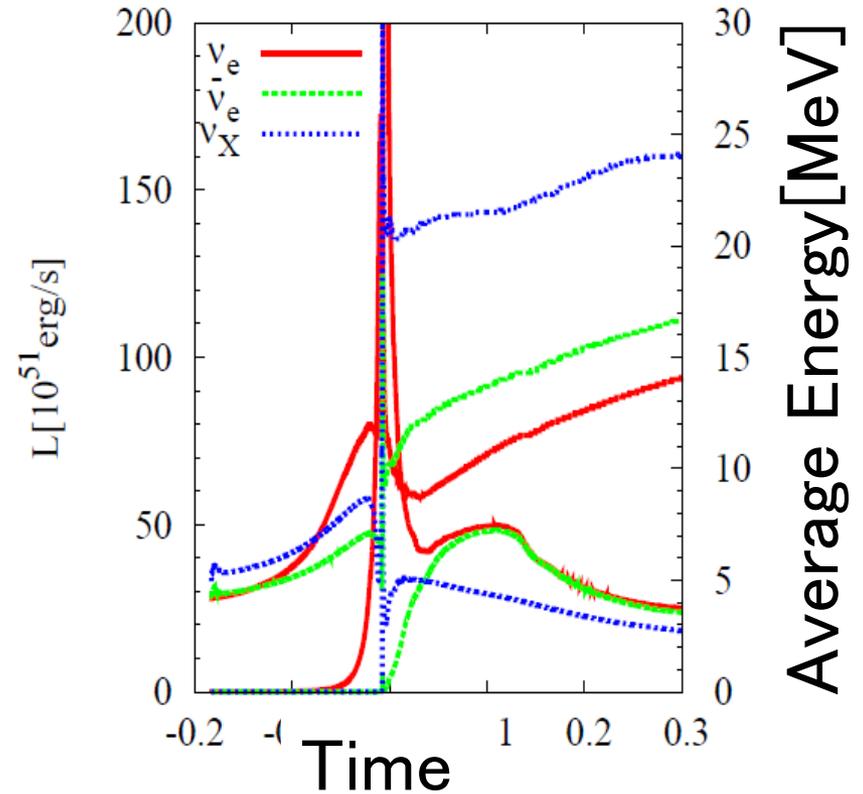
Towards further sophistications



Liebendoerfer et al 2005

Sn and VE

General relativistic simulation



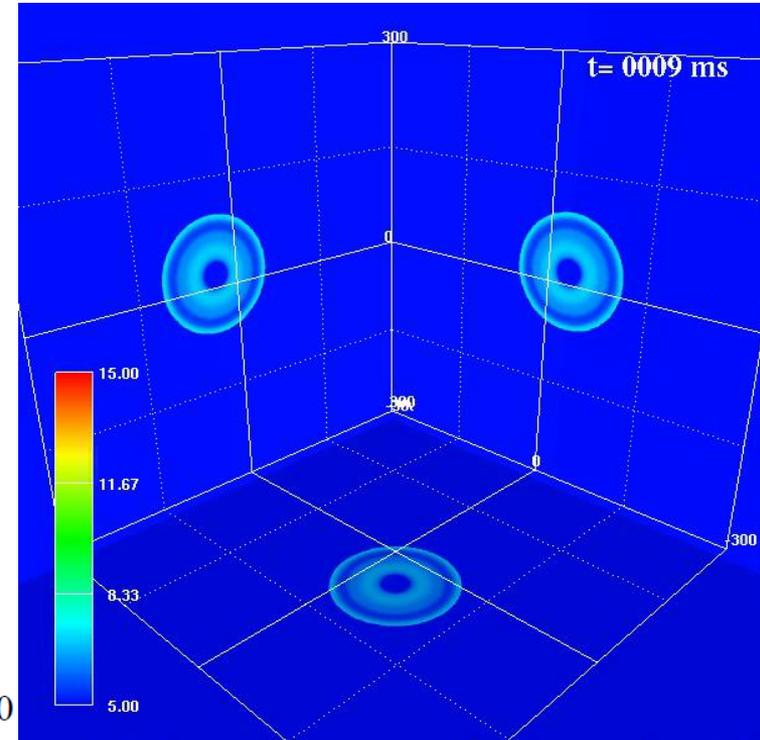
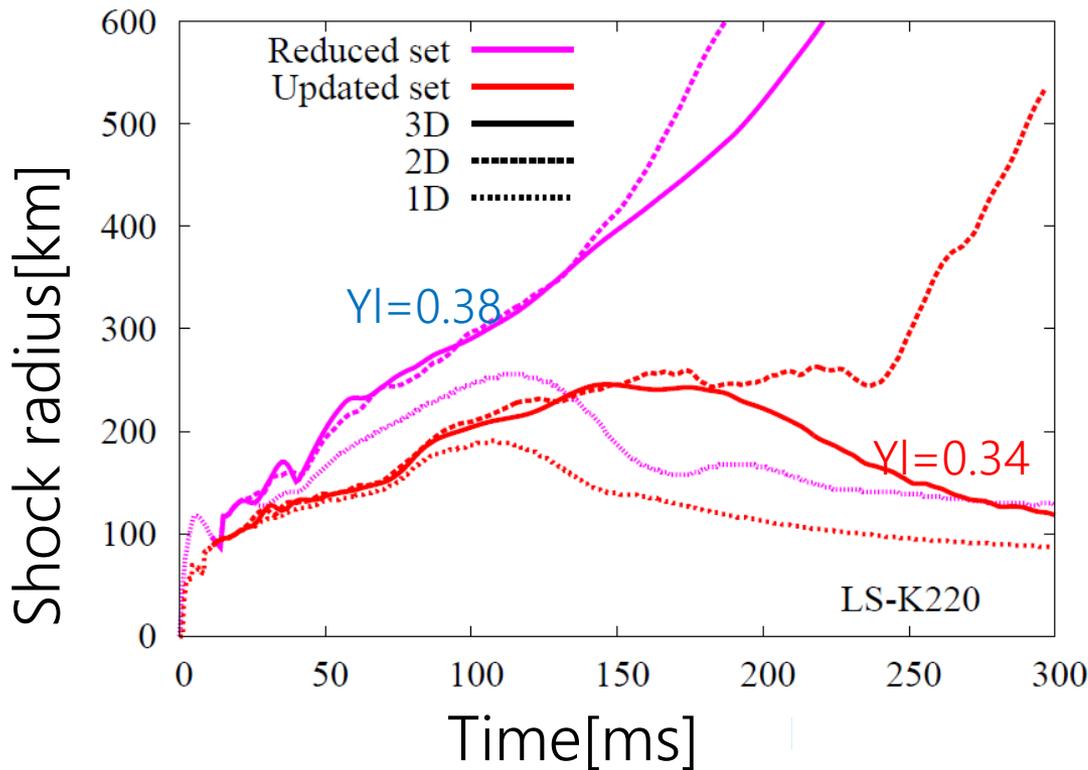
Our newest version of IDSA

ecp,aecp,eca,csc,nsc,pap,nes,nbr

Newtonian Gravity

Our simulation is roughly consistent with the sophisticated 1D model.

Towards further sophistications



Unfortunately our 3D model with updated neutrino reaction does not explode.
But do not forget that we now ignore GR Effect that should help the explosion!

Plan

- Recent status of SN simulations
- Our efforts for making sophisticated model
- How EOS affects the explosion
- Systematic studies on EOS (in progress)

Important ingredients for core-collapse supernovae

We have to update all input physics and numerics.

- Dimensionality
- General Relativity
- Neutrino reactions
- Equation of state
- Progenitor Structure

Stiffness of EOS

THE ASTROPHYSICAL JOURNAL, 335:301–305, 1988 December 1

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SUPERNOVA EXPLOSIONS AND THE SOFT EQUATION OF STATE

MARIKO TAKAHARA

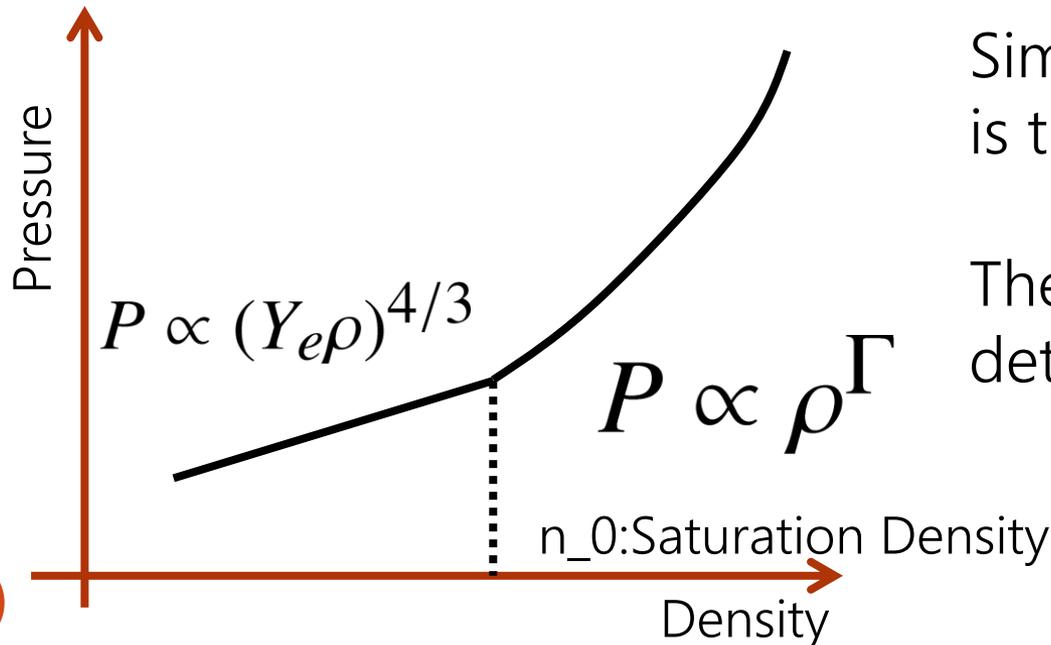
Department of Astronomy, Faculty of Science, University of Tokyo

AND

KATSUHIKO SATO

Department of Physics, Faculty of Science, University of Tokyo

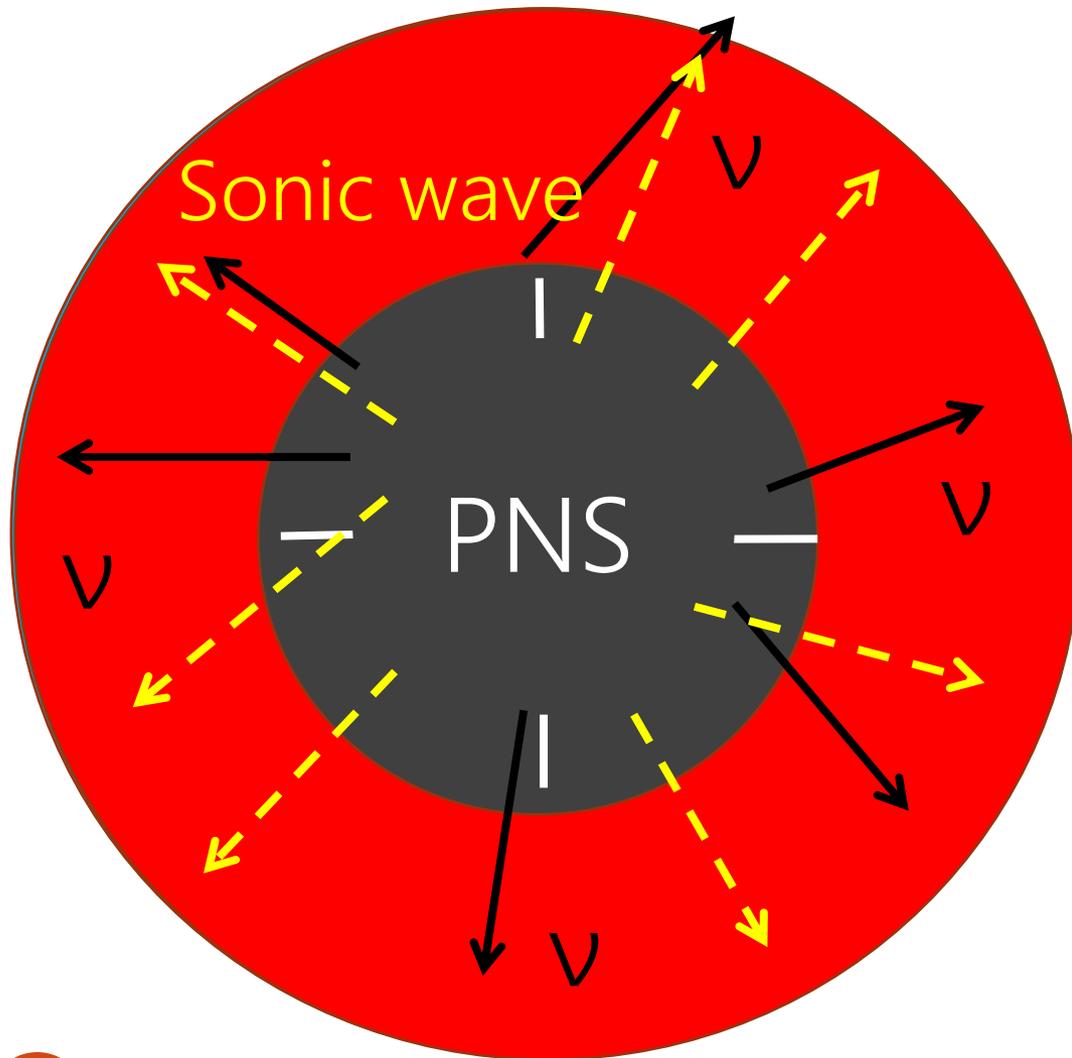
Received 1987 May 29; accepted 1988 May 28



Simply speaking, stiffness is the value of Γ .

The evolution of PNS is determined by that.

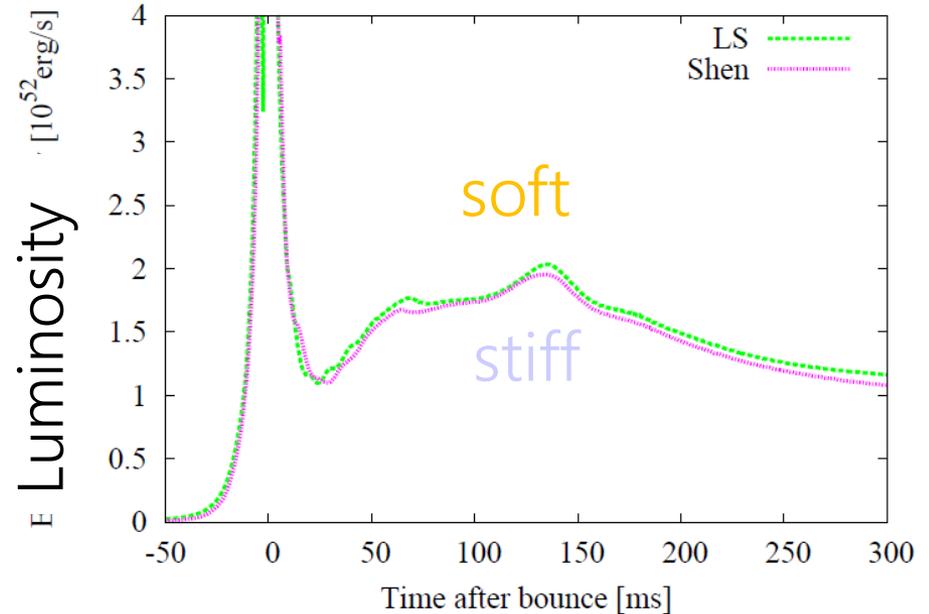
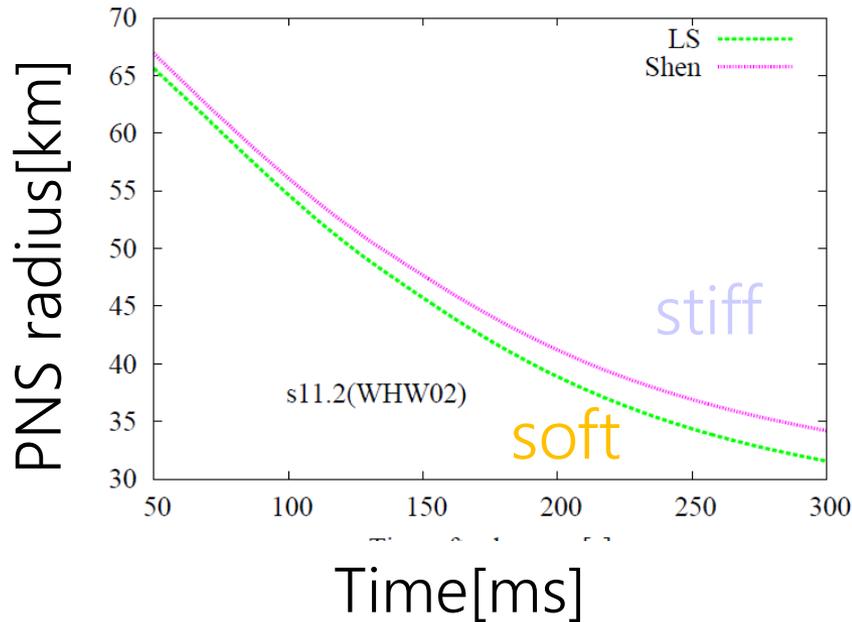
Basic idea to connect EOS and Explosion



1. The PNS gradually shrinks by the gravity.
2. E_{grav} is released.
3. E_{thermal} is increased.
4. The L_{ν} and sonic waves are emitted from the surface of PNS.

Soft EOS releases large energy and makes the PNS dense, that produce strong acoustic wave.

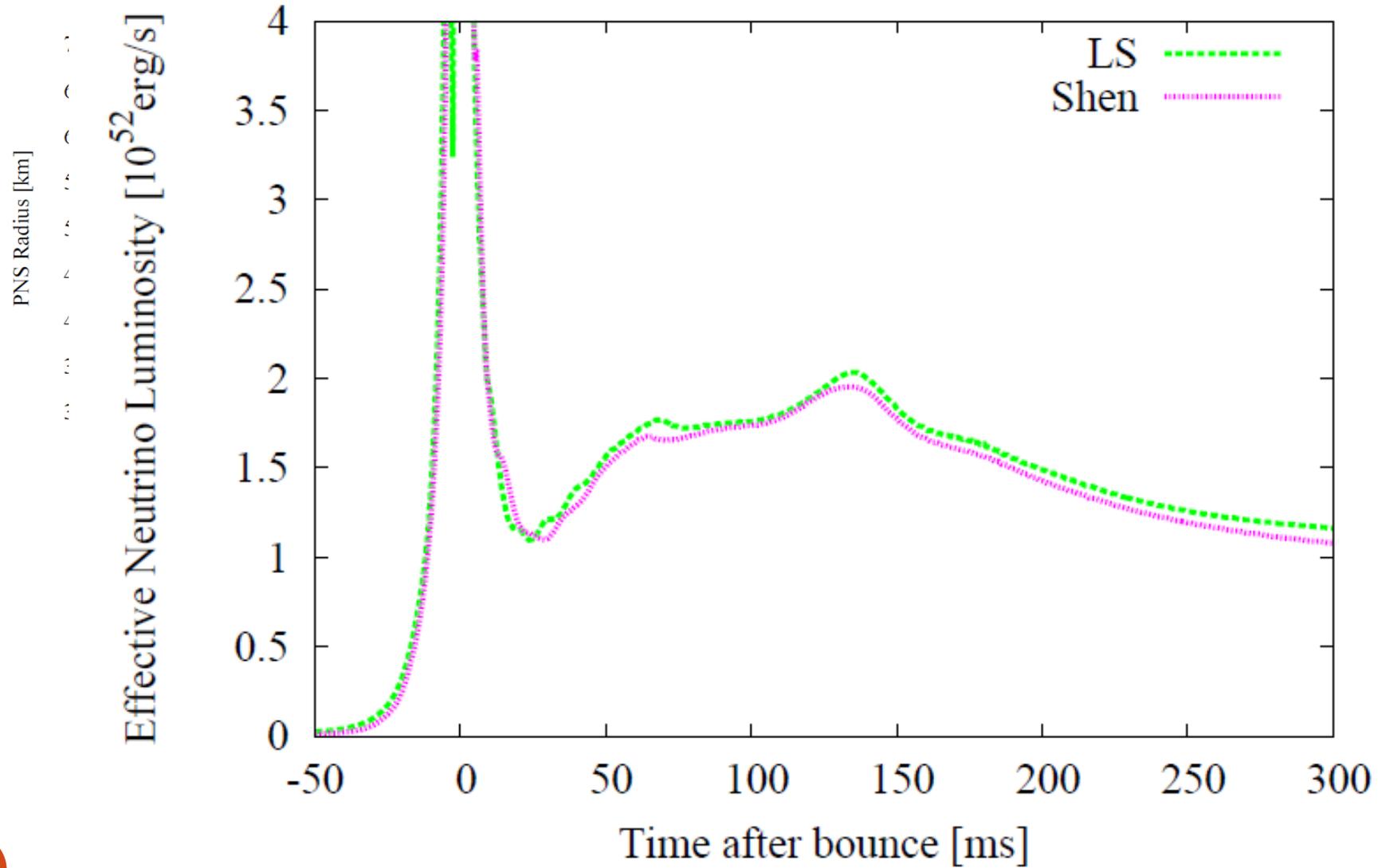
Neutrino Luminosity



LS(K220): Soft EOS \Rightarrow rapidly shrink \Rightarrow Large L_ν

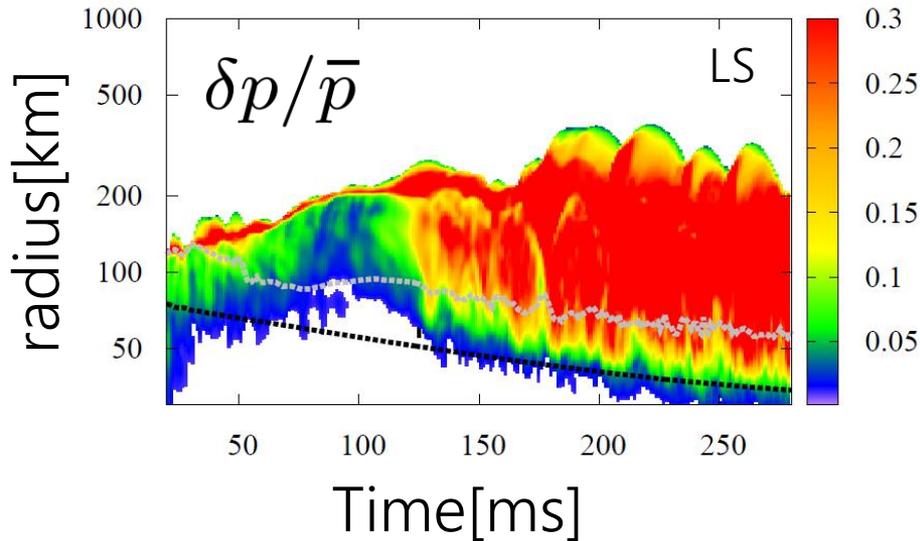
Shen: Stiff EOS \Rightarrow slowly shrink \Rightarrow small L_ν

Neutrino Luminosity

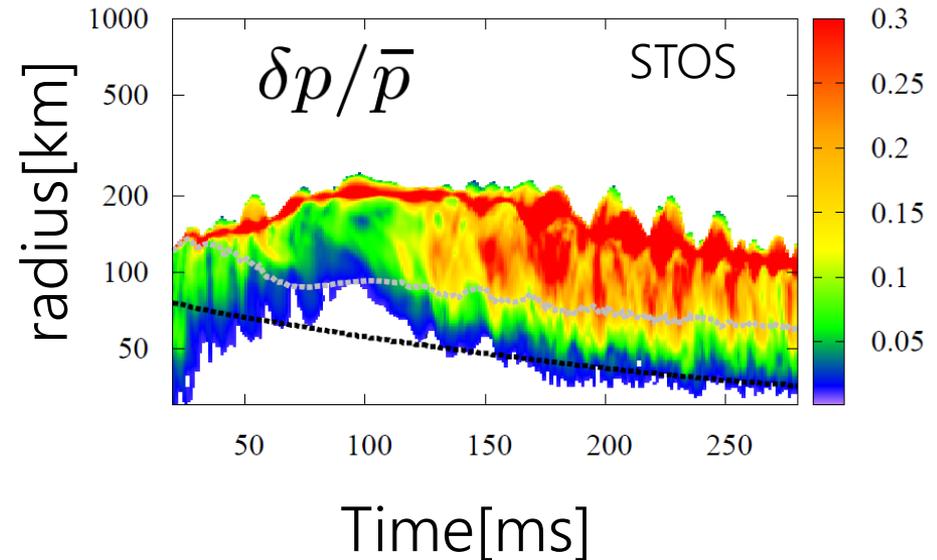


Sonic Wave

s11.2(WHW02)-LS



s11.2(WHW02)-STOS

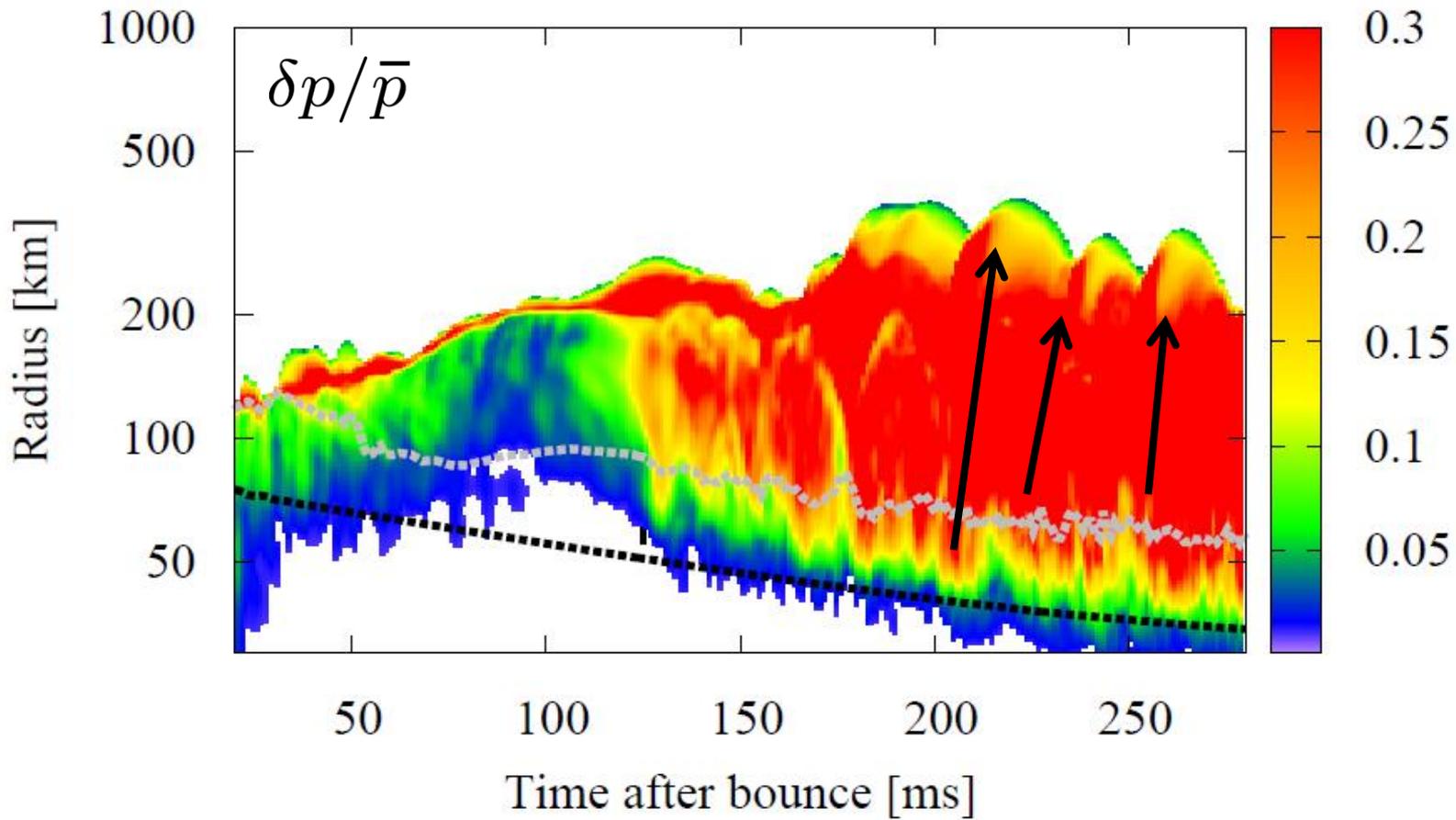


Gray: gain radius, black PNS radius

Strong sonic wave is reflected at the PNS!
(It is a little bit hard to see, but) softer EOS
make stronger sonic wave.

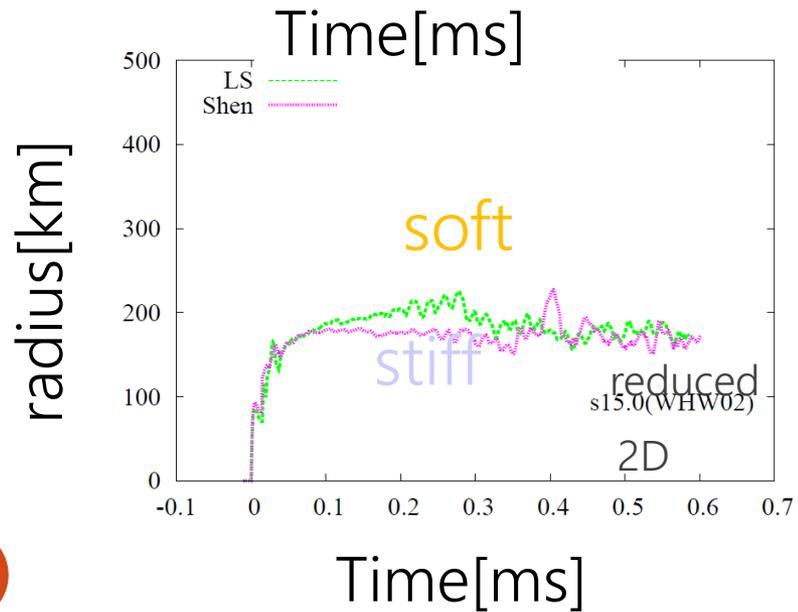
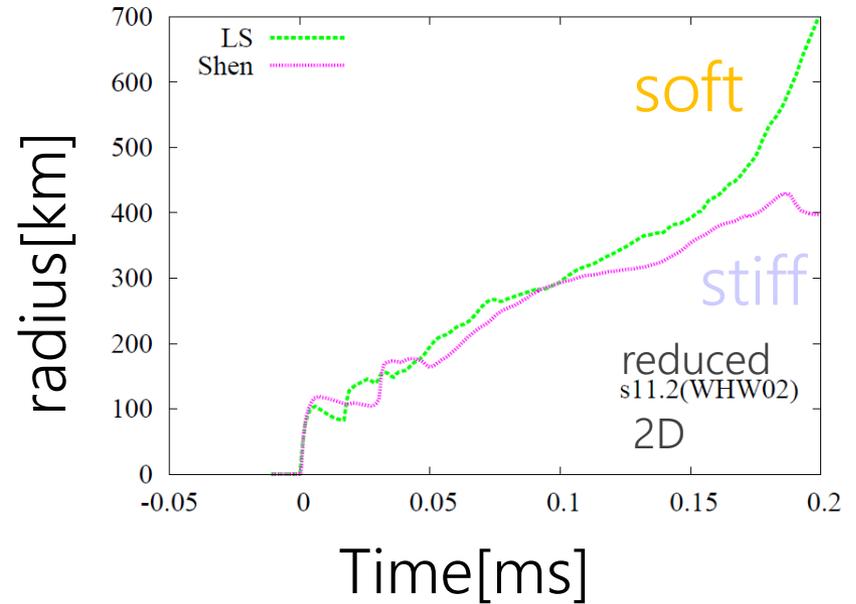
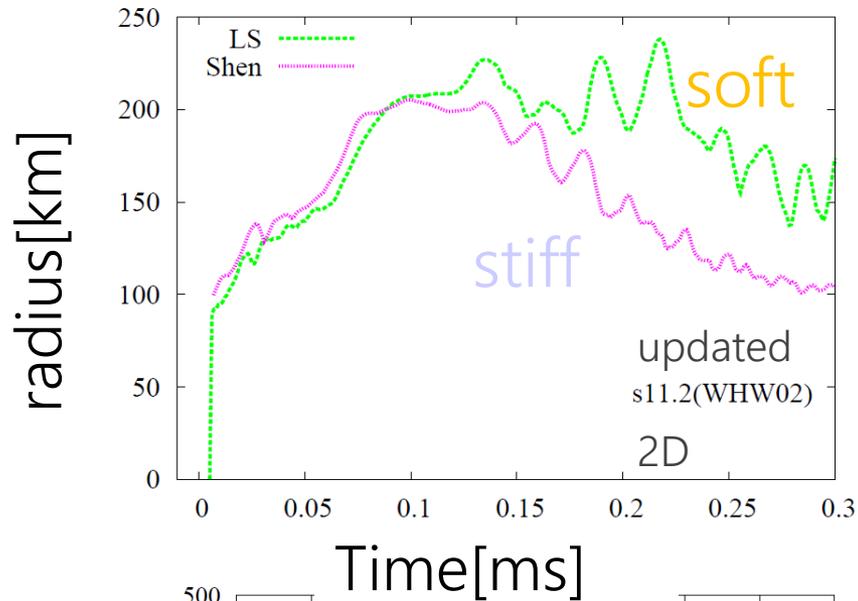
Sonic Wave

s11.2(WHW02)-LS



Gray: gain radius, black PNS radius

Evolution of the shock

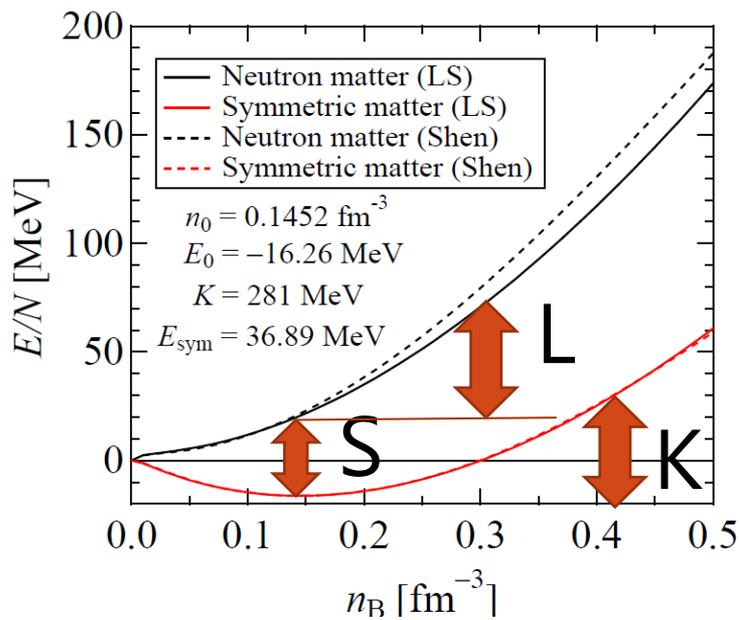


Softer EOS shows larger shock radius.

Plan

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Many theories for EOS

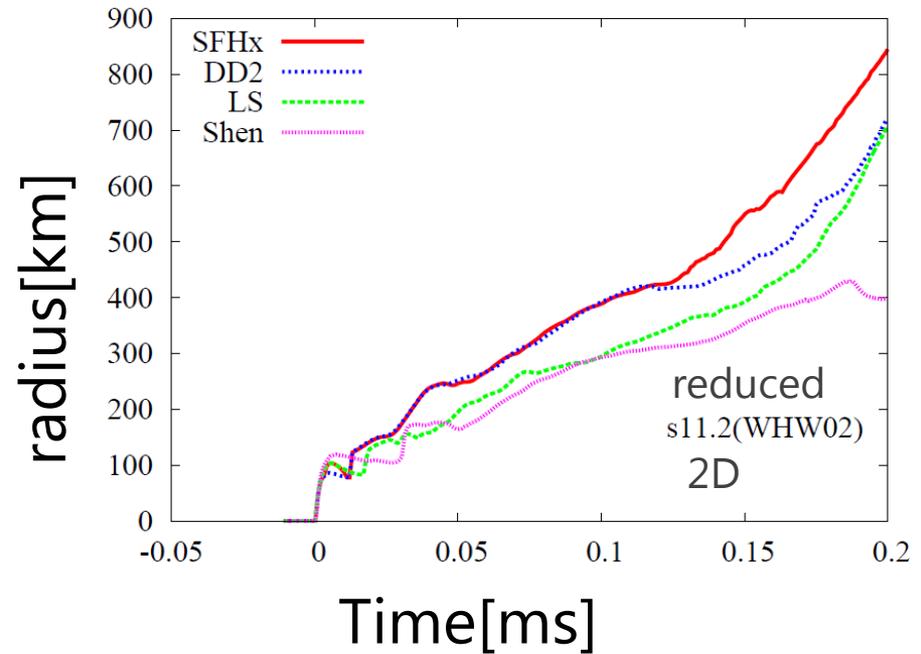
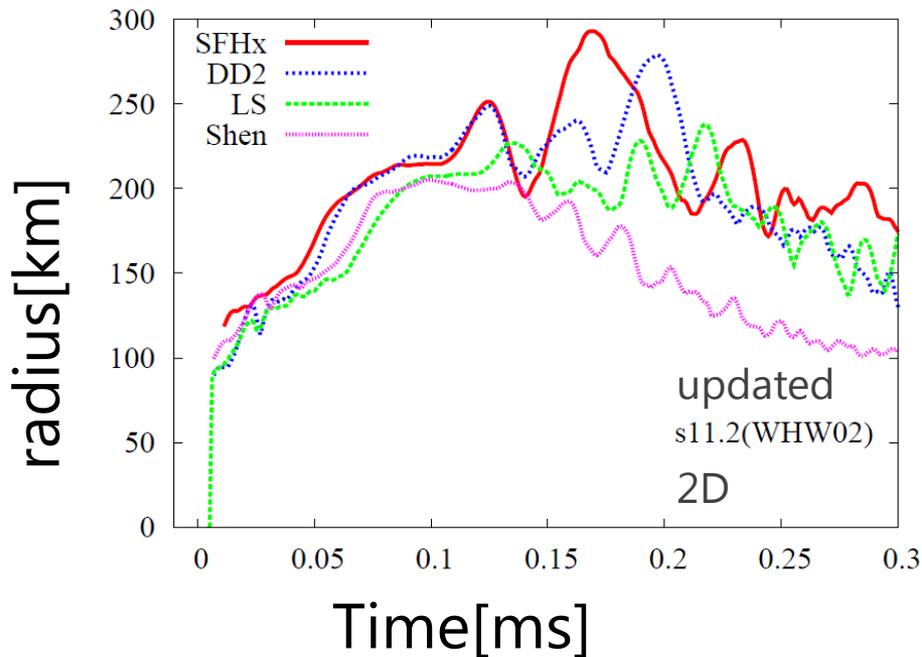


$$p = n^2 \frac{\partial (E/N)}{\partial n}$$

Fisher+2014

| EOS | n_0 [fm^{-3}] | E_0 [MeV] | K [MeV] | S [MeV] | L [MeV] | $R_{1.4}$ [km] | M_{max} [M_{\odot}] |
|-------------|-------------------------------|----------------|--------------------|---------------------------|---------------------------|---------------------------|-------------------------------------|
| SFHo | 0.1583 | 16.19 | 245 | 31.57 | 47.10 | 11.89 | 2.06 |
| SFHx | 0.1602 | 16.16 | 238 | 28.67 | 23.18 | 11.99 | 2.13 |
| HS(TM1) | 0.1455 | 16.31 | 281 | 36.95 | 110.99 | 14.47 | 2.21 |
| HS(TMA) | 0.1472 | 16.03 | 318 | 30.66 | 90.14 | 13.85 | 2.02 |
| HS(FSUgold) | 0.1482 | 16.27 | 229 | 32.56 | 60.43 | 12.55 | 1.74 |
| HS(DD2) | 0.1491 | 16.02 | 243 | 31.67 | 55.04 | 13.22 | 2.42 |
| HS(IUFSU) | 0.1546 | 16.39 | 231 | 31.29 | 47.20 | 12.68 | 1.95 |
| HS(NL3) | 0.1482 | 16.24 | 272 | 37.39 | 118.49 | 14.77 | 2.79 |
| STOS(TM1) | 0.1452 | 16.26 | 281 | 36.89 | 110.79 | 14.50 | 2.22 |
| LS (180) | 0.1550 | 16.00 | 180 | 28.61 | 73.82 | 12.16 | 1.84 |
| LS (220) | 0.1550 | 16.00 | 220 | 28.61 | 73.82 | 12.67 | 2.05 |
| Exp. | ~ 0.15 | ~ 16 | $240 \pm 10^{(a)}$ | $29.0\text{--}32.7^{(b)}$ | $40.5\text{--}61.9^{(c)}$ | $10.4\text{--}12.9^{(c)}$ | $\gtrsim 2.0^{(d),(e)}$ |

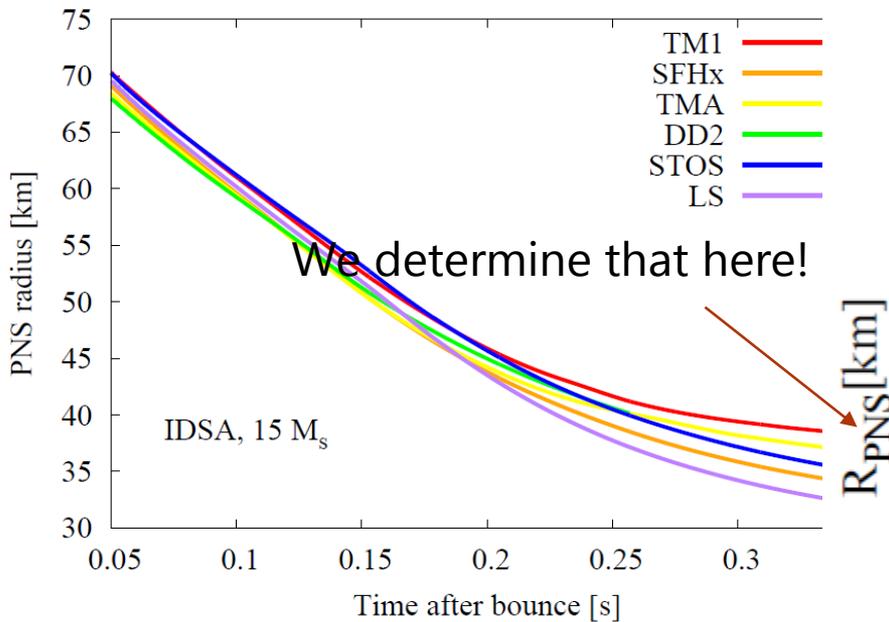
New EOS



Again, softer EOS shows larger shock radius.

SFHx and DD2: Multi species of heavy nuclei is included.
SFHx and DD2 > LS and Shen.

NS radius vs PNS radius

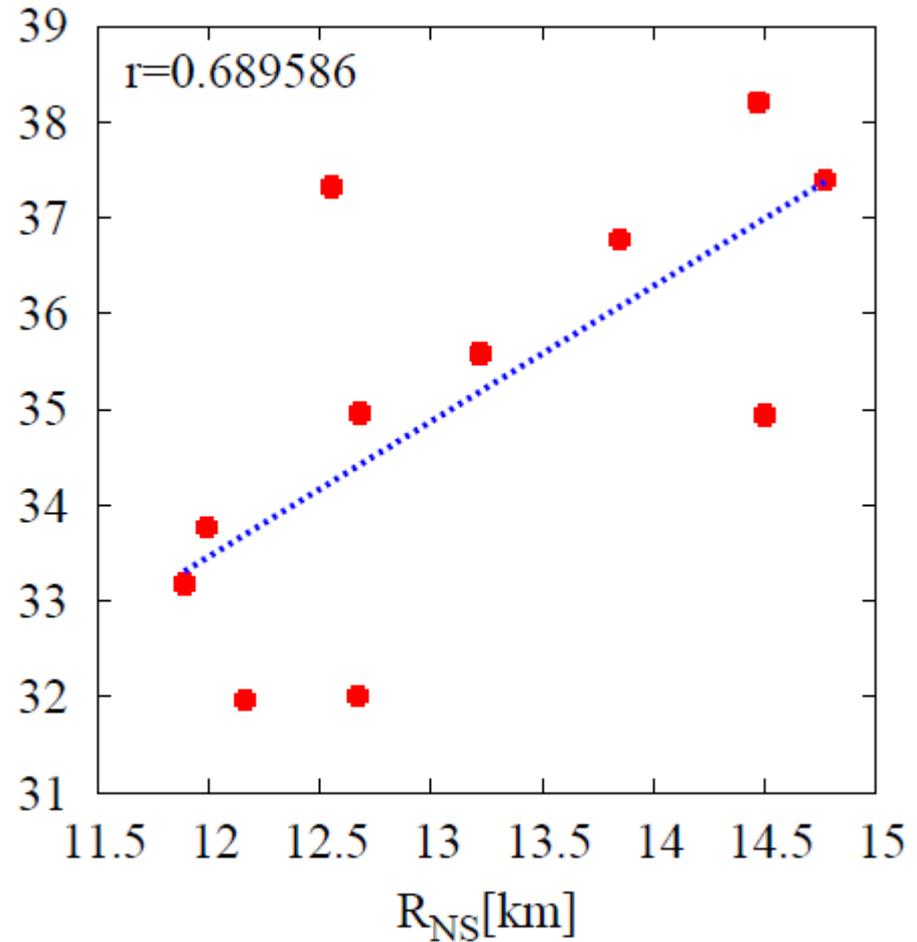


Takiwaki in ρ

PNS radius:

TM1 > TMA ~ DD2 > SFHx

STOS > LS



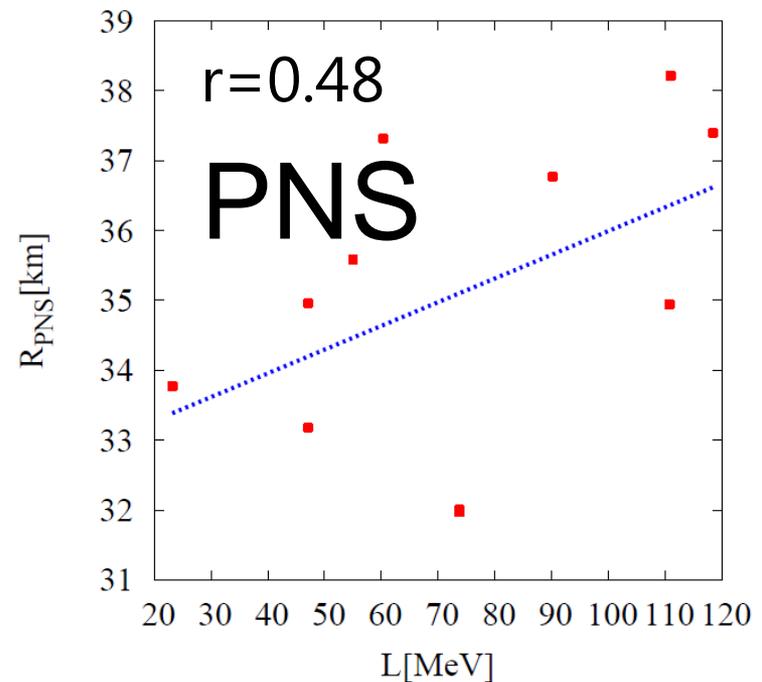
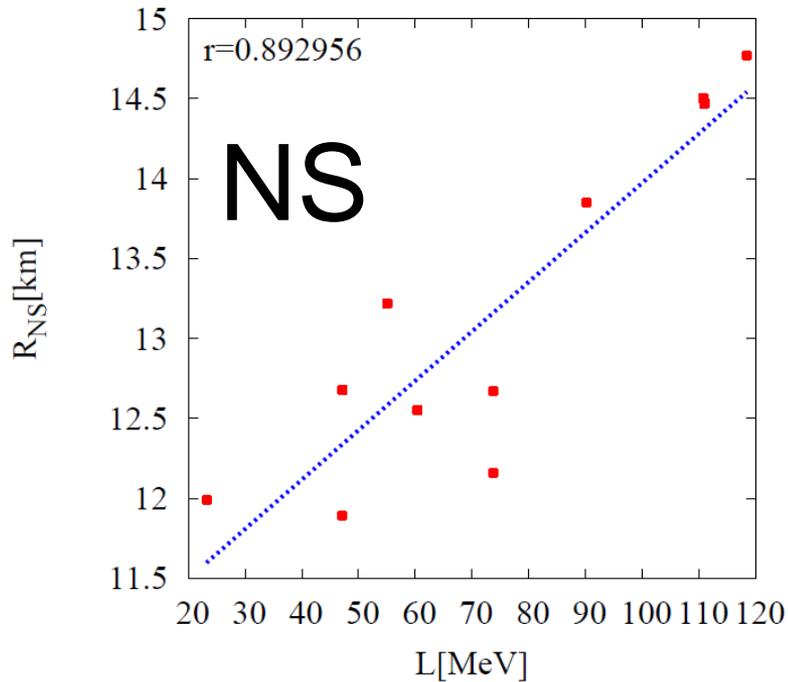
PNS radius is "roughly" predicted by the NS radius at zero-temperature.

Towards more general understanding

In SNe simulations, **the radius of PNS** is focused as the key ingredients for successful explosion.

Can we predict the radius of PNS from the parameters of nuclear physics.

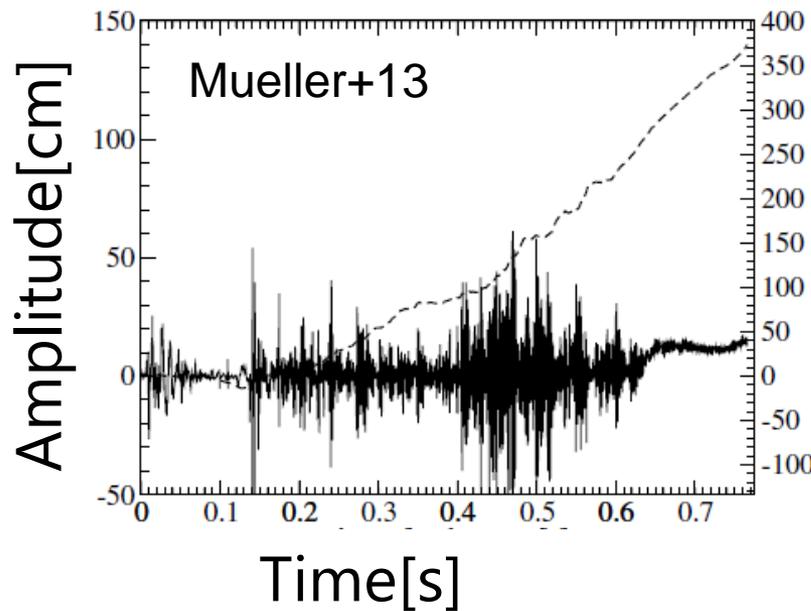
What parameter determine PNS radius



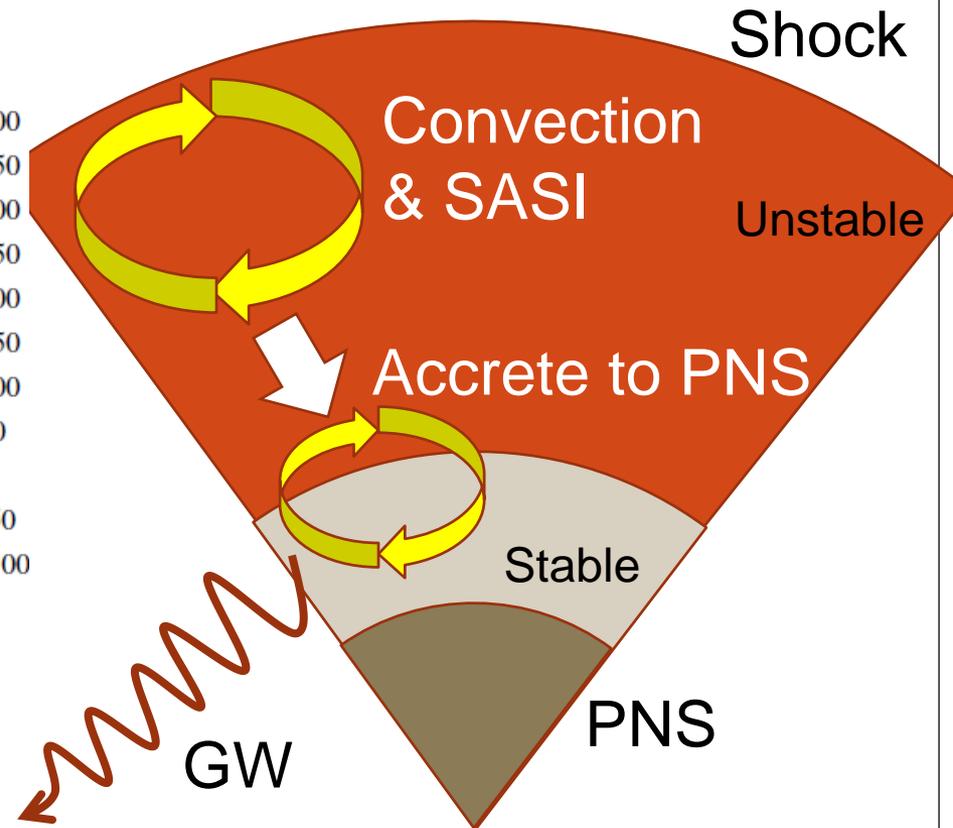
Radius of NS ($T \sim 0$ and $Y_e \sim 0$) is determined by L .
(or $(KL^2)^{1/3}$)
Radius of PNS is not determined by L .
 S and K have stronger correlation to PNS.
 $r=0.71$ for S . $r=0.69$ for K .

Gravitational Wave from Convection & SASI

Activity of convection and SASI is printed in the waveform of GW indirectly.



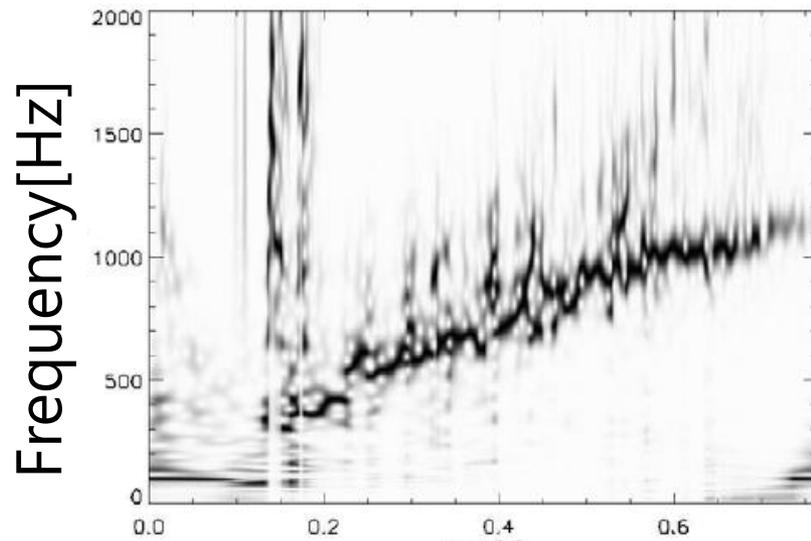
Convection & SASI



Gravitational Wave from Convection

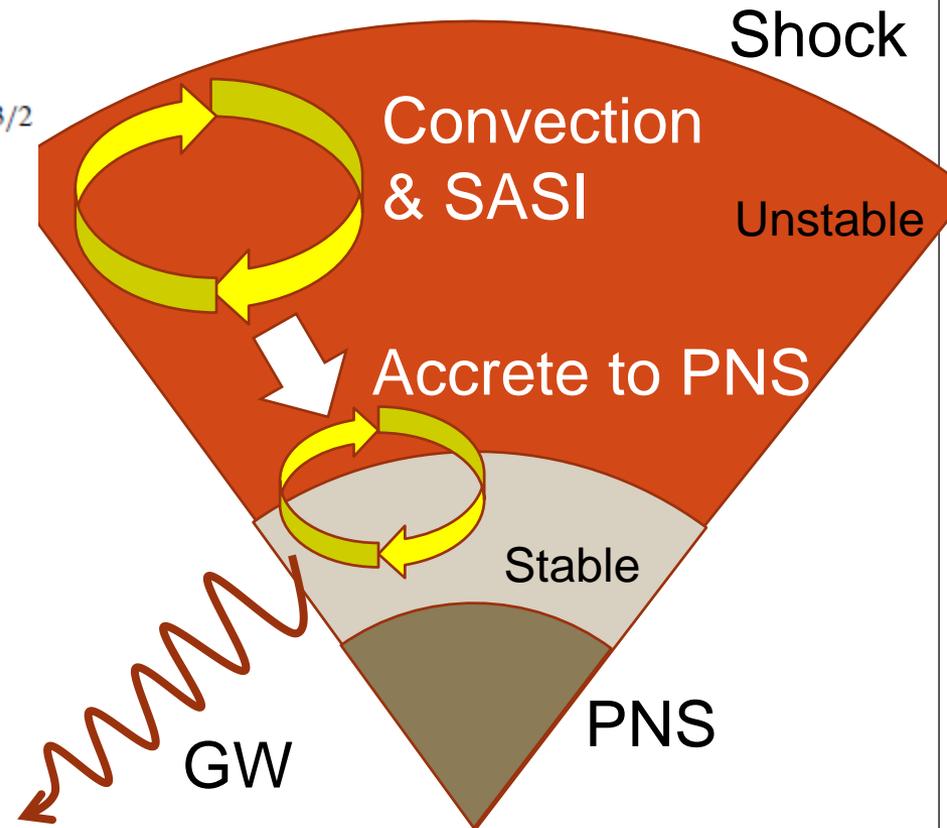
Mass, radius and temperature of PNS determine the typical frequency.

$$f_p = \frac{N}{2\pi} = \frac{1}{2\pi} \frac{GM}{R^2} \sqrt{\frac{(\Gamma - 1)m_n}{\Gamma k_b T}} \left(1 - \frac{GM}{Rc^2}\right)^{3/2}$$



Mueller+13

Time[s]

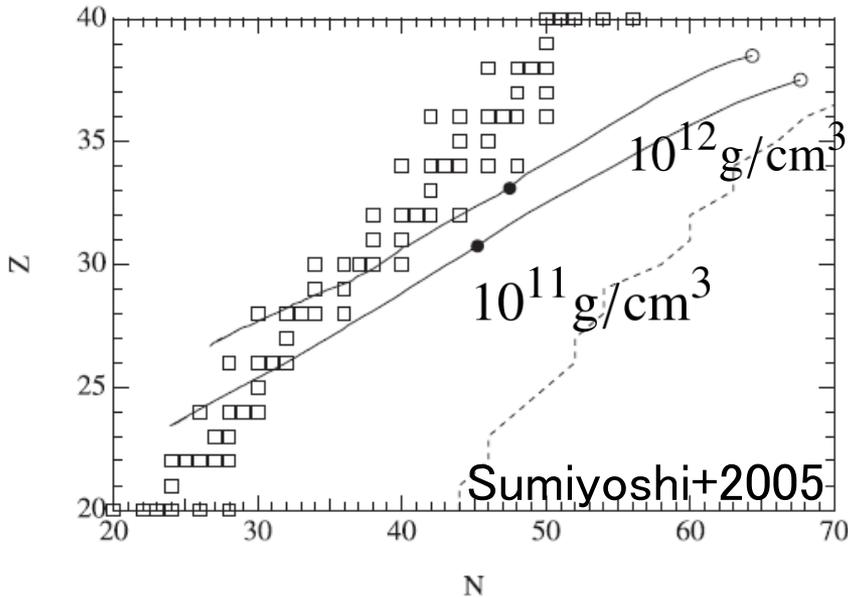


The results of my 3D calculation is coming soon.

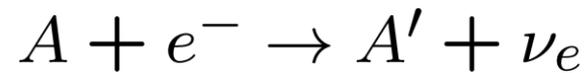
Summary

- Multi-D simulations that naturally employ convection. Those are promising, but the results are sensitive to the input physics.
- Neutrino reaction rates significantly affects the fate of the star if that changes the **lepton fraction of PNS**.
- Equation of State is also important ingredients. If that is sufficiently soft, the **PNS rapidly shrinks** and help explosion via the emission of ν -Luminosity and reflection of sonic wave.
- Radius of PNS are roughly correlated with S and K. The result is not fully interpreted and should be fully investigated urgently.

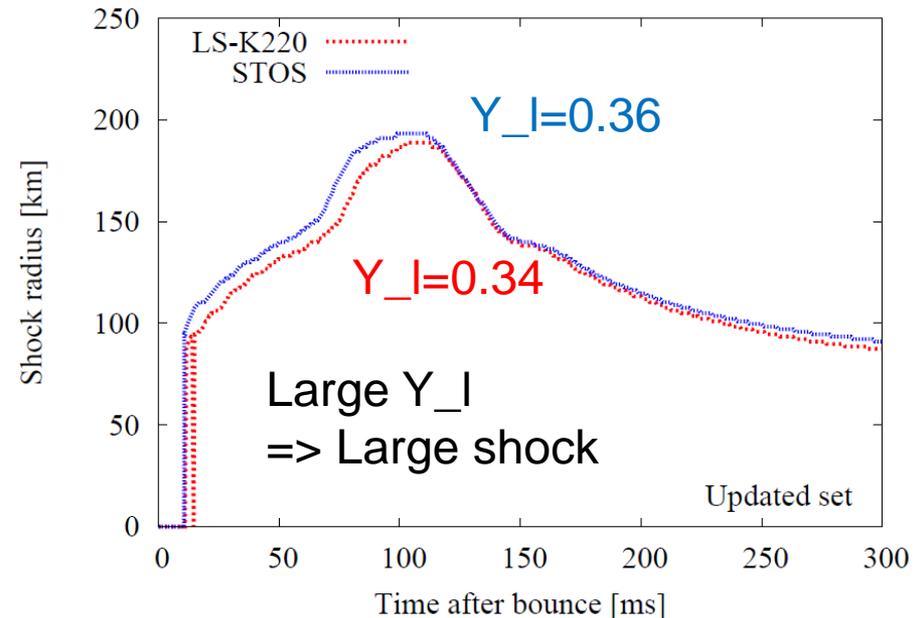
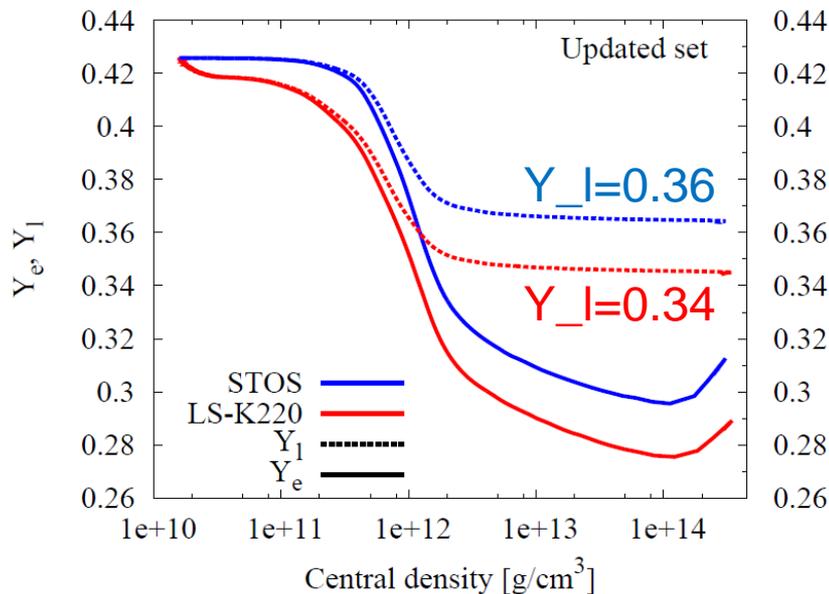
EOS dependence on Y_I



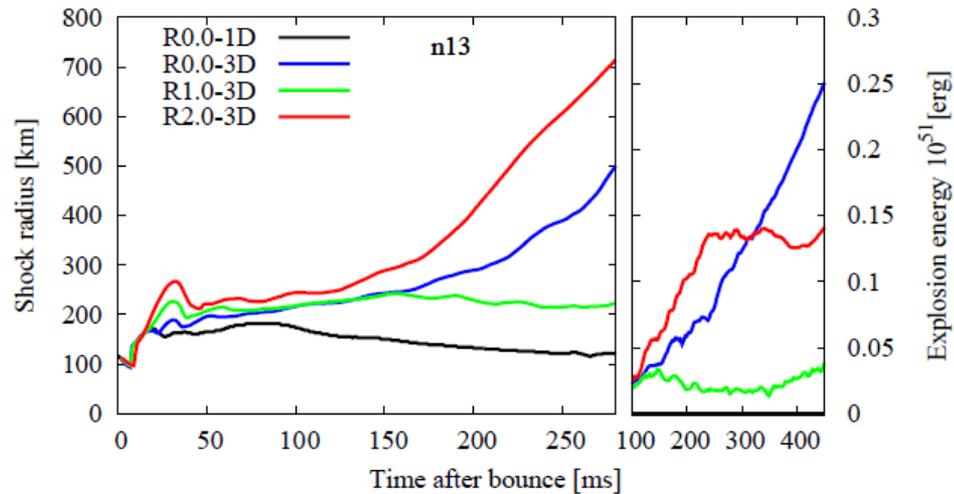
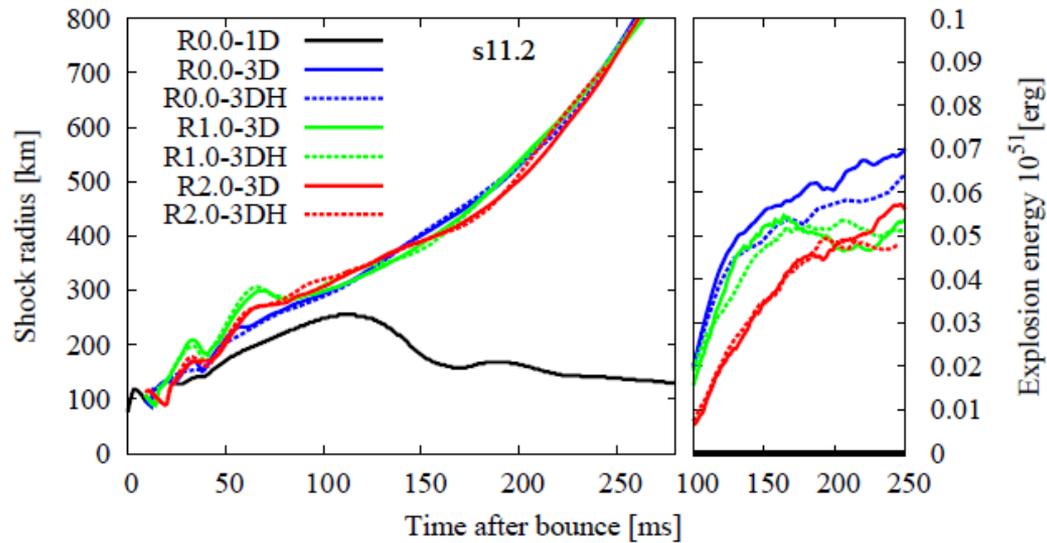
EOS changes the species of heavy nuclei.



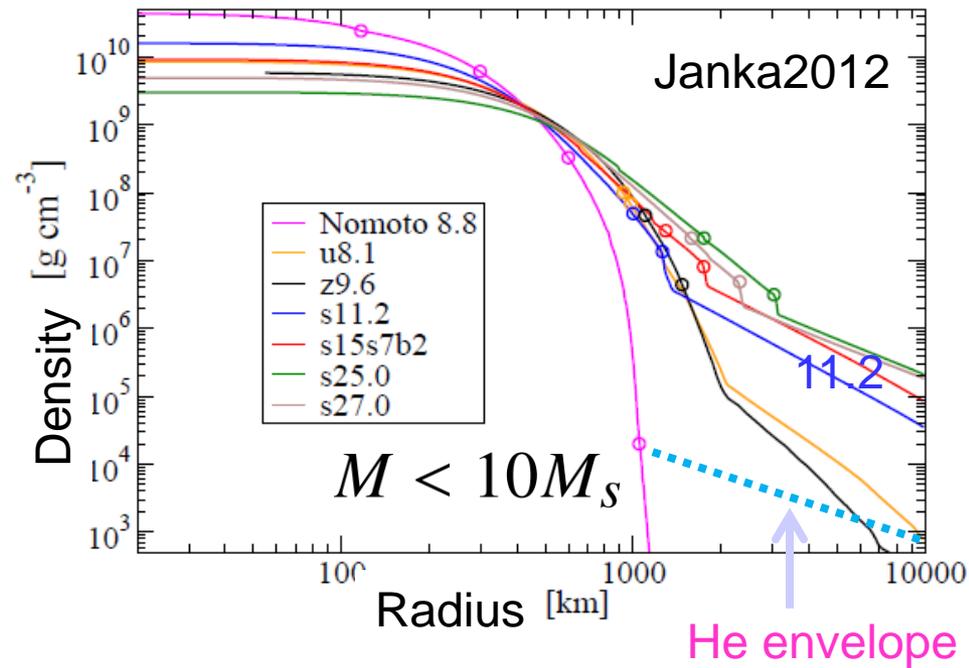
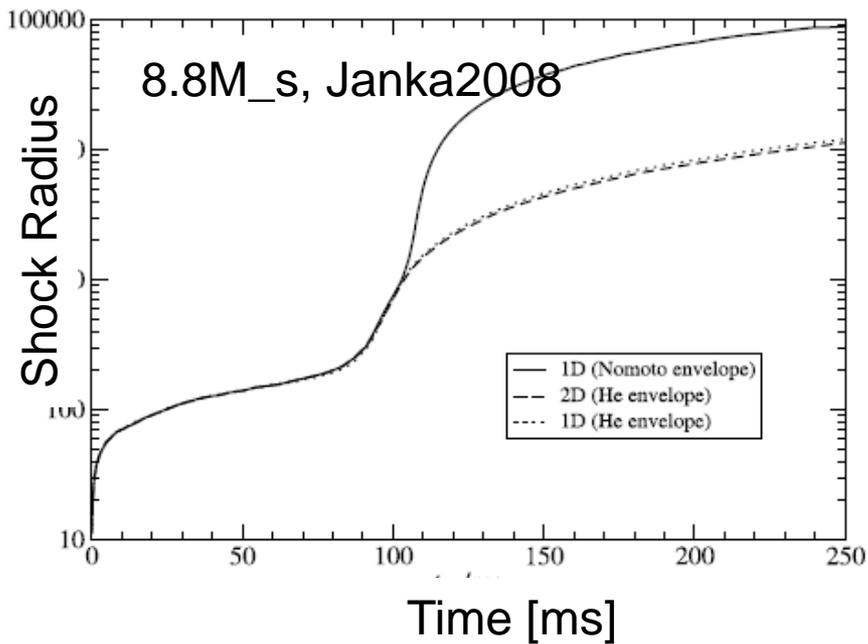
Electron capture rate significantly depends on the species of the nuclei.



Averaged shock radius and Exp. Energy

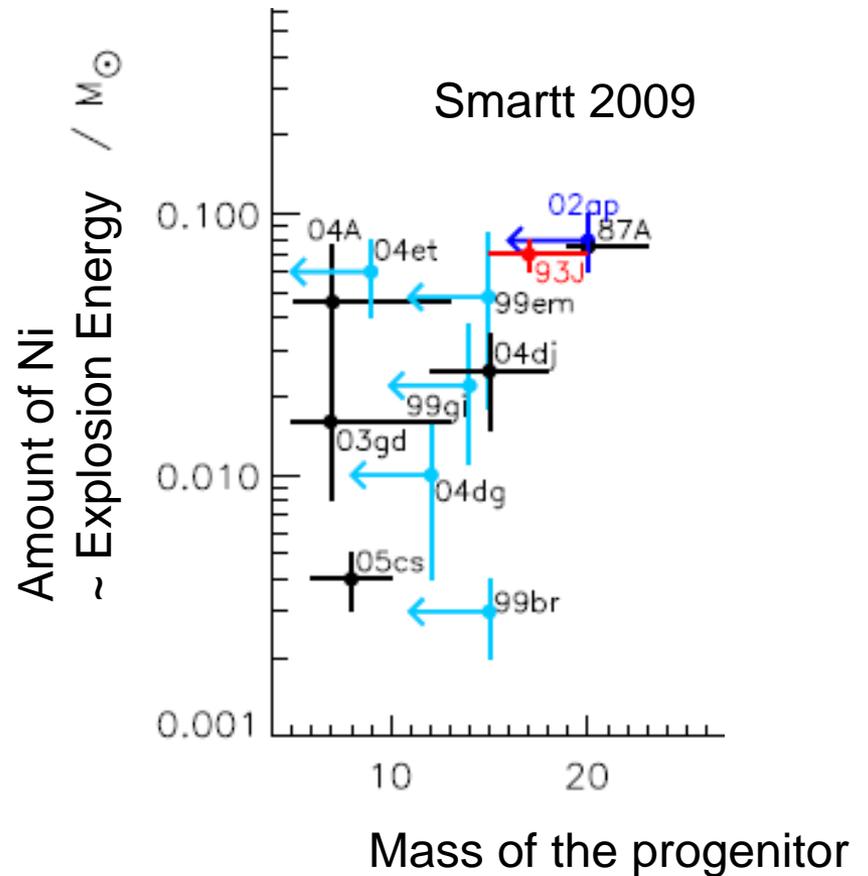
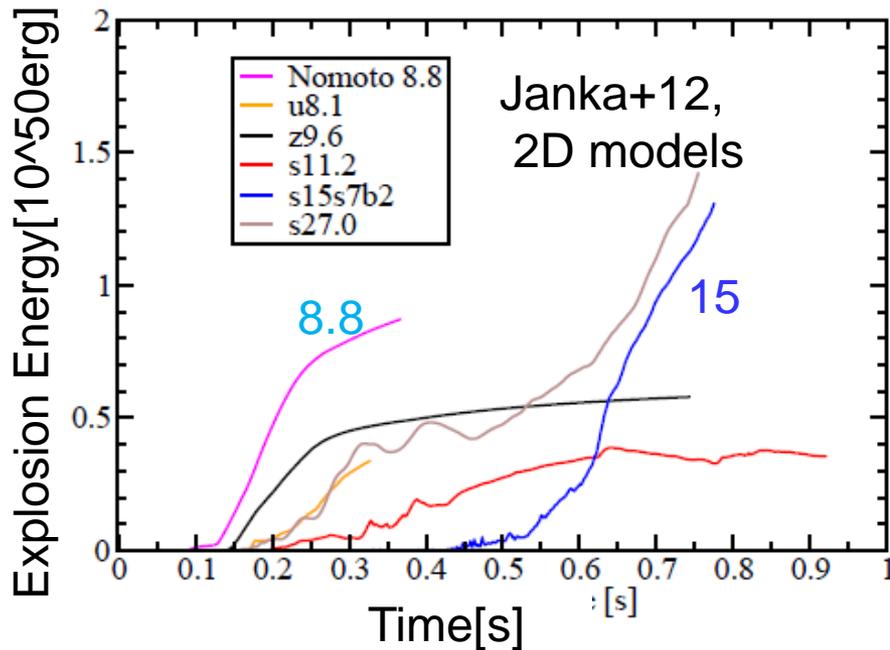


Pure ν heating



Easy shock revival
Dilute outer layer

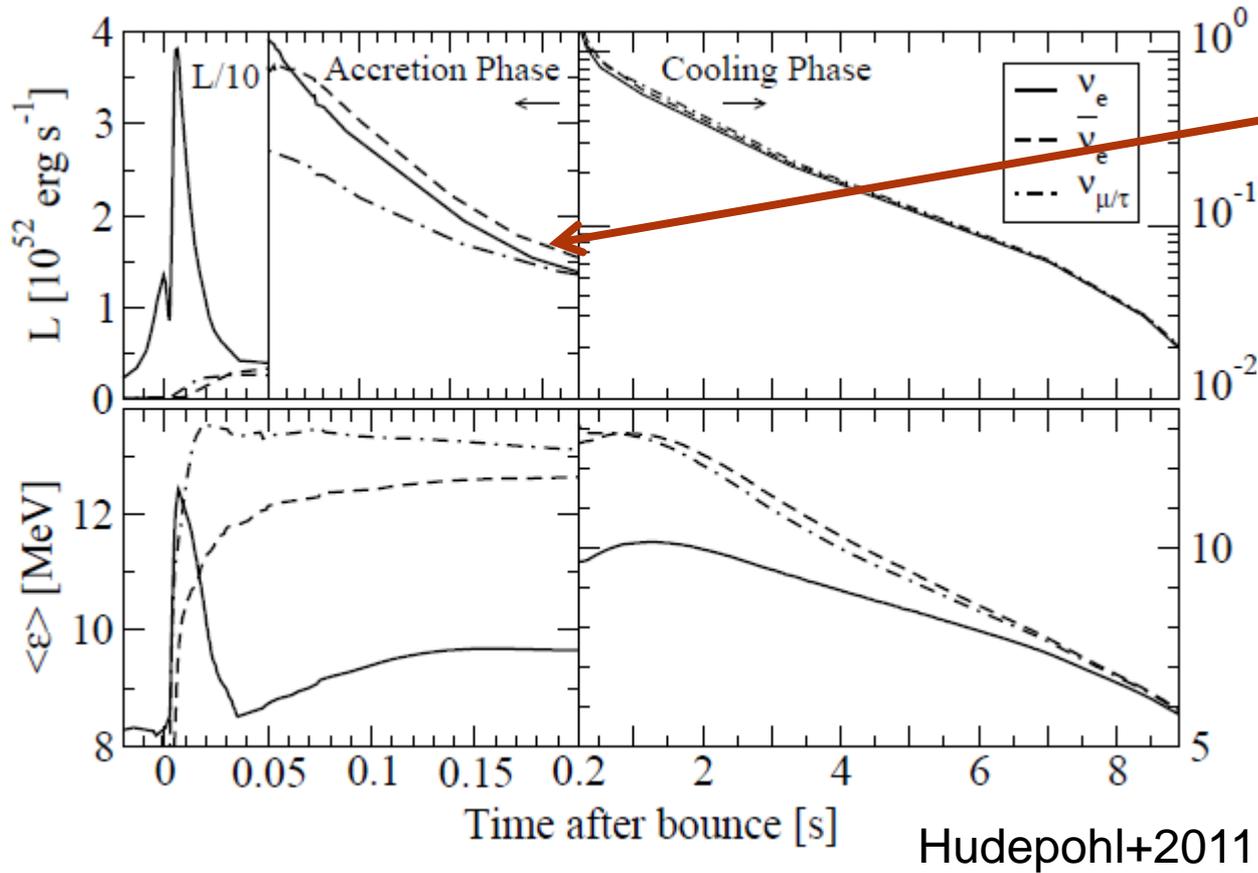
Pure ν heating



軽い親星の爆発は、爆発エネルギーが典型的に $\sim 10^{50}$ erg で普通の超新星の1/10程度。

観測のトレンドとは合っている(ような?)

Pure ν heating(1 D でも爆発)



200ms
 このモデルだと
 $1.5 \times 10^{52} \text{erg/s}$
 $15M_{\odot}$ だと
 $5 \times 10^{52} \text{erg/s}$

バウンス時は他と似たようなものだが、accretion phase以降で ν 光度が低い。後期まで ν のライトカーブをとることで、他と区別可能だと思われる。