

# Pre-main sequence evolution of low-mass stars: Effects of planet formation on stellar composition

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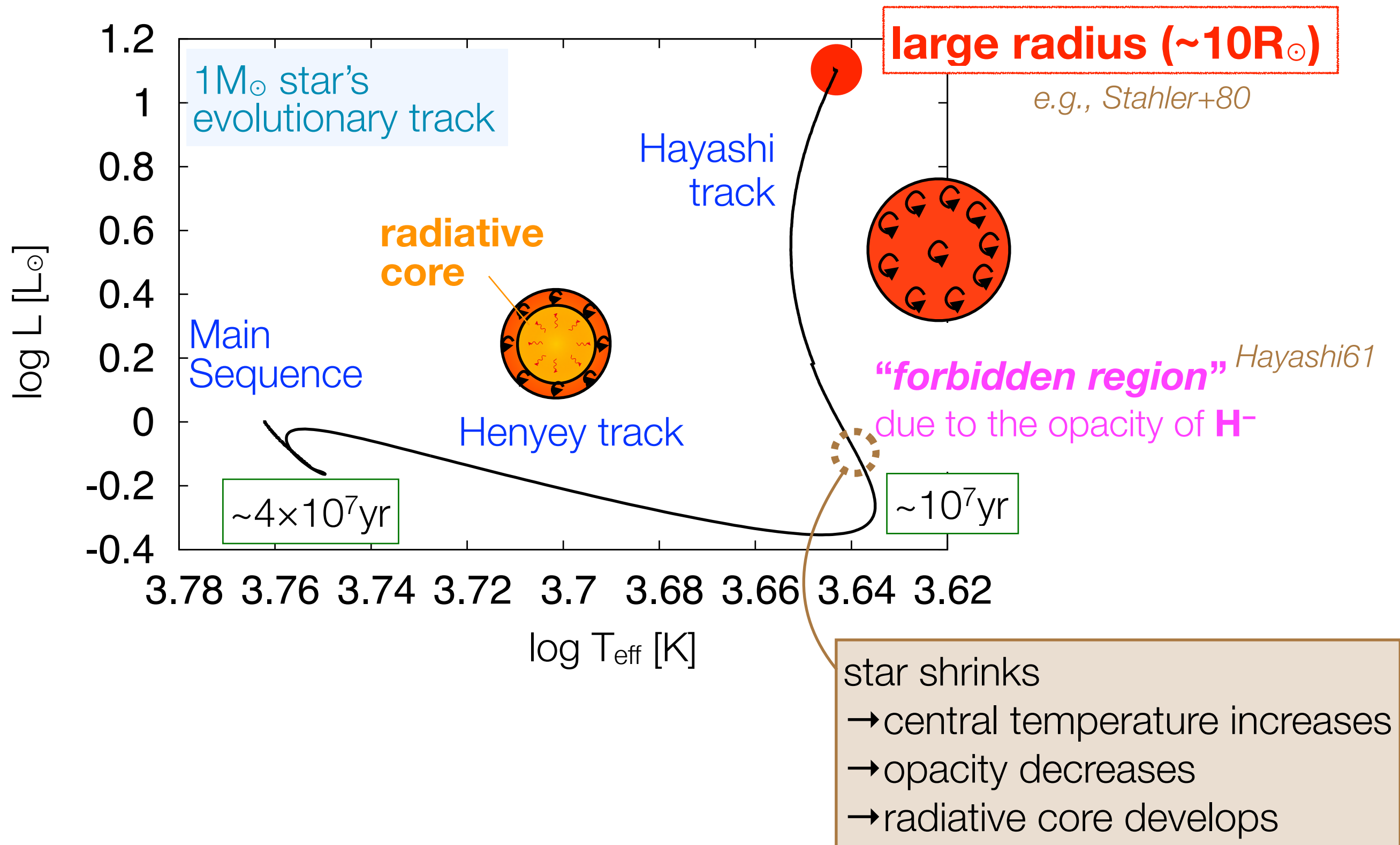
**Masanobu Kunitomo** (*Nagoya Univ.*)

collaborators

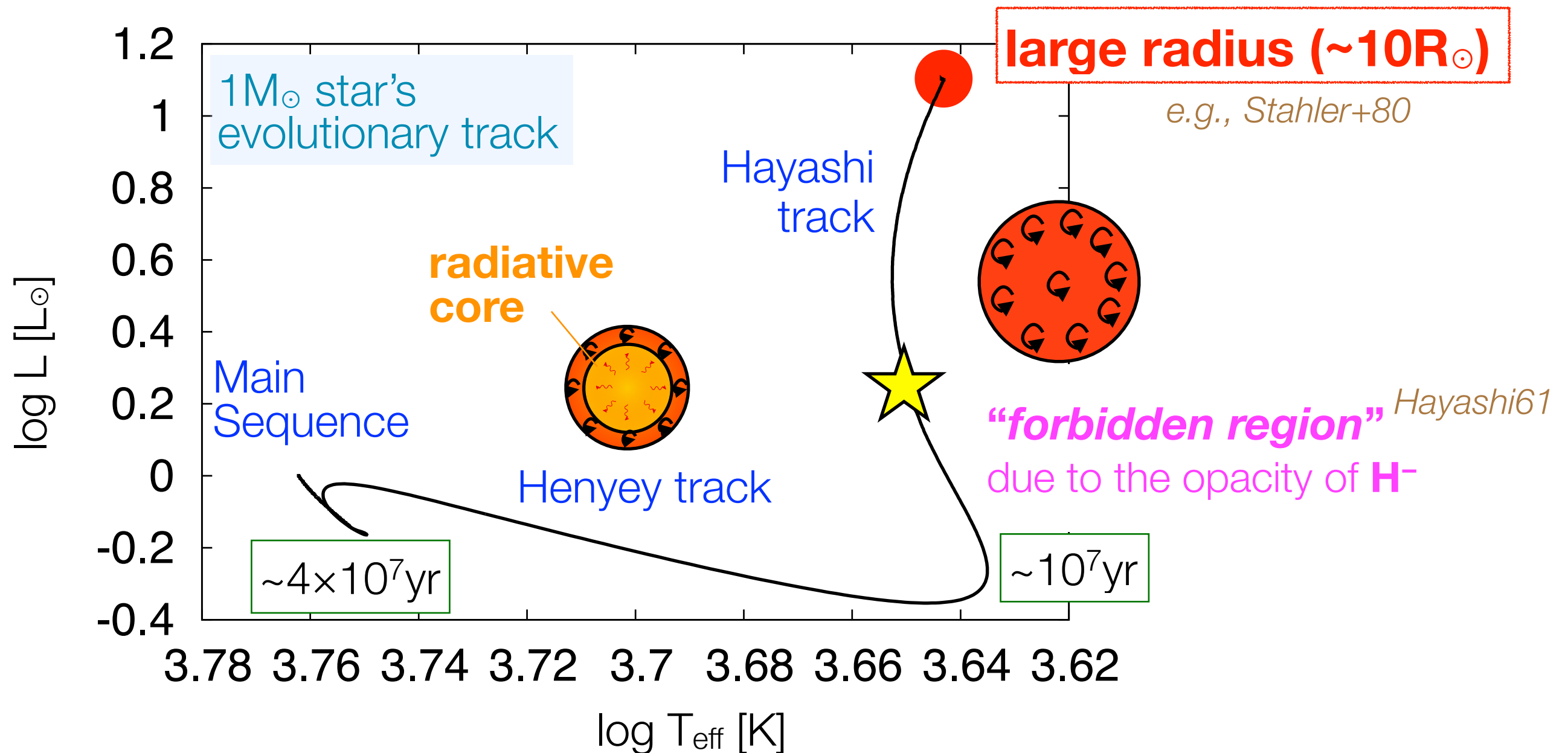
**Tristan Guillot** (*Observatoire de la Côte d'Azur*),

**Taku Takeuchi** and **Shigeru Ida** (*Tokyo Tech.*)

# Classical picture of pre-main sequence evolution



# Classical picture of pre-main sequence evolution



stellar age and mass are estimated by comparing observed  $T_{\text{eff}}$  and  $L$  with theoretical evolutionary tracks

# Classical PMS evolution may not be accurate

the classical PMS evolution has been called into question by recent observations:

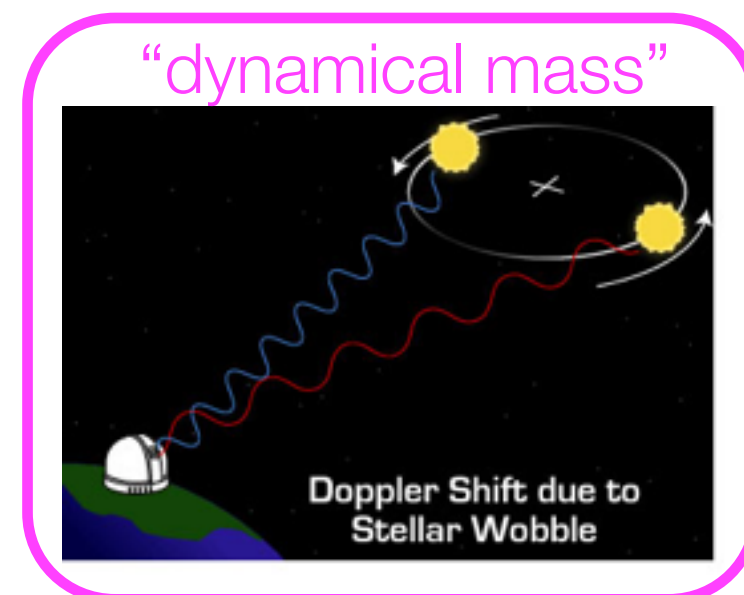
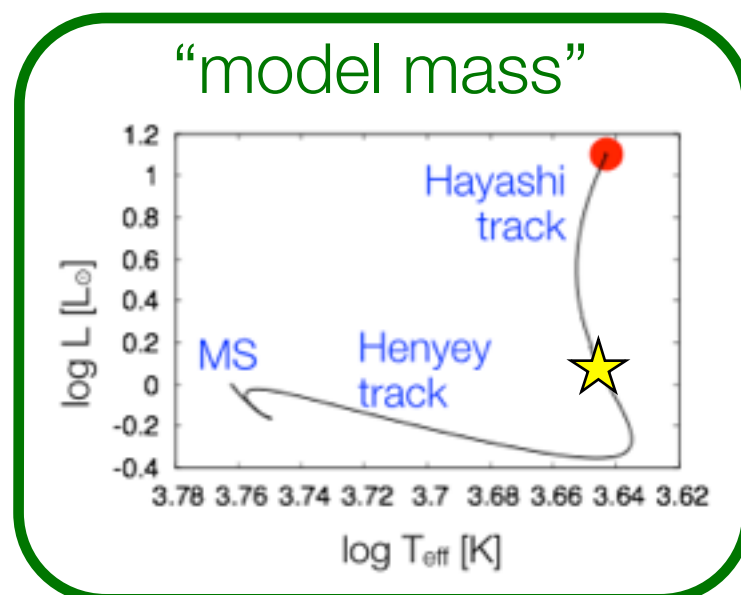
## ❖ **mass anomaly of PMS stars**

*Stassun+14*

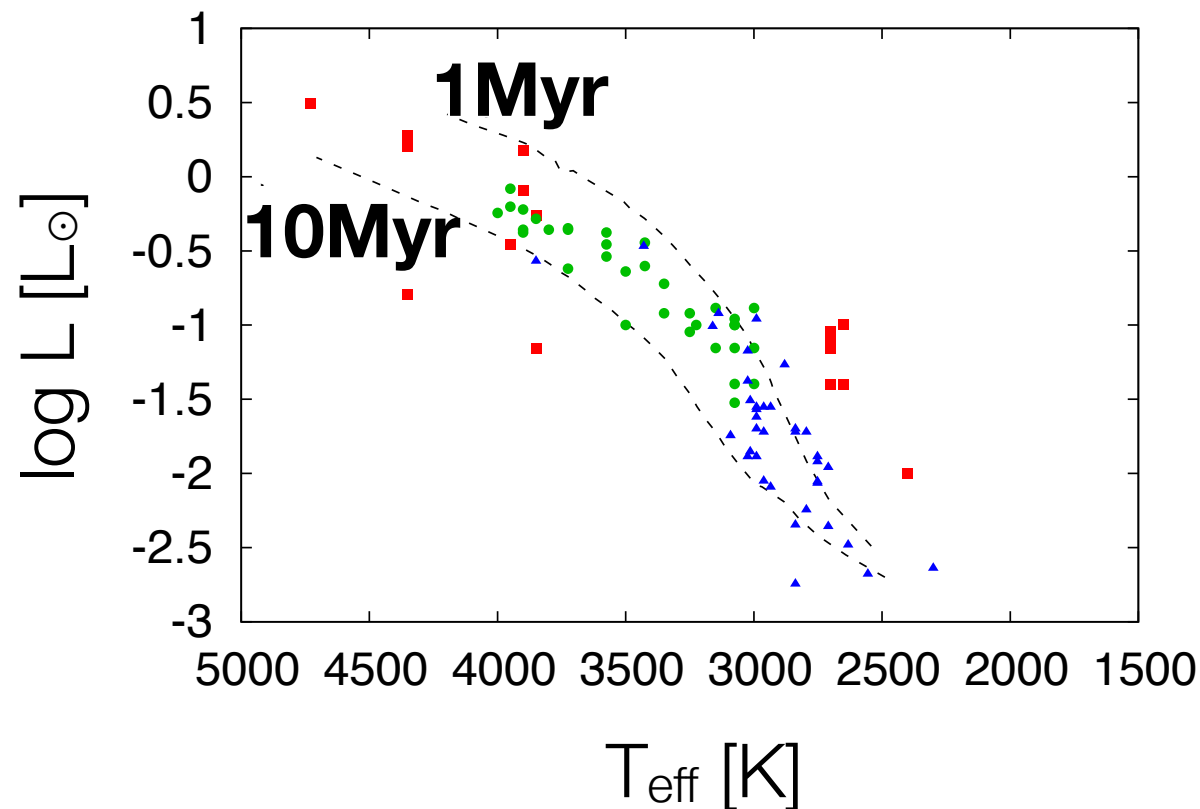
PMS stars' masses estimated with the classical evolutionary tracks are inaccurate up to **50-100%** using eclipsing binary systems

## ❖ **luminosity (age) spread problem**

*Hillenbrand09*



# Luminosity (age) spread problem



**PMS stars' ages in the same cluster widely spread ( $\sim 10\text{Myr}$ )**  
*if the classical PMS evolution is used*

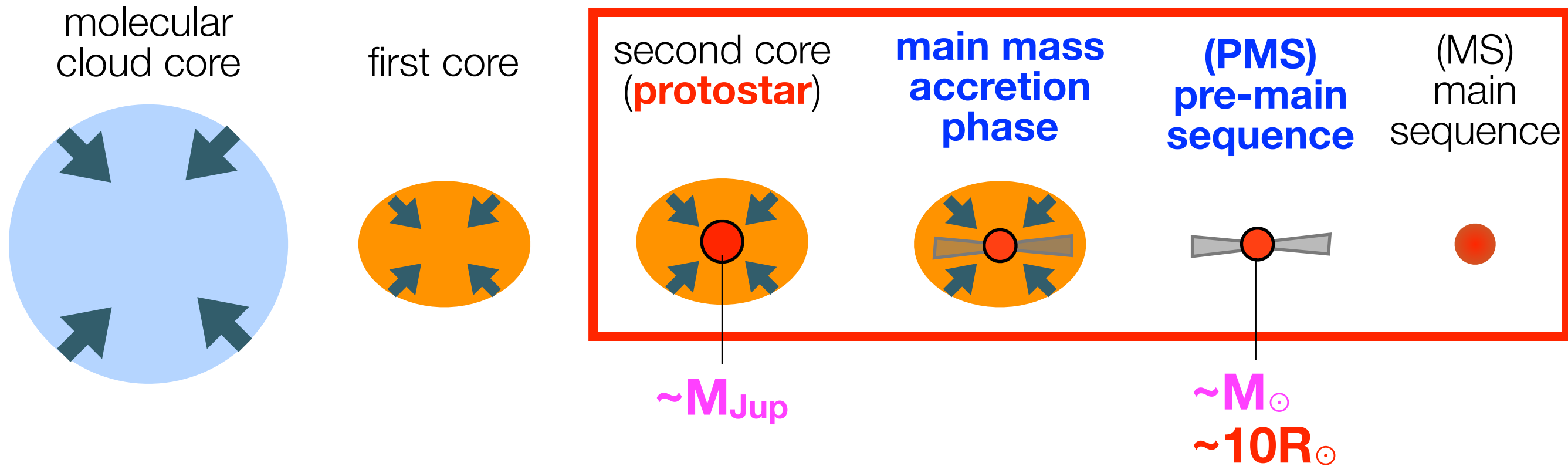
if stars in a cluster are almost coeval,  
**this is a big problem**

*possible solutions:*

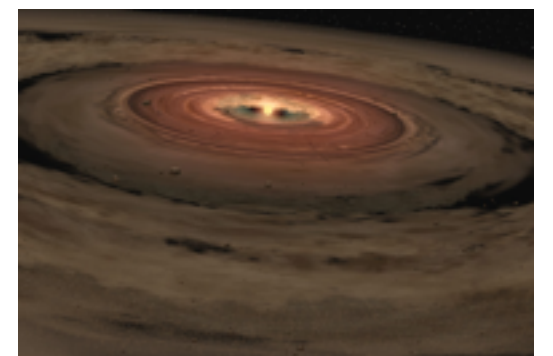
1. observational error
2. long-lasting star formation in a cluster  
(Inutsuka+15)
- 3. classical isochrones are not accurate**

(Muzerolle+05; Gatti+06,08;  
Baraffe+98)

# Standard picture of star formation

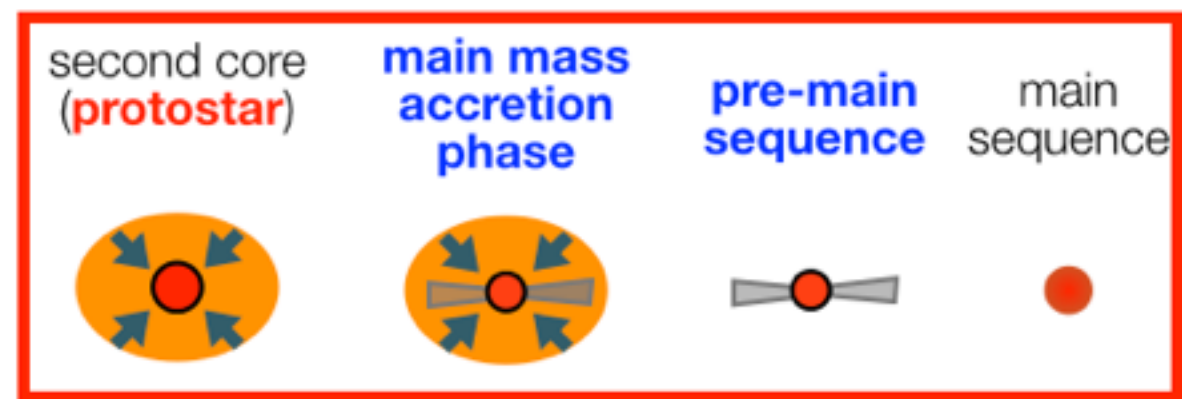


(c) NASA



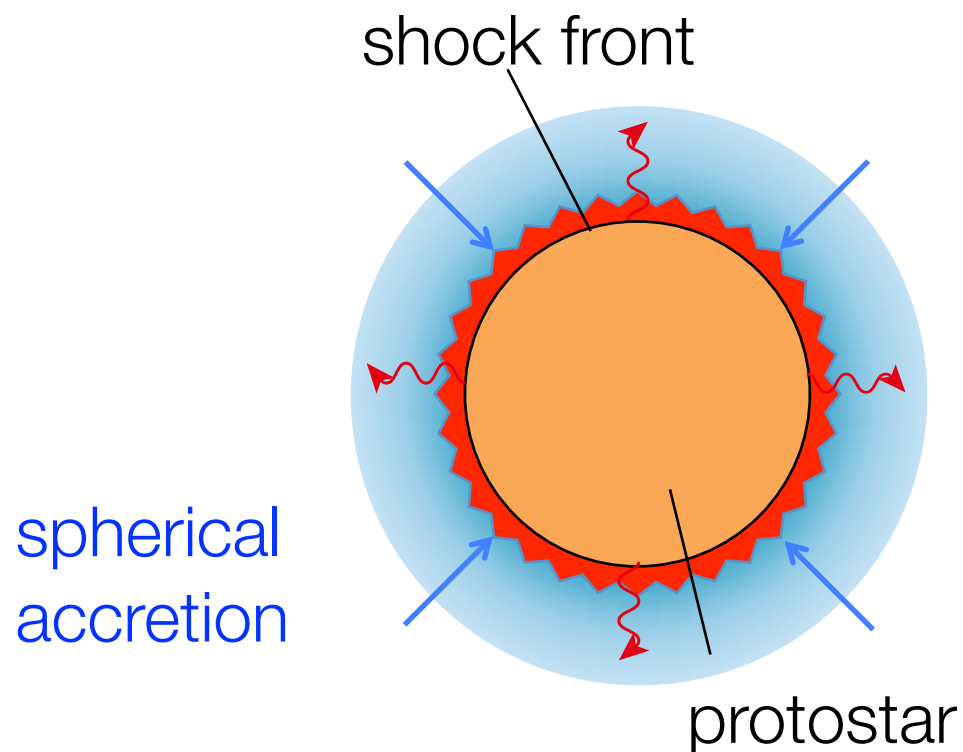
(c) NASA

# Configuration of accretion



## ■ *Classical picture*

*e.g., Stahler+80*



gravitational energy ( $GM\dot{M}/R$ )



supersonic (free-fall) velocity



thermalized at stellar surface



**inefficient radiative cooling**



**large entropy is carried**

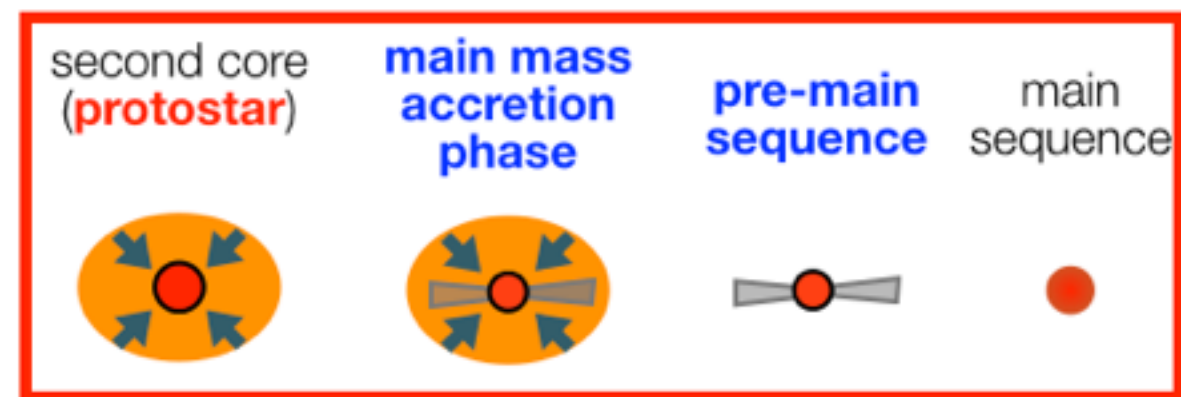
**inefficient radiative cooling**

→ **a large amount of entropy** is injected

→ star is formed with **large radius**

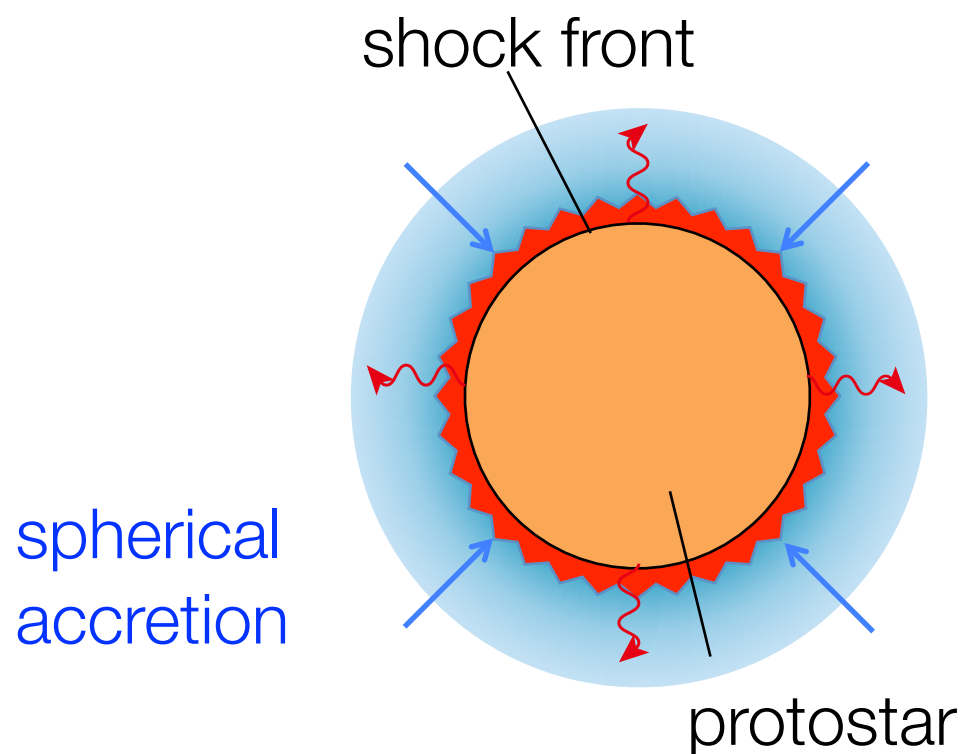


# Configuration of accretion



## ■ Classical picture

*e.g., Stahler+80*



## inefficient radiative cooling

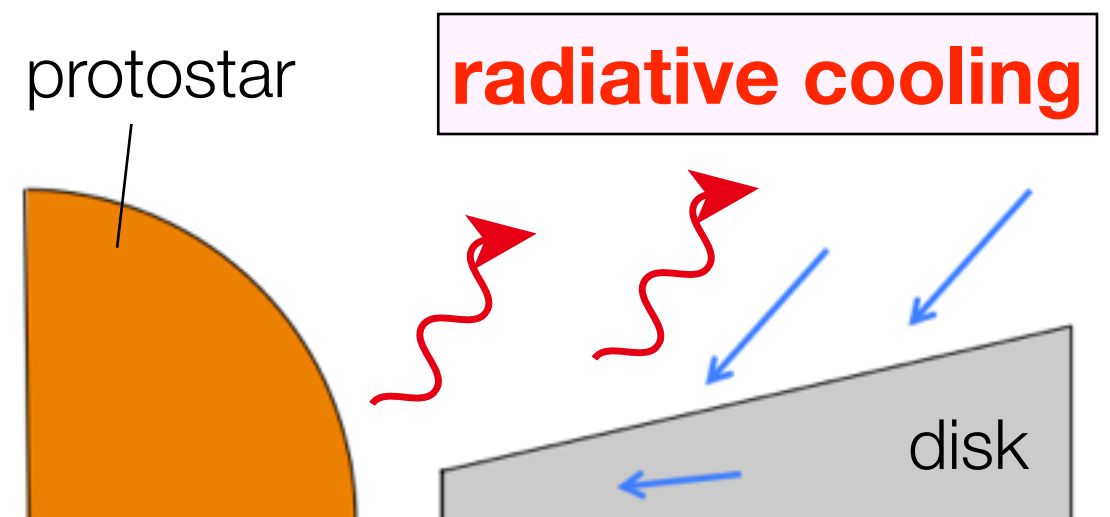
→ **a large amount of entropy** is injected

→ star is formed with **large radius**

## ■ Recent picture

*e.g., Baraffe+09*

*e.g., Machida+10,  
Tsukamoto+11,  
Kratter+10*



## efficient radiative cooling

from disk's and/or stellar surface

→ **low-entropy accretion**

we revisit the PMS evolution  
with the low-entropy accretion



# Computational method

■ Stellar evolution code MESA *Paxton+11,13*

■ Stellar structure equations (1D) **accretion is included**

1. **continuity**  $\frac{\partial r}{\partial M_r} = \frac{1}{4\pi r^2 \rho}$
2. **momentum**  $\frac{\partial P}{\partial M_r} = -\frac{GM_r}{4\pi r^4}$  (*hydrostatic equilibrium*)
3. **energy**  $\frac{\partial l}{\partial M_r} = \epsilon_{\text{nuc}} - T \frac{\partial s}{\partial t} + \epsilon_{\text{add}}$
4. **temp. gradient**  $\frac{\partial T}{\partial M_r} = -\frac{GM_r T}{4\pi r^4 P} \nabla$   
 $\nabla = \frac{d \ln T}{d \ln P}$
5. **composition**  $\left(\frac{\partial X_i}{\partial M_r}\right)_{M_r} = \frac{m_i}{\rho} \left( \sum_j r'_{ji} - \sum_k r'_{ik} \right) + \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 D \frac{\partial X_i}{\partial r} \right)$   
**nuclear reaction**      **diffusion**

$M_r$ : mass coordinate

mixing-length theory,  
 $\alpha_{\text{MLT}}=1.905$

(Cox & Giuli68;  
Henyey+65)

composition  
 $X=0.70, Z=0.02$

# Computational method

## ■ Effect of the low-entropy accretion

$$\frac{\partial l}{\partial M_r} = \varepsilon_{\text{nuc}} - T \frac{\partial s}{\partial t} + \varepsilon_{\text{add}} \quad \text{heat injection by accretion}$$

$$L_{\text{add}} = \xi G M_{\star} \dot{M} / R_{\star}$$

- heating efficiency  $\xi$  (=0-1)  
 $\xi$  is poorly constrained by RHD simulations

$$\varepsilon_{\text{add}} = L_{\text{add}} / M_{\star}$$

- distribute the injected heat uniformly in the entire star

accreting materials' gravitational energy from infinity to star:

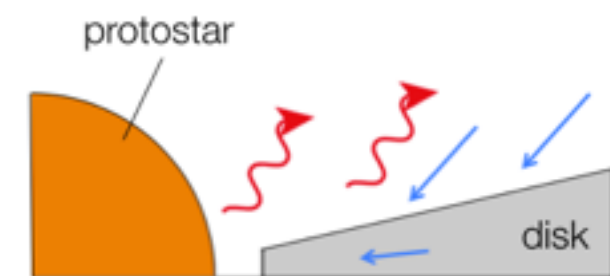
$$L_{\text{acc}} = \frac{G M_{\star}}{R_{\star}} \dot{M}$$

$$L_{\text{add}} = \xi L_{\text{acc}}$$

**injected to the star**

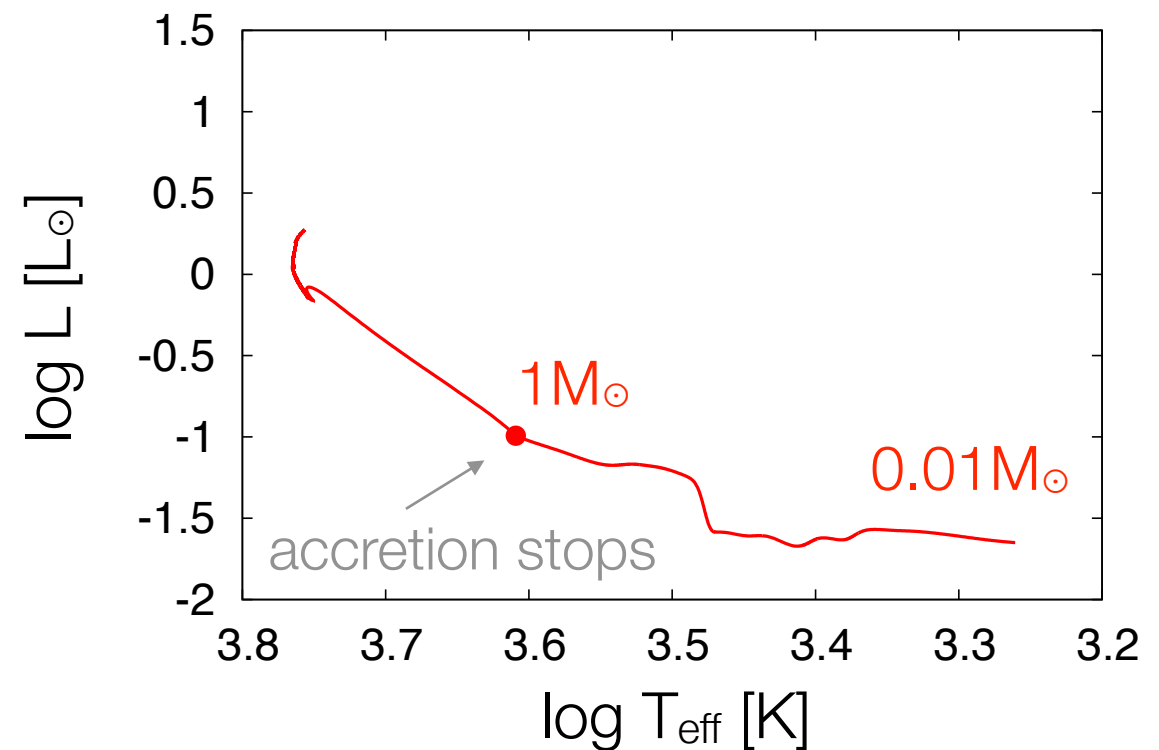
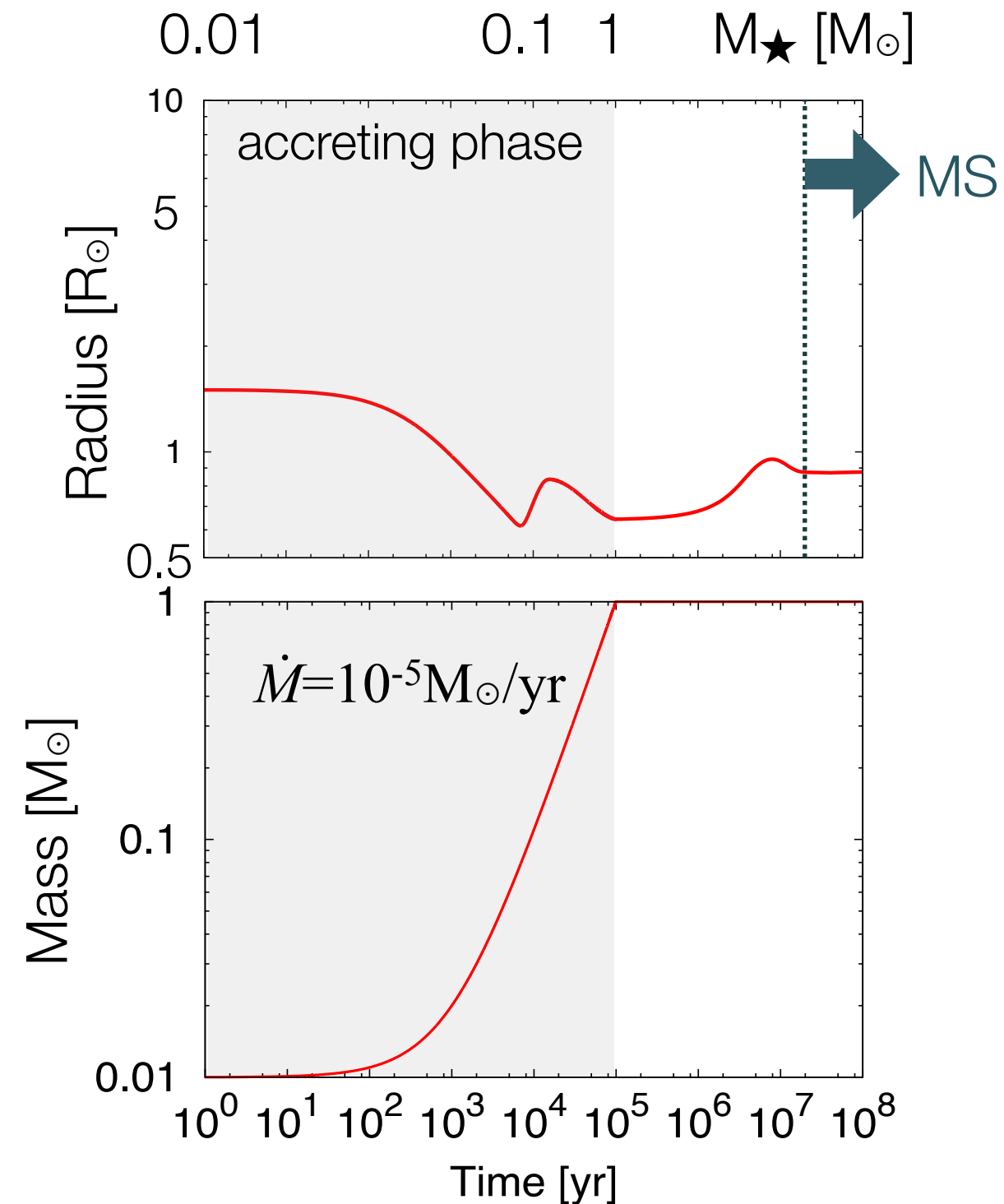
$$L_{\text{rad}} = (1 - \xi) L_{\text{acc}}$$

**radiated away (+rotation)**



# PMS evolution with low-entropy accretion

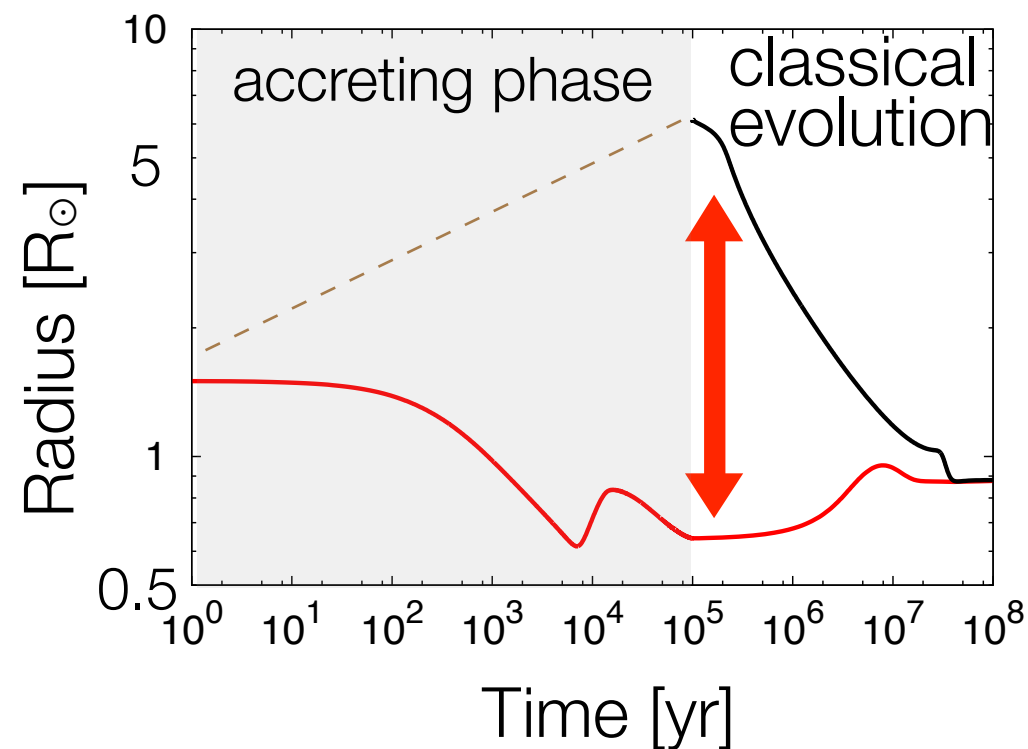
$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ \xi &= 0, X_D = 2.0 \times 10^{-5} \end{aligned}$$



# Comparison with classical evolution

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ \xi &= 0, X_D = 2.0 \times 10^{-5} \end{aligned}$$

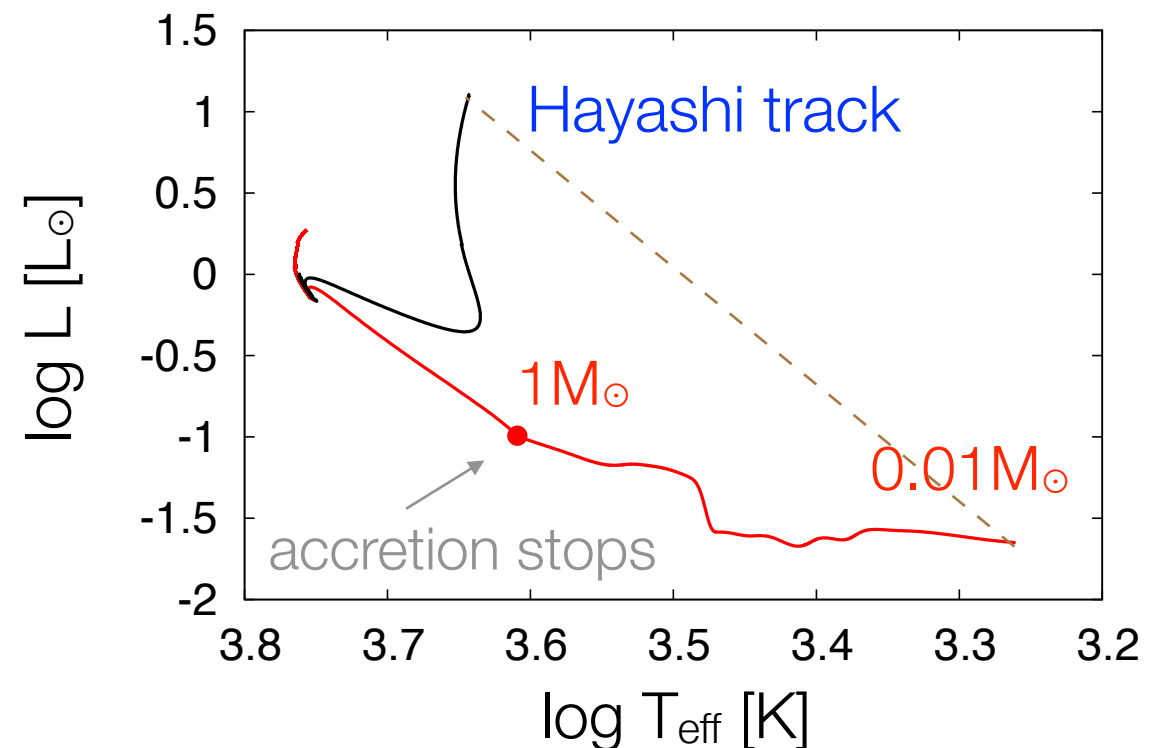
■ Radius evolution



- **below  $1 R_{\odot}$**

- about one order of magnitude smaller radius

■ Evolutionary track



- small luminosity

- **no Hayashi track**

**low-entropy accretion** →  
significantly different from  
the classical evolution

different evolutionary track  
results in different estimation of  
 $M_{\star}$  and age

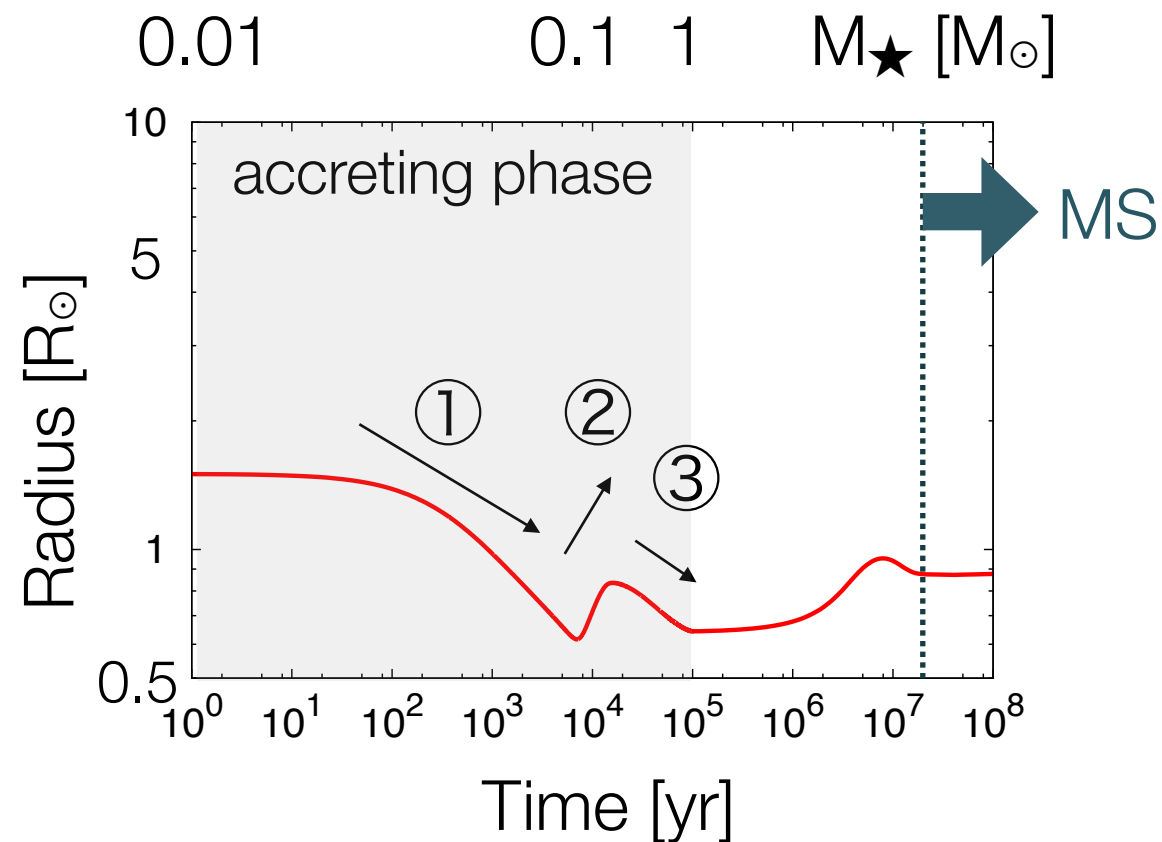
# PMS evolution with low-entropy accretion

$$M_{\text{ini}} = 0.01 M_{\odot}$$

$$M_{\text{fin}} = 1 M_{\odot}$$

$$\dot{M} = 10^{-5} M_{\odot}/\text{yr}$$

$$\xi = 0, X_{\text{D}} = 2.0 \times 10^{-5}$$



## ①: adiabatic contraction

- constant entropy because  $\xi = 0$
- shrink due to the mass accretion

## ②: deuterium burning

- $\text{D} + \text{p} \rightarrow {}^3\text{He} + 5.5 \text{ MeV}$  ( $T > 10^6 \text{ K}$ )  
→ **entropy supply**

## ③: depletion of deuterium

- mass accretion overcomes D-burning

stellar radius is determined by **mass** and **entropy**

$$R \propto M^{-1/3} \exp \left[ \frac{2}{3} \frac{\mathcal{R}}{\mu} (s - s_0) \right]$$

(fully convective, hydrostatic equilibrium, monoatomic ideal gas)

*Chandrasekhar67*

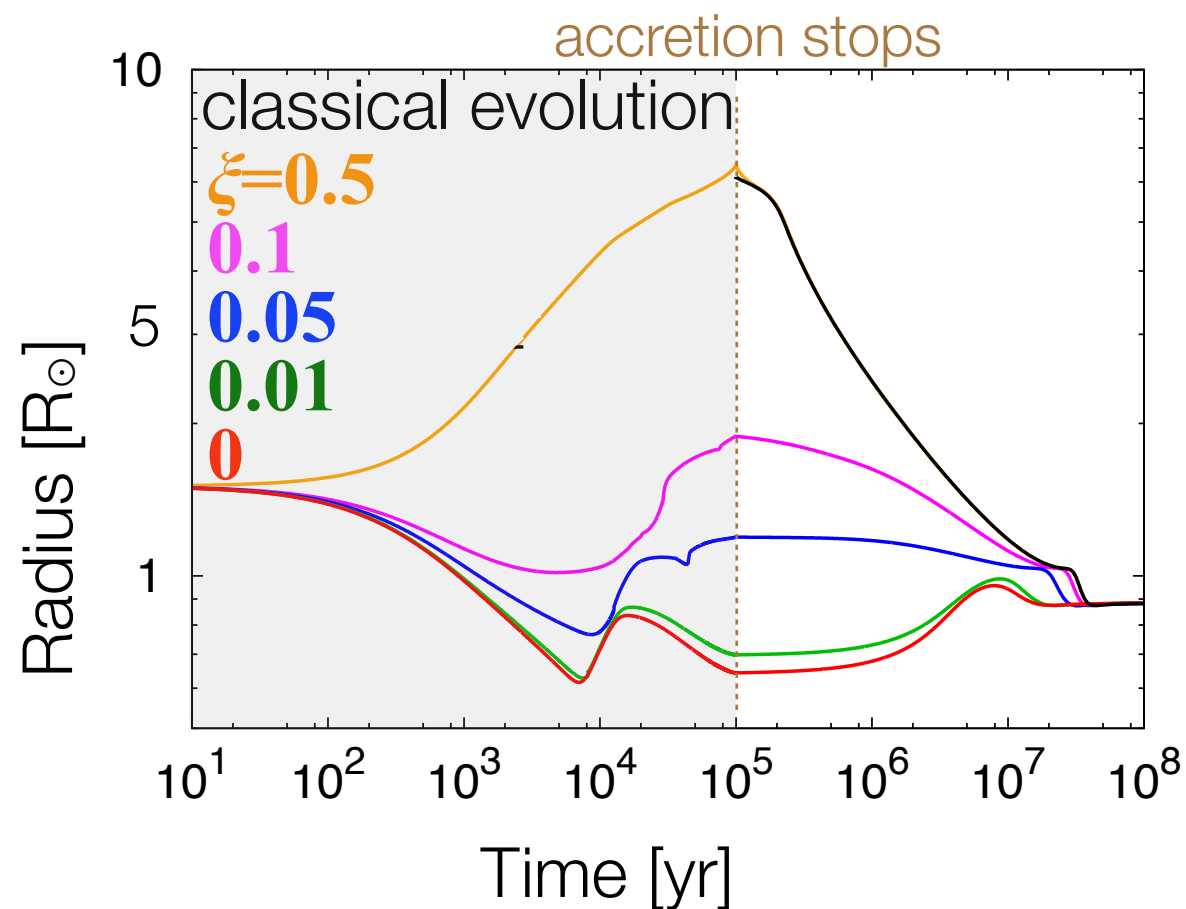
**accreting material's entropy**  
and **deuterium content**  
are important

# Dependence on the **heating efficiency** $\xi$

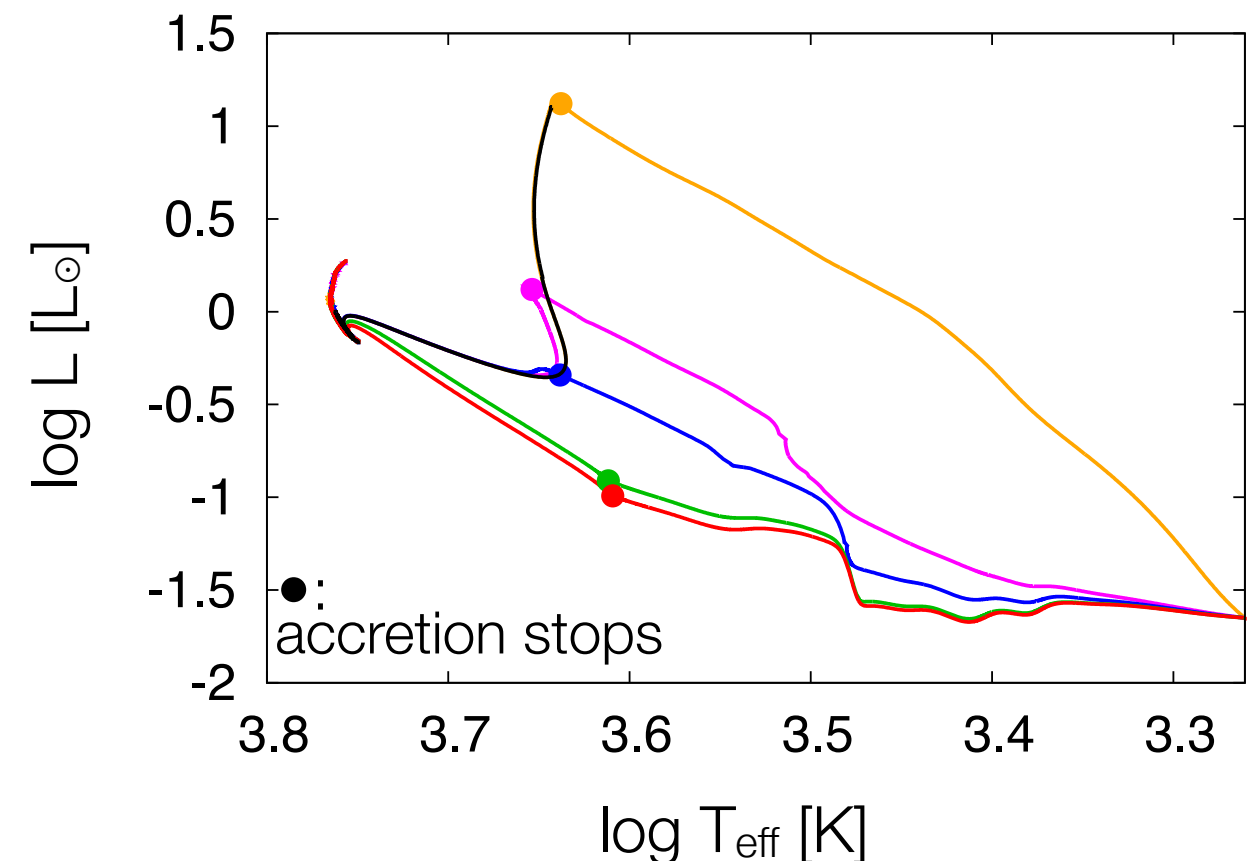
$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ X_{\text{D}} &= 2.0 \times 10^{-5} \end{aligned}$$

$$L_{\text{add}} = \xi G M \dot{M} / R$$

## ■ Radius evolution



## ■ Evolutionary track



$$R \propto M^{-1/3} \exp \left[ \frac{2}{3} \frac{\mathcal{R}}{\mu} (s - s_0) \right]$$

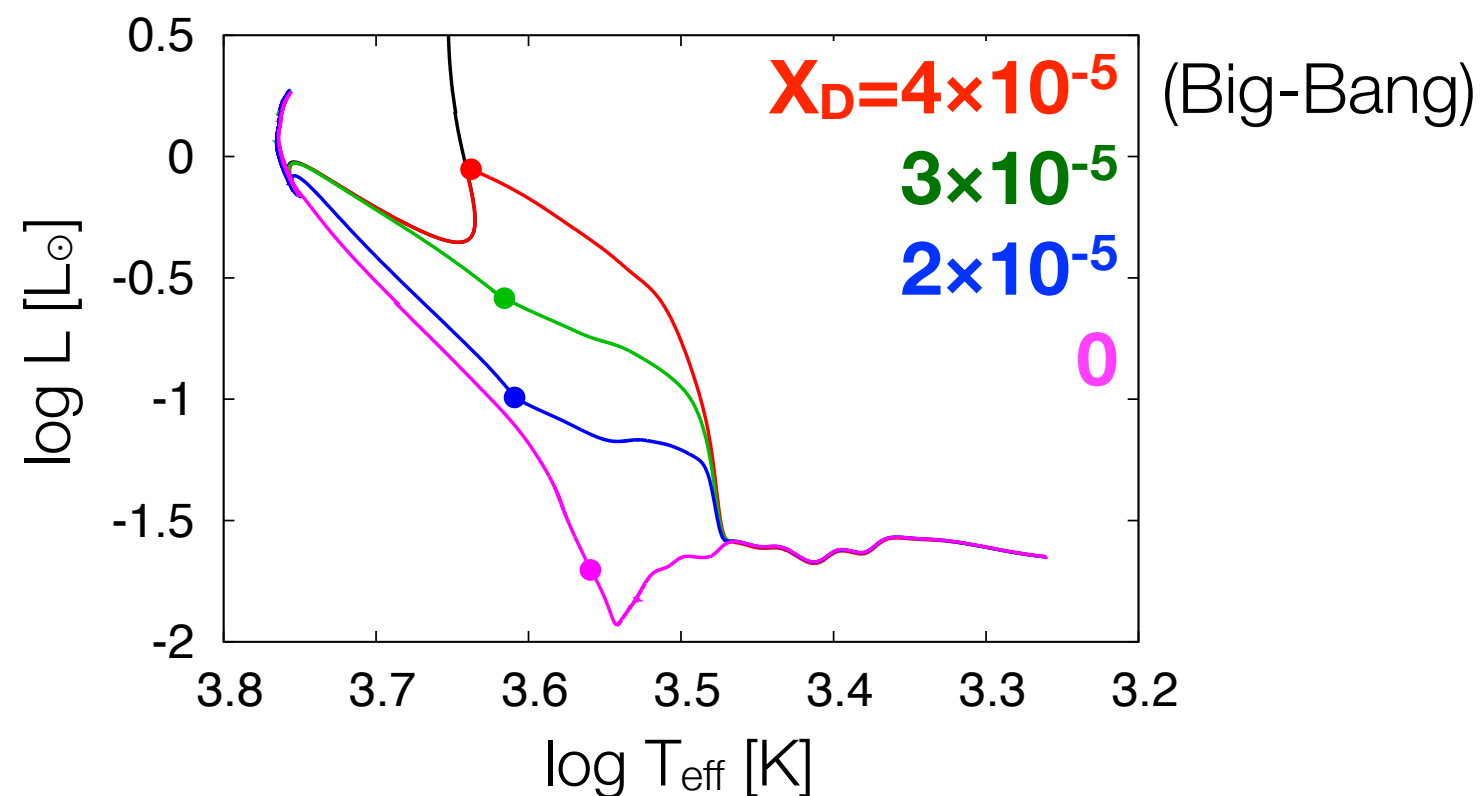
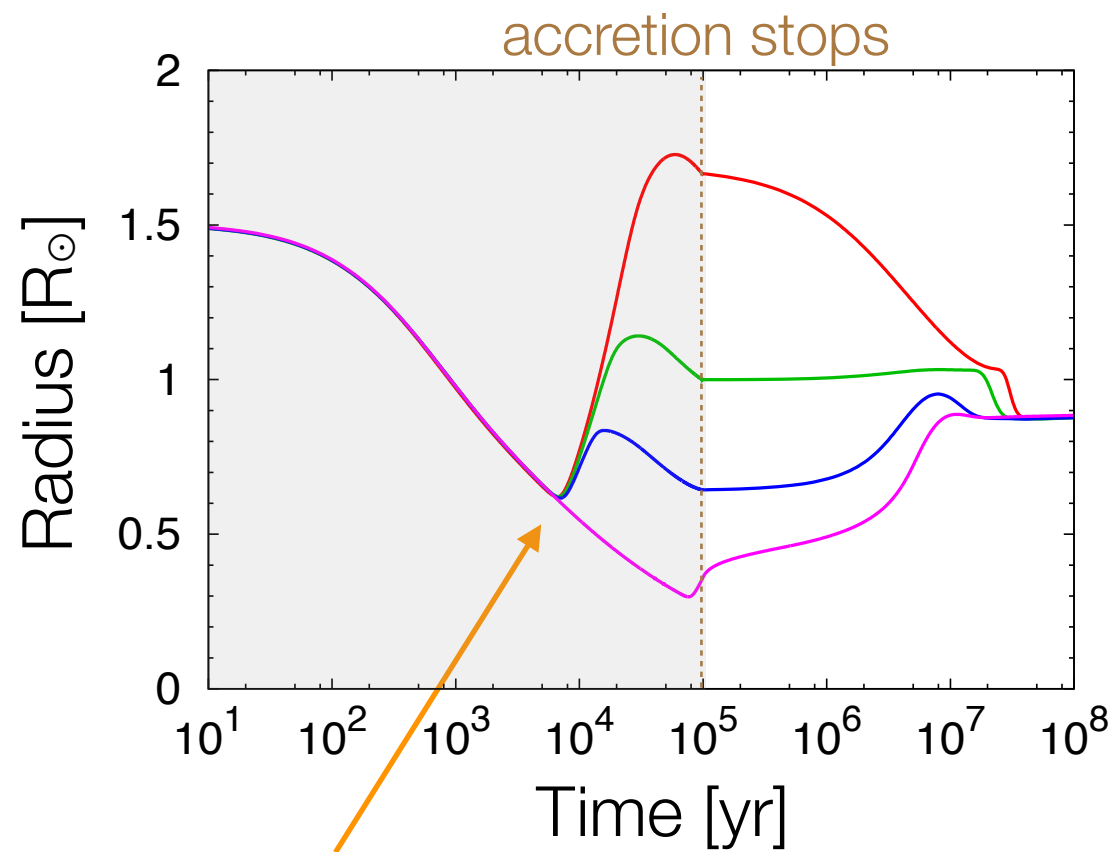
- high entropy injection rate  $\rightarrow$  expansion
- $\xi$  largely affects the **PMS evolution**



# Dependence on the **deuterium content** $X_D$

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ \xi &= 0 \end{aligned}$$

- Deuterium content **decreases with time** after the Big-Bang
- It can be different in each star even in the same age**

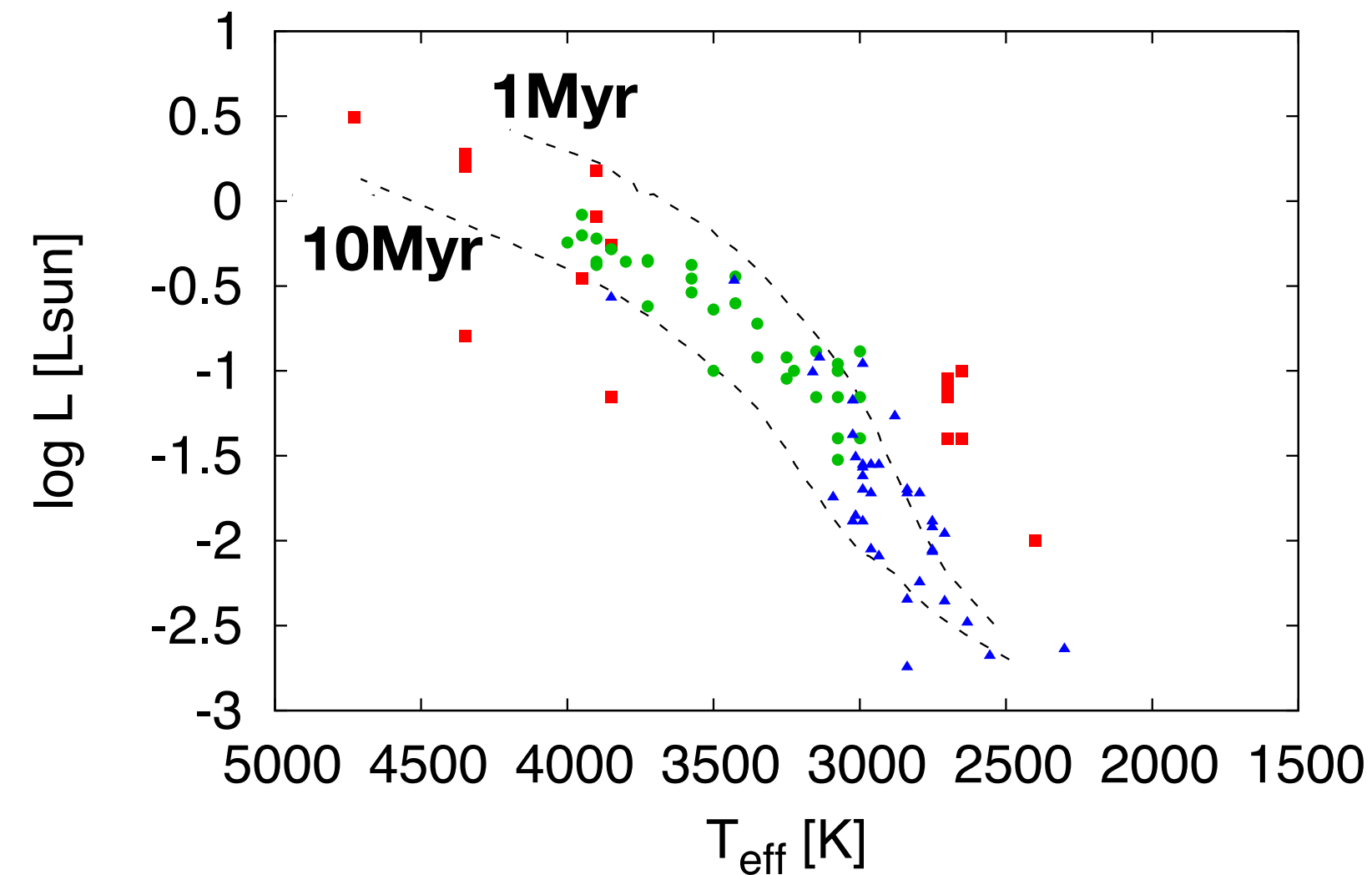


deuterium burning starts

- large deuterium content  $\rightarrow$  lots of entropy is generated  $\rightarrow$  expansion
- different evolutionary tracks in the high temperature region**

# Impact on the luminosity spread problem

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ X_{\text{D}} &= 2.0 \times 10^{-5} \end{aligned}$$



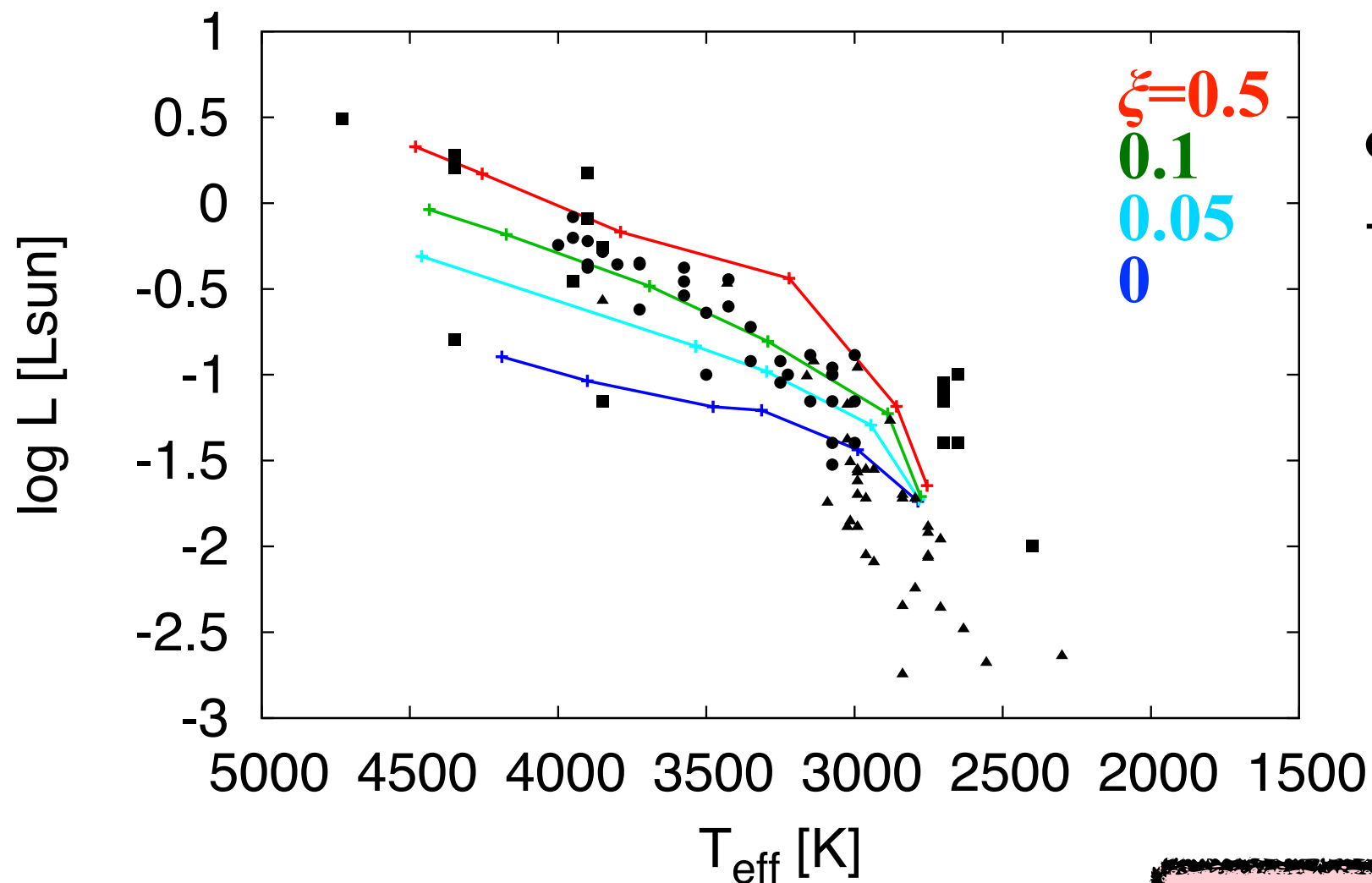
- ▲ Taurus and Chamaeleon I
- ρ Ophiucus
- σ Orionis
- classical isochrone

(Muzerolle+05; Gatti+06,08;  
Baraffe+98)

# Impact on the luminosity spread problem

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ X_{\text{D}} &= 2.0 \times 10^{-5} \end{aligned}$$

## 1 Myr isochrones with different $\xi$



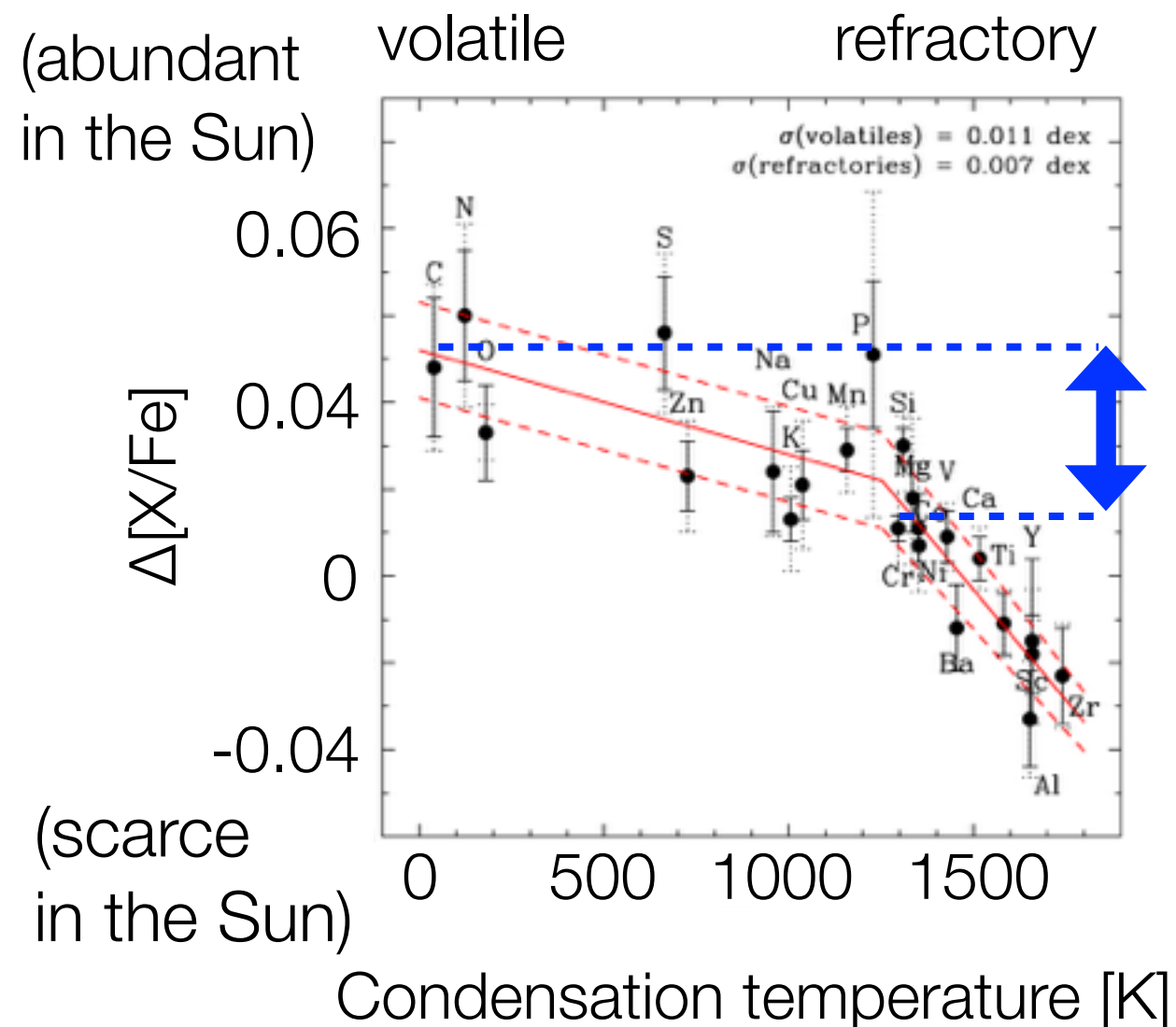
- isochrones spread widely
- **isochrones of different  $\xi$  can explain the observed luminosity spread**



**Estimation of stellar ages and masses using the classical isochrones is no longer valid**

# Anomaly of the solar surface composition

## Our Sun is a peculiar star



$\Delta[X/Fe] = [X/Fe]_{\odot} - [X/Fe]_{\text{solar-twins}}$   
: difference between the Sun and solar-twins

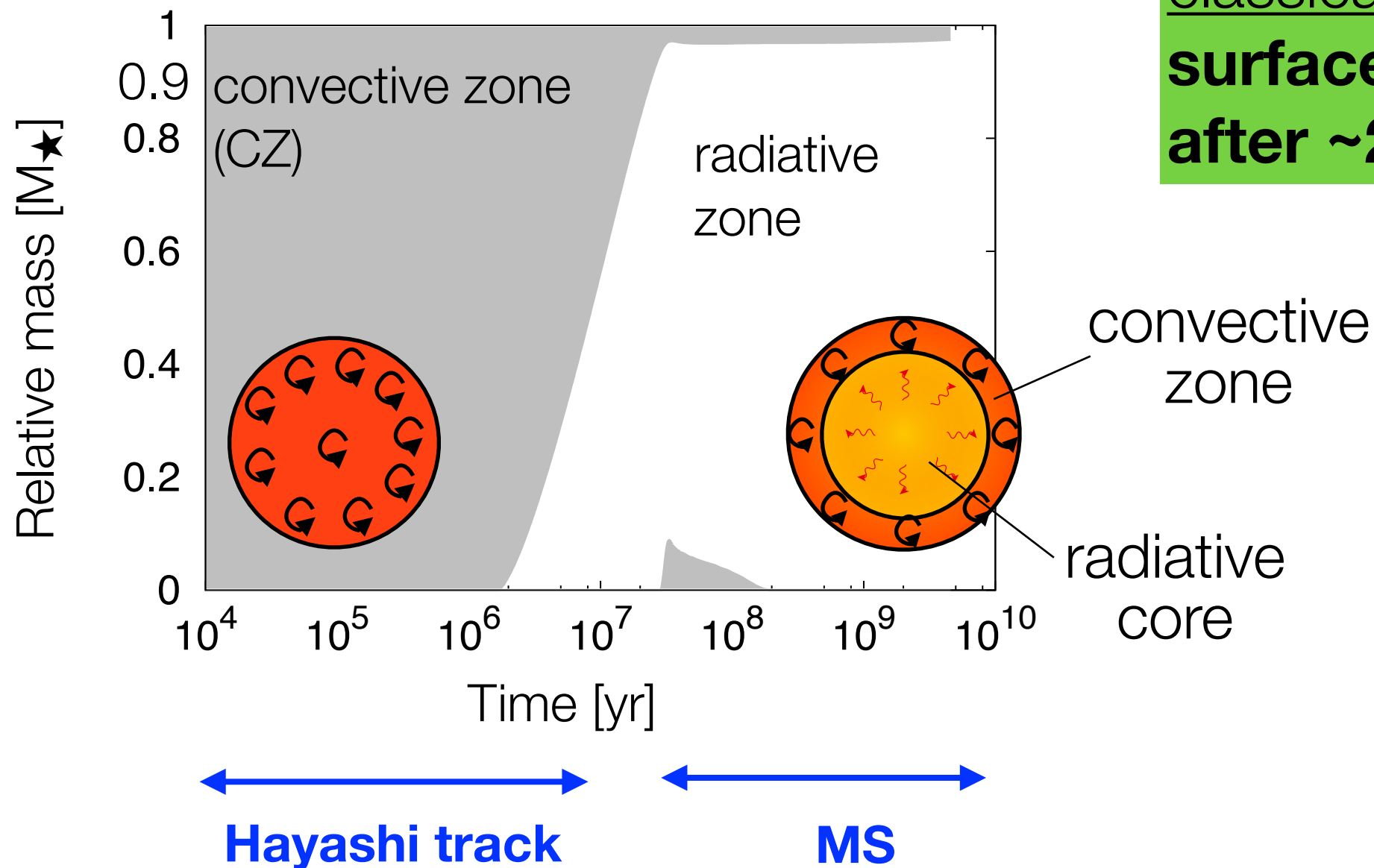
- the Sun is
  - **abundant in volatile** and
  - **scarce in refractory elements**compared to the solar-twins
- difference:  $\sim 0.04 \text{ dex} \sim 10\%$

Melendez+09

\*solar-twins: stars with the similar **age**,  
**metallicity**, **luminosity** and **mass** to the Sun

# Internal structure evolution

## ■ Classical $1 M_{\odot}$ evolution

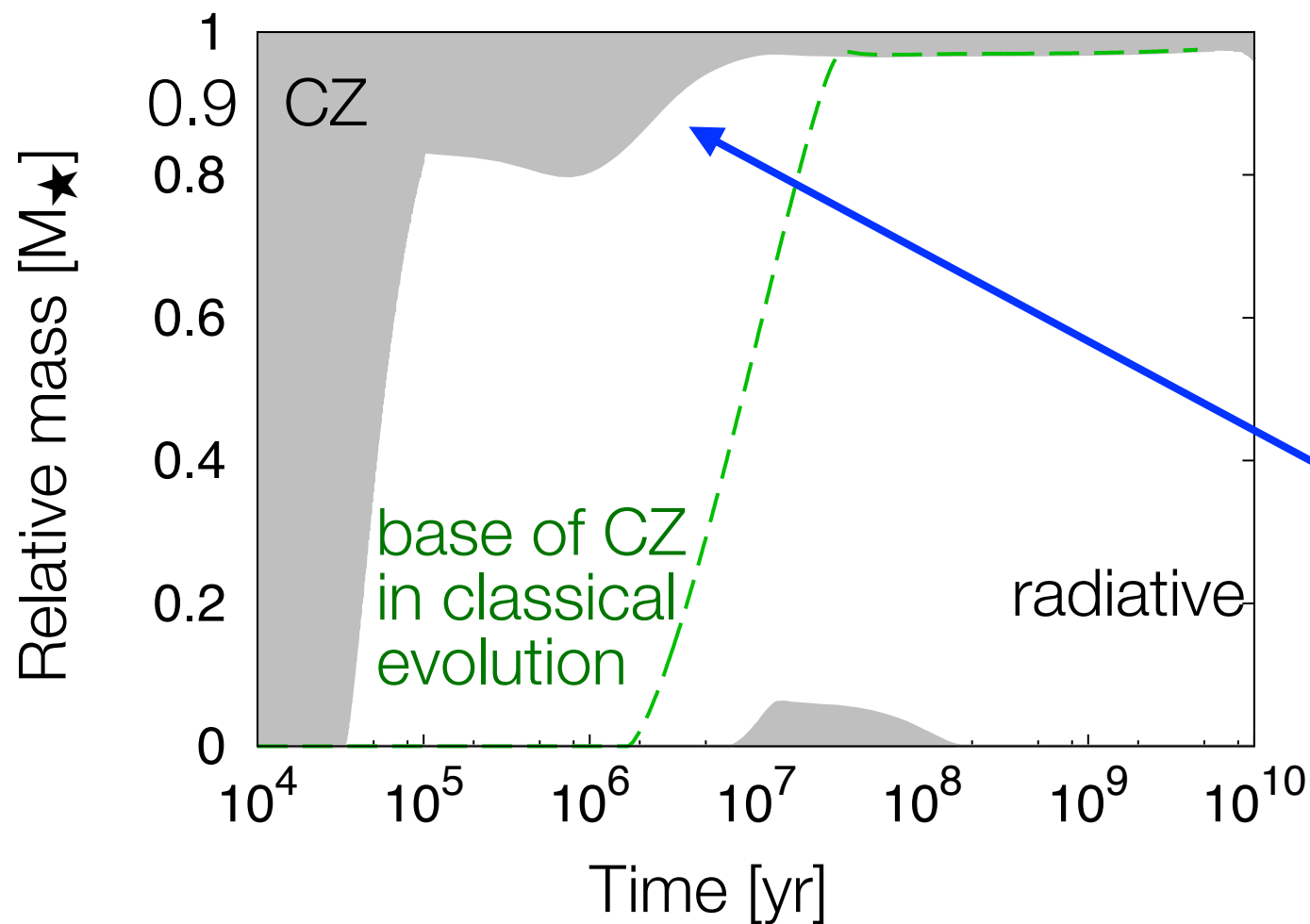


classical evolution:  
**surface CZ shrinks  
after ~20 Myr**

# Internal structure evolution with low-entropy accretion

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ \xi &= 0, X_D = 2.0 \times 10^{-5} \end{aligned}$$

## ■ low-entropy accretion



classical evolution:  
**surface CZ shrinks  
after ~20 Myr**



low-entropy accretion:  
**CZ shrinks much faster**

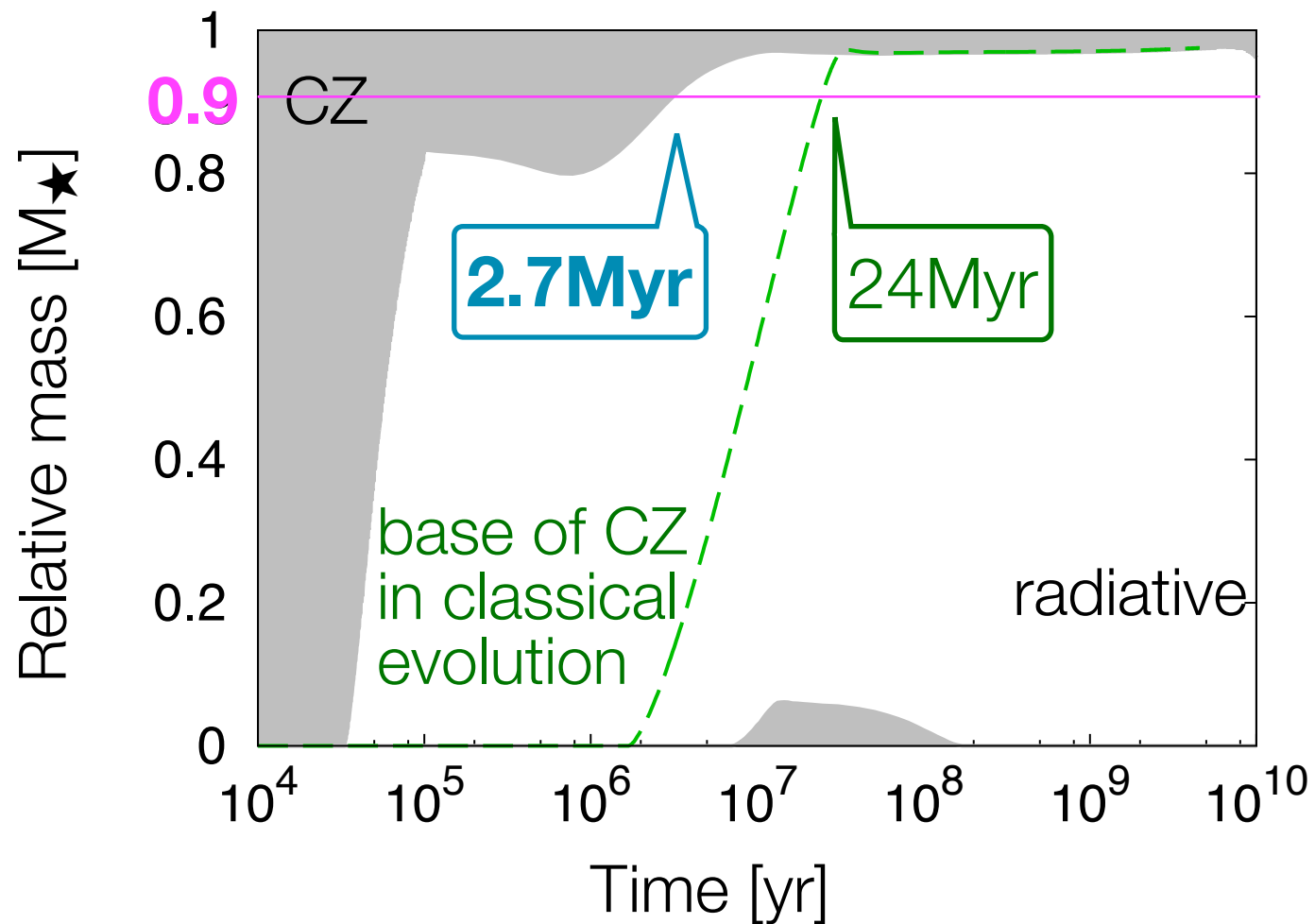
- smaller radius
  - higher internal temperature
  - smaller opacity
  - radiative zone can be developed more easily



# Internal structure evolution with low-entropy accretion

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \\ \xi &= 0, X_D = 2.0 \times 10^{-5} \end{aligned}$$

## ■ low-entropy accretion

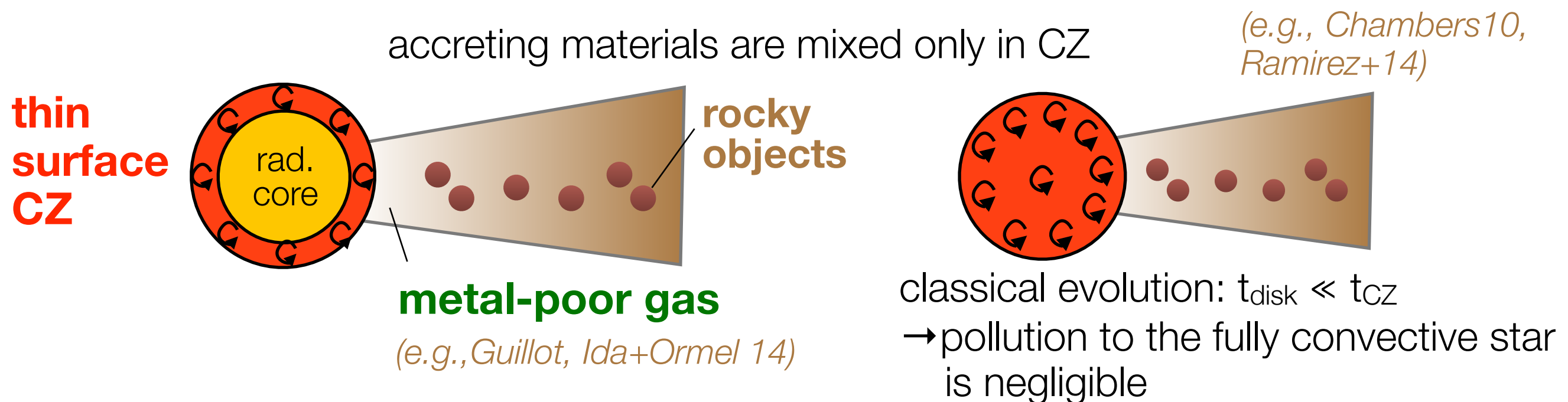


- age when mass in CZ becomes  $0.1 M_{\odot}$   
low-entropy acc.: **2.7Myr**

- ~10 times faster than the classical evolution
- **shorter than the typical disk lifetime (~6Myr)**

# Pollution of stellar surface by planet formation

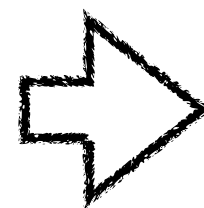
- **thin CZ** within the disk lifetime
- **metal-poor accretion** due to formation of rocky planets
- **stellar surface can be polluted** to be metal-poor composition



Planet formation can affect the host star's surface composition

This process may be the solution of

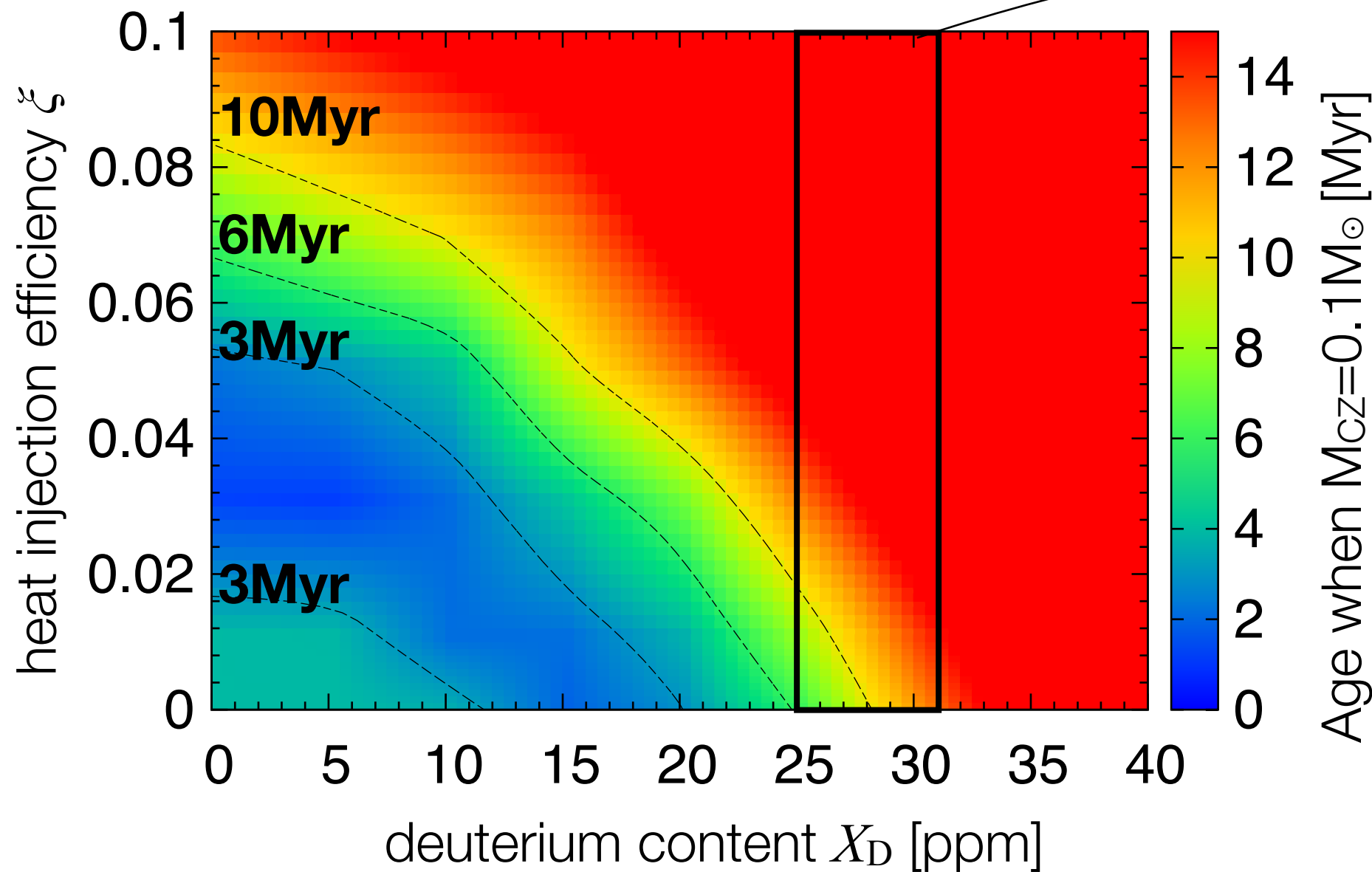
- the solar/stellar anomaly of composition
- the solar metallicity problem



We derive the condition in which this mechanism occurs ( $t_{\text{disk}} > t_{\text{cz}}$ )

# Age of CZ shrinkage

$$\begin{aligned} M_{\text{ini}} &= 0.01 M_{\odot} \\ M_{\text{fin}} &= 1 M_{\odot} \\ \dot{M} &= 10^{-5} M_{\odot}/\text{yr} \end{aligned}$$



**terrestrial planet formation can be imprinted to the stellar surface**

- CZ shrinks before disk lifetime in low  $\xi$  and  $X_{\text{D}}$
- given **low entropy accreted ( $\xi=0-0.02$ ), the solar surface composition anomaly** can be made by planet formation process

# Summary

We calculated PMS evolutions with the low-entropy accretion and found

(1) stars formed by the low-entropy accretion evolve with the much lower radius and luminosity than the classical evolution

→ **affects the estimation of stellar mass and age,  
disk evolution, and planet formation**

(2) the PMS evolution strongly depends on the heat injection efficiency and deuterium content

(3) the luminosity spread problem and the solar composition anomaly can be explained by the low-entropy accretion

(4) multidimensional RHD simulations are needed to determine the accreting materials' entropy

