

High Density Matter from QCD



<https://www.youtube.com/watch?v=MTvgnYG9b9g>



Muse - Neutron Star Collision (Love Is Forever) [OFFICIAL VIDEO]

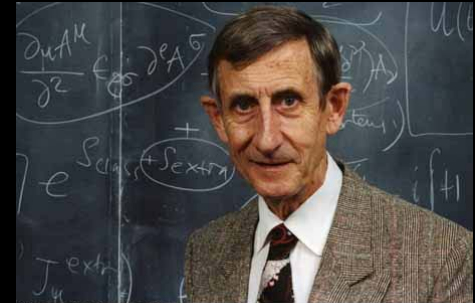
第27回 理論懇シンポジウム「理論天文学・宇宙物理学と境界領域」

2014年 12月24日(水)

Tetsuo Hatsuda (RIKEN)

The progress of science requires the growth of understanding in both directions, downward from the whole to the parts and upward from the parts to the whole.

From "The Scientist as Rebel" by Freeman J. Dyson



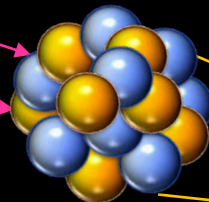
Scanned at the American Institute of Physics

nucleon



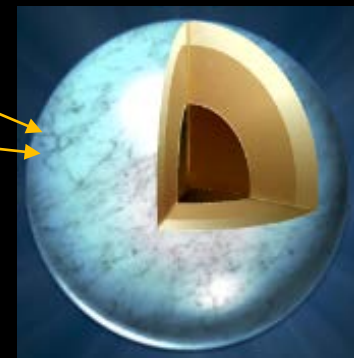
$r \sim 1$ [fm]

nucleus



$r \sim 10$ [fm]

Neutron star



$r \sim 10$ [km]

Plan of this Talk

1. Introduction : **phase structure** of QCD

2. **Baryon forces** from Lattice QCD (LQCD)

Inoue et al. [HAL QCD Coll.], PRL 106 (2011) 162002

3. **Nuclear & Neutron Matter** from LQCD

Inoue et al. [HAL QCD Coll.], PRL 111 (2013) 112503

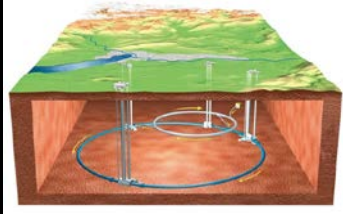
4. **Finite Nuclei** from LQCD

Inoue et al. [HAL QCD Coll.], arXiv: 1408.4892

5. Summary

QCD Phase Structure

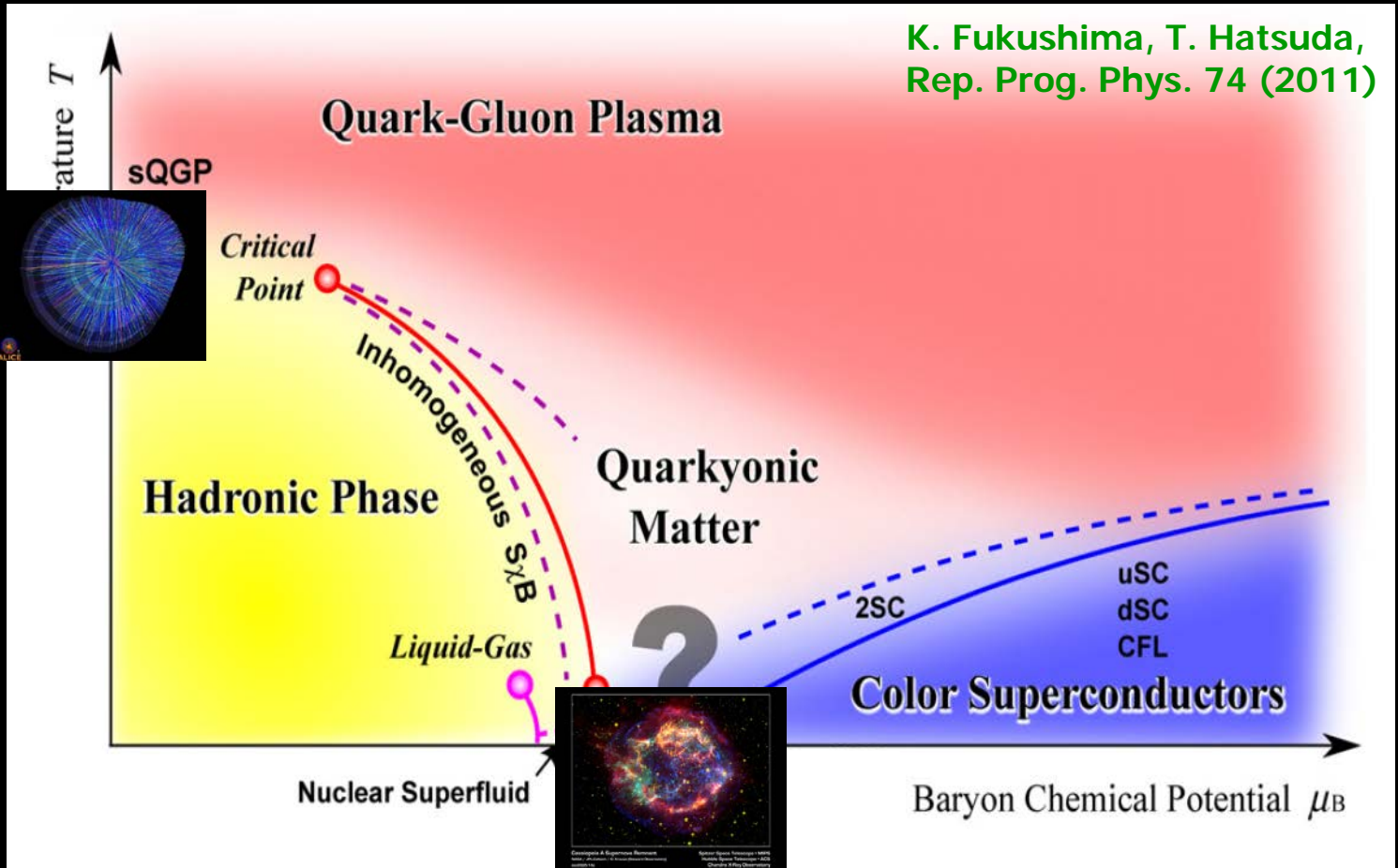
Physics of
Early Universe



LHC @ CERN



RHIC @ BNL

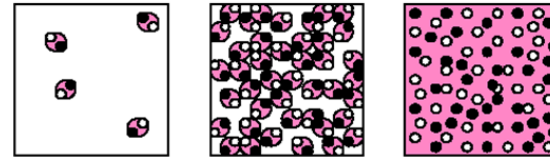


Physics of
Neutron stars
and Black holes

From QCD to Hot Matter

Quantum Chromo Dynamics

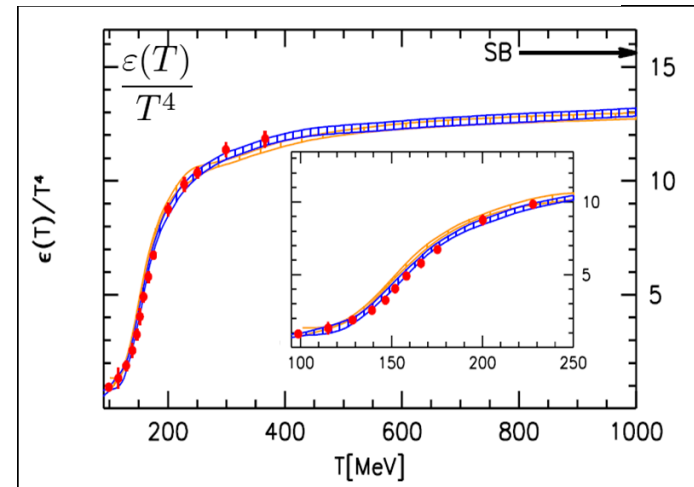
Lattice QCD



$T < T_c$

$T \sim T_c$

$T > T_c$

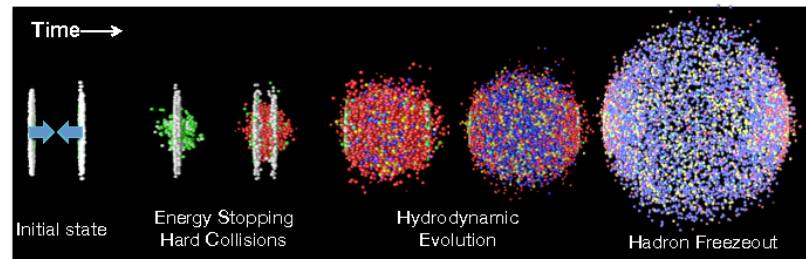


Wuppertal-Budapest Coll. JHEP 1011 (2010) 77

Equation of State for Hot Matter

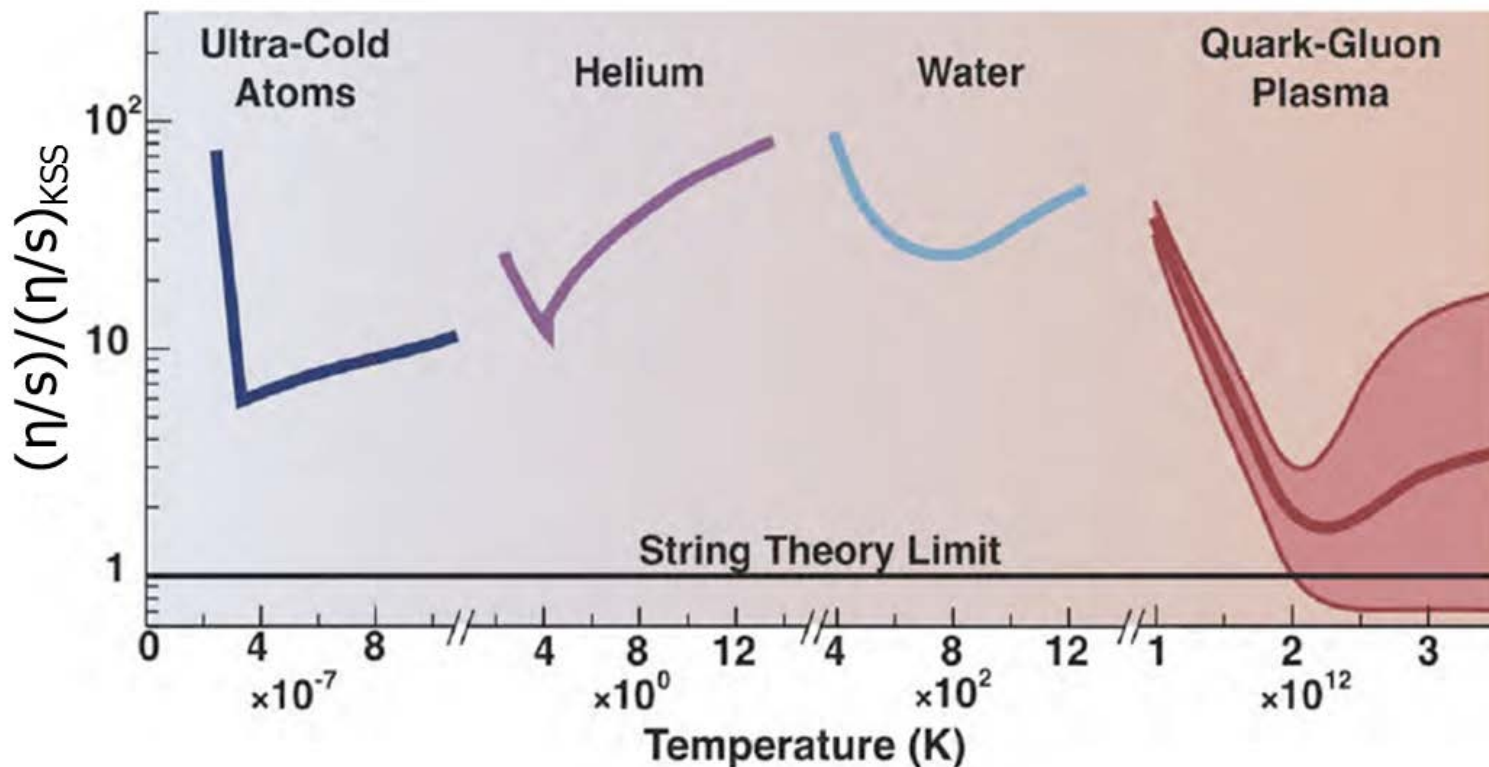
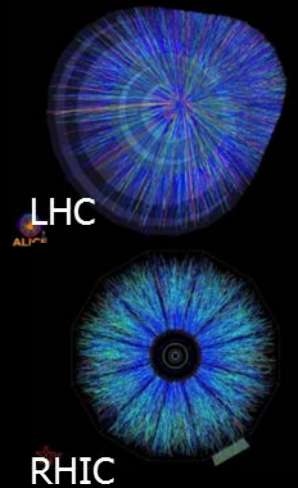
Relativistic hydrodynamics

Relativistic heavy-ion collisions



Quark-Gluon Plasma at RHIC/LHC

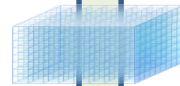
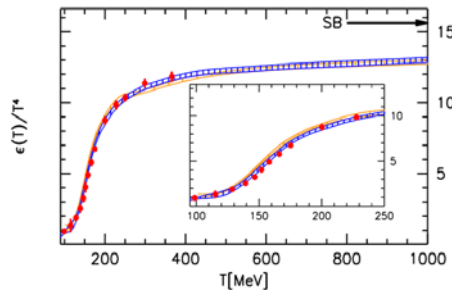
- high temp.: $T \sim 4 \times 10^{12}$ K
- low viscosity: $\eta/s \sim 1/4\pi$



From QCD to Dense Matter

Quantum Chromo Dynamics

Lattice gauge simulations



sign
problem



Phenomenological
nuclear force

Baryon interactions

Many-body
techniques

Equation of State for Hot Matter

Relativistic
hydrodynamics

Relativistic heavy-ion collisions

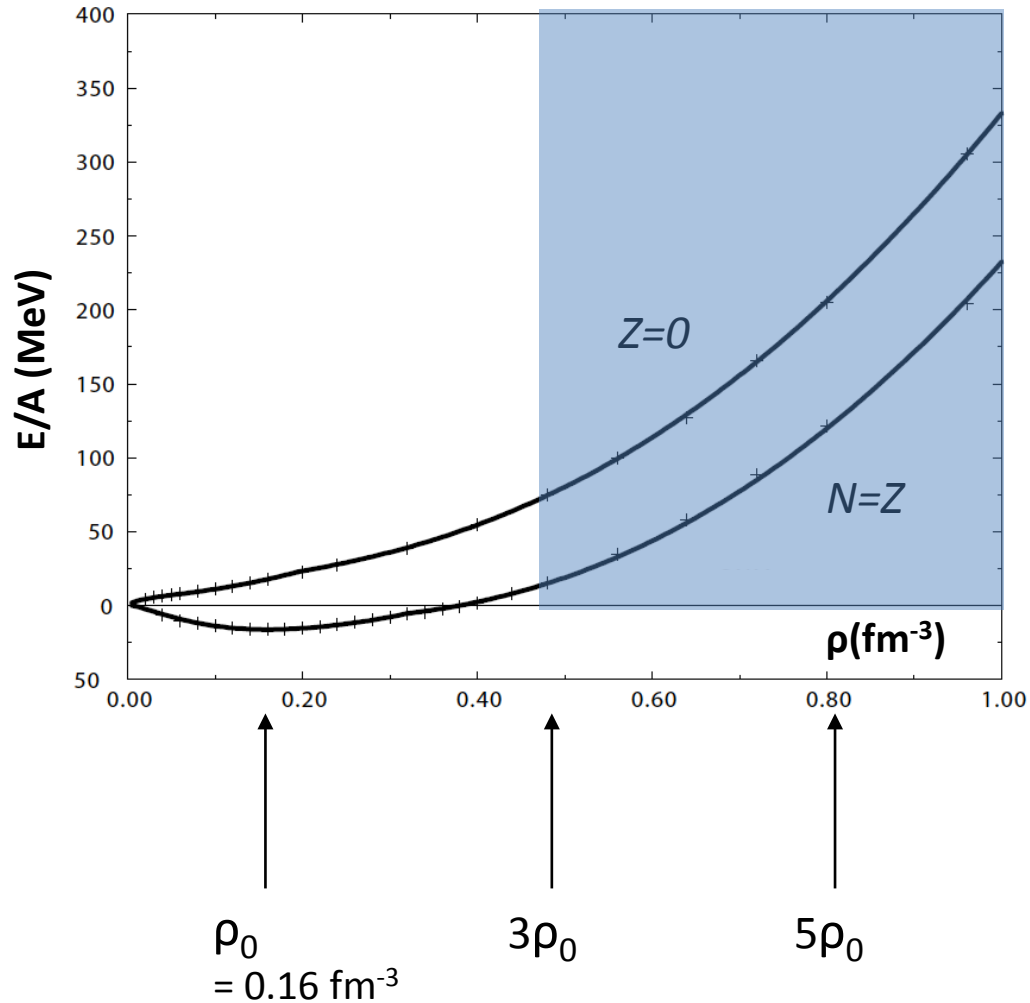
Equation of State for Dense Matter

General relativity

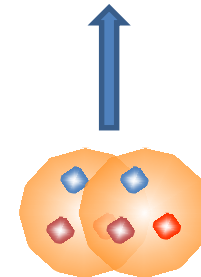
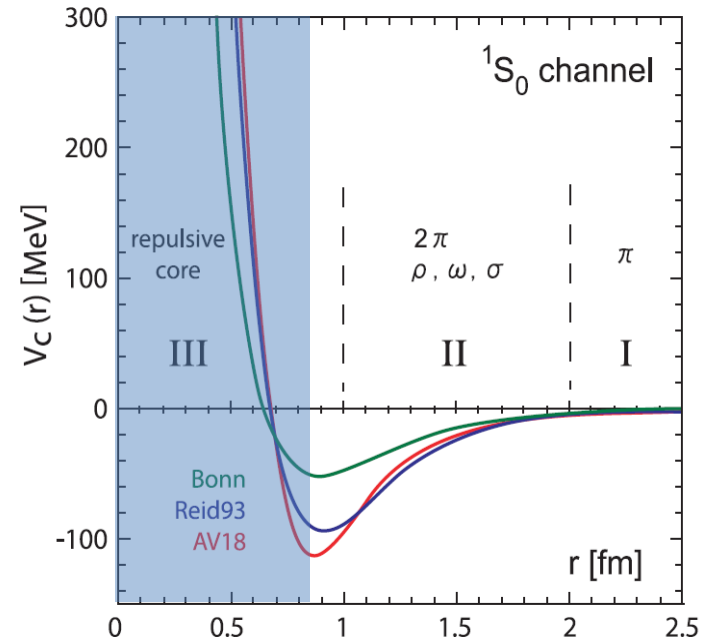
Neutron stars

Nuclear Force and dense EOS (nucleons only)

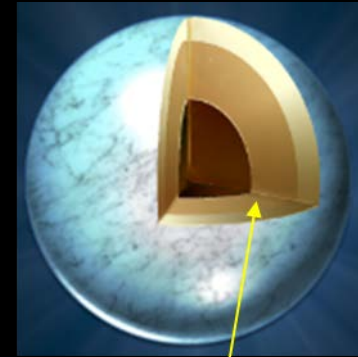
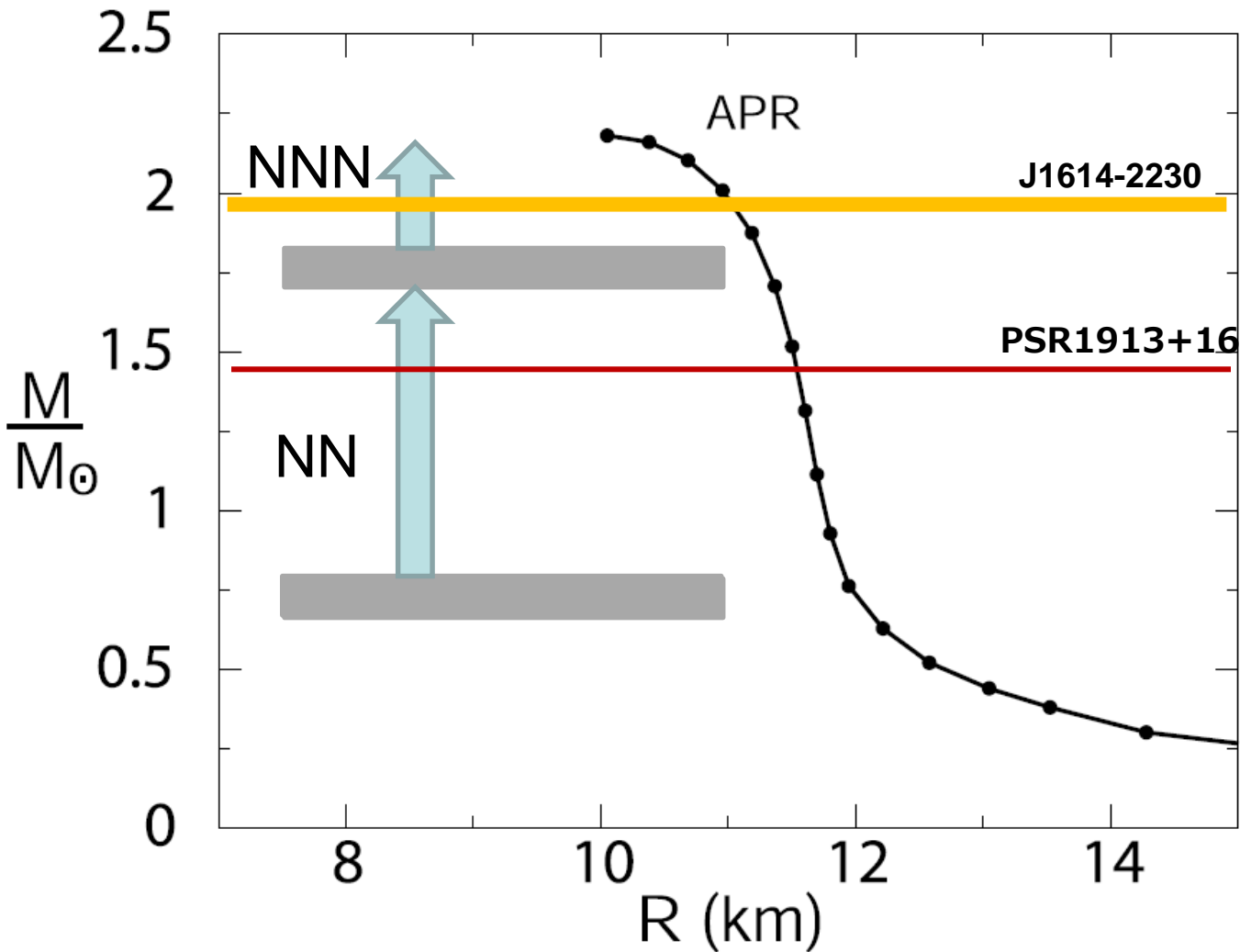
Akmal, Pandharipande & Ravenhall, PRC58 ('98)



Phenomenological nuclear force

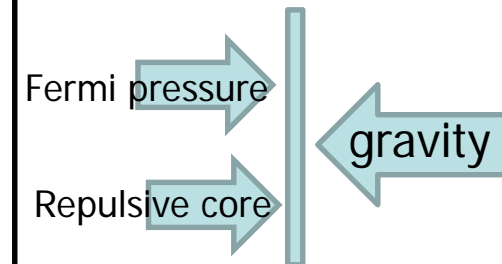


Mass-Radius relation of N_{\star} (nucleons only)

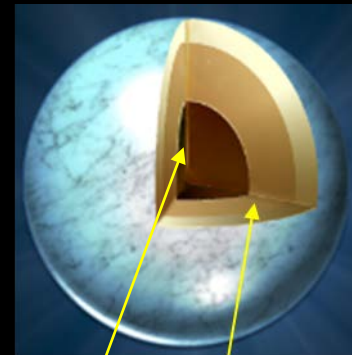
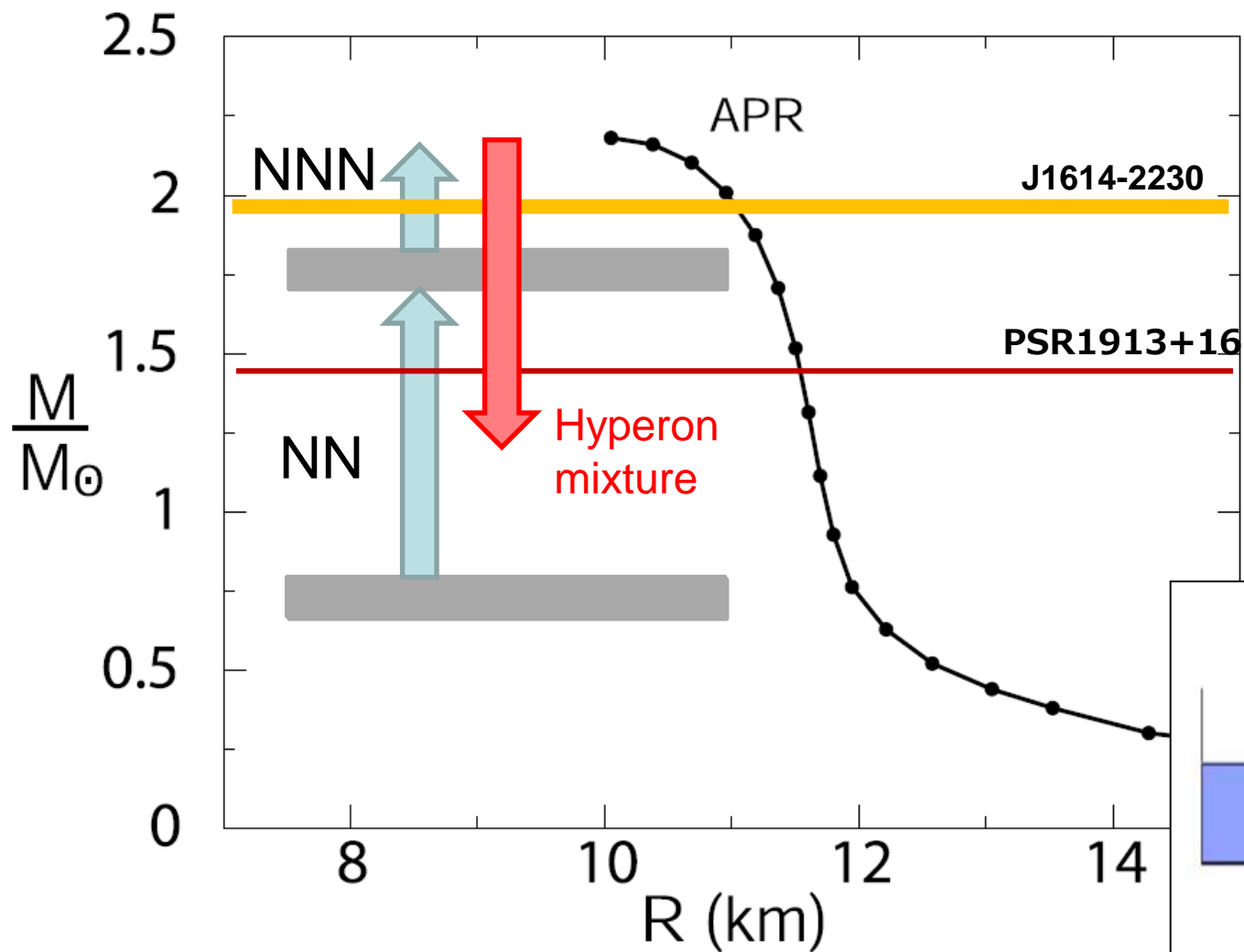


neutrons

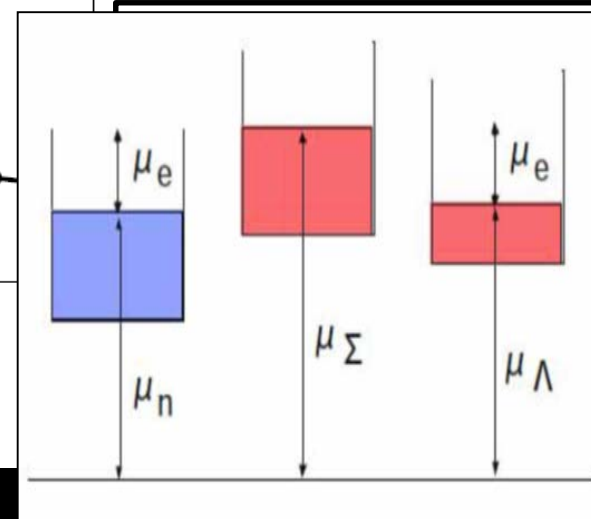
Pressure balance



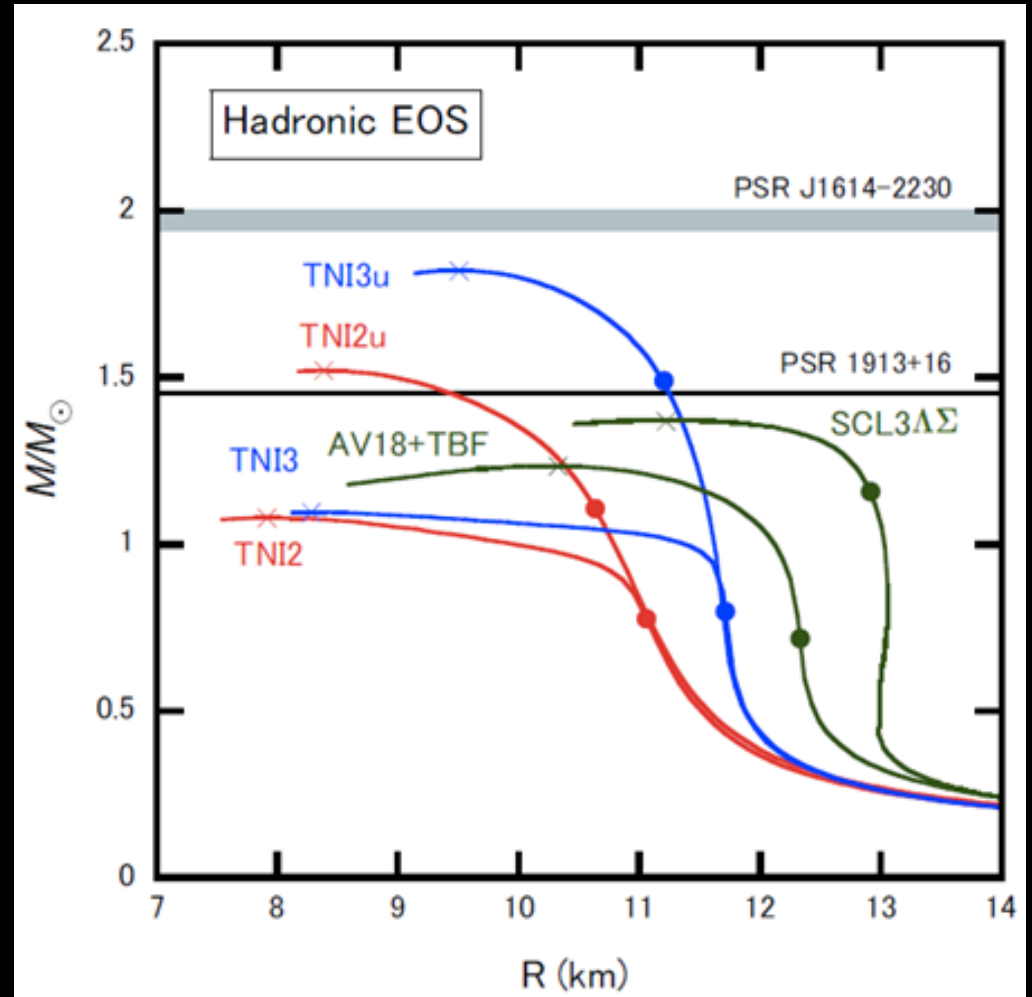
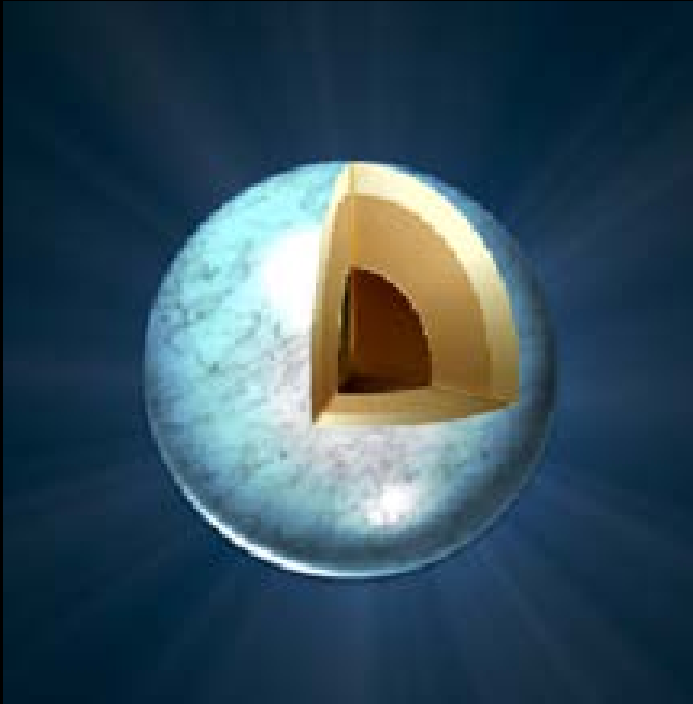
Hyperon Crisis (Takatsuka et al., 2002)



hyperons
neutrons



Hyperon Crisis

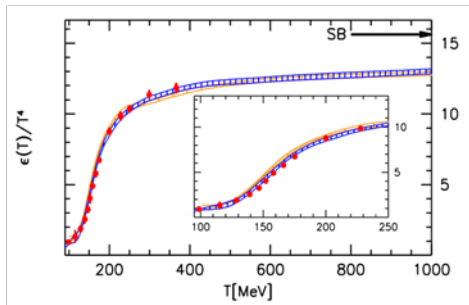


Masuda, Hatsuda & Takatsuka,
Astrophysical Journal Letters 764 (2013) 12

From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

Lattice gauge simulations



sign
problem



Lattice
QCD simulations

Baryon interactions

Many-body
techniques

Equation of State for Hot Matter

Relativistic
hydrodynamics

Relativistic heavy-ion collisions

Equation of State for Dense Matter

General relativity

Neutron stars

Precision QCD

$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} + \bar{q}\gamma^\mu(i\partial_\mu - gt^a A_\mu^a)q - m\bar{q}q$$

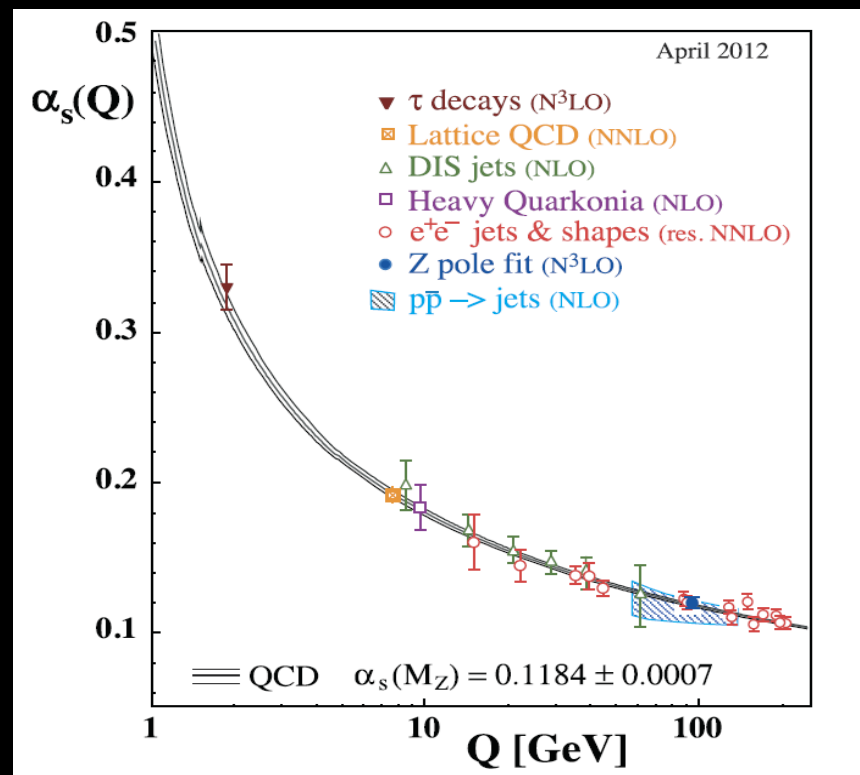
$$G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc}A_\mu^b A_\nu^c$$

Running masses: $m_q(Q)$

quark masses (from lattice QCD)	[MeV] (MS-bar @ 2GeV)
m_u	2.16 (9)(7)
m_d	4.68 (14)(7)
m_s	93.8 (2.4)

FLAG Collaboration update(July 26, 2013)
<http://itpwiki.unibe.ch/flag/>

Running coupling: $\alpha_s(Q)=g^2/4\pi$



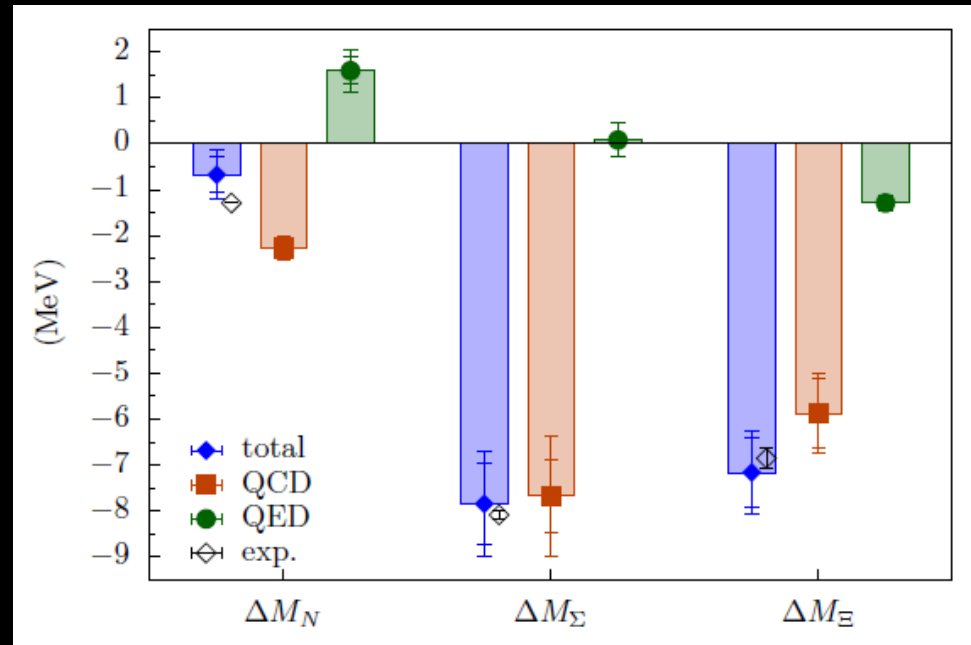
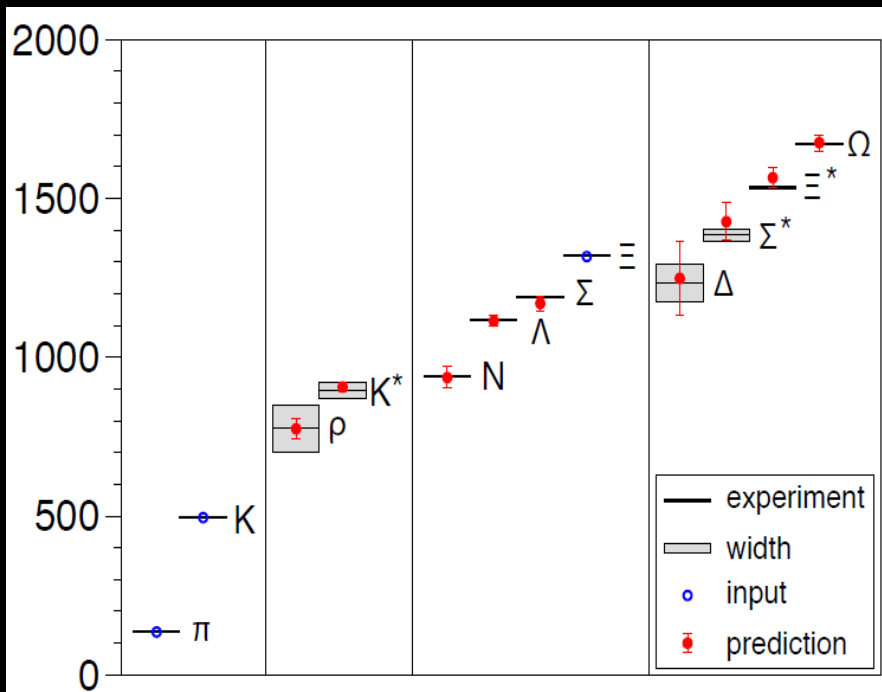
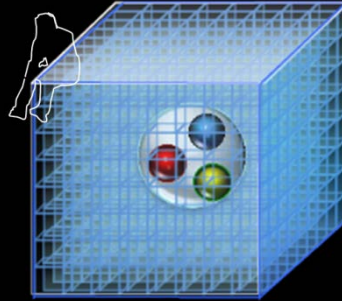
PDG (2012) <http://pdg.lbl.gov/>

Hadron masses (2008)

$$m_{\pi} > 190 \text{ MeV}$$

Hadron masses (2013)

$$m_{\pi} = 135 \text{ MeV with QED}$$



HPCI Program (FY2011-2015) Field 5: All Japan Computational Physics Collaboration

The Origin of Matter and the Universe

(particle physics – nuclear physics – astrophysics, 11 institutions)



Lattice 2015 (July)

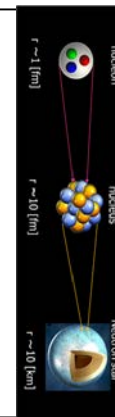
Quark Matter 2015 (Oct.)

Project 1: Baryon-Baryon interaction from lattice QCD

Project 2: Nuclear quantum many-body calculation

Project 3: Supernova explosion and black-hole formation

Project 4: First stars and galaxies



Present un-physical point simulation
for single and multi-baryons

On-going physical point simulation
for single and multi-baryons in K

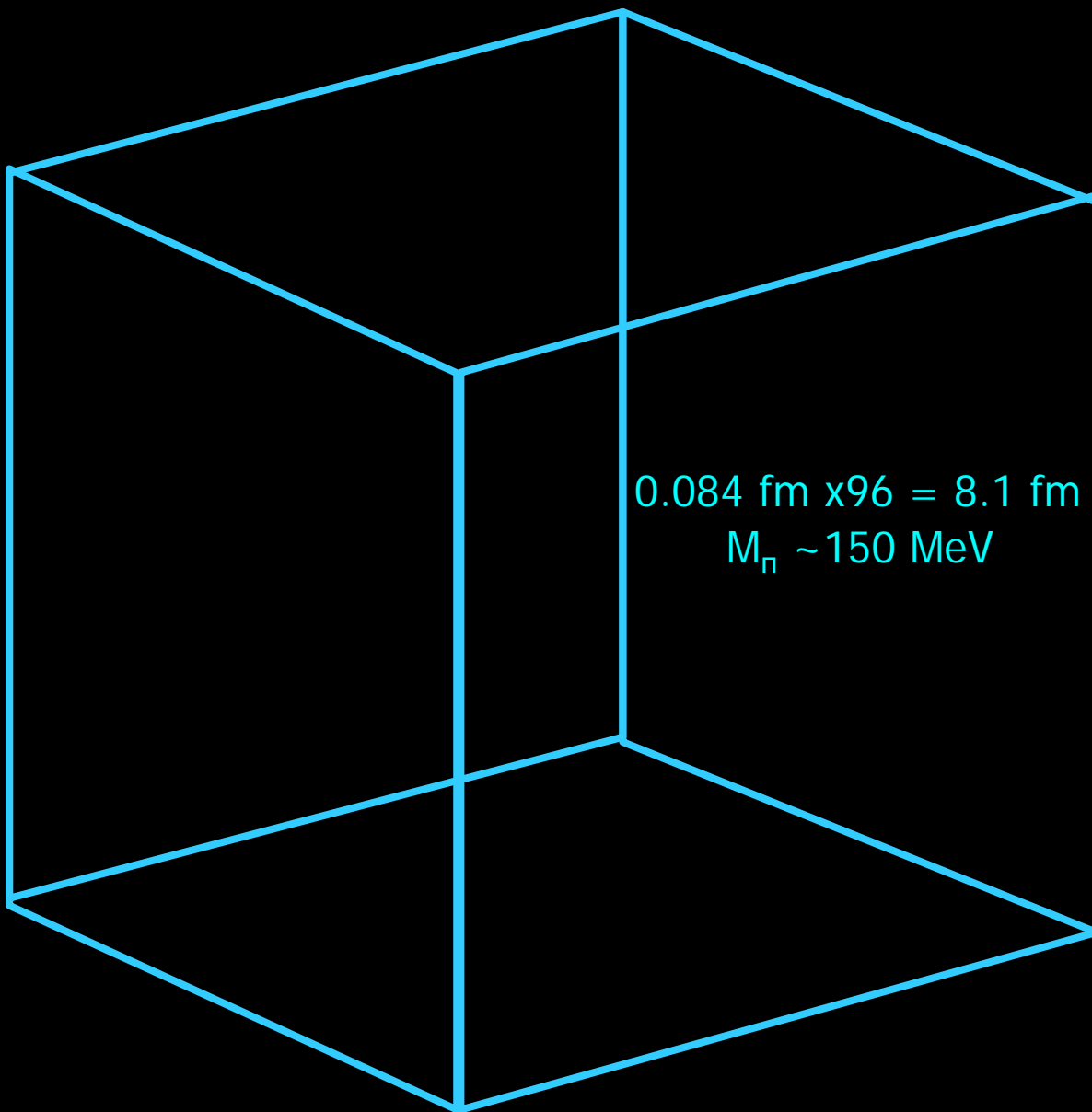
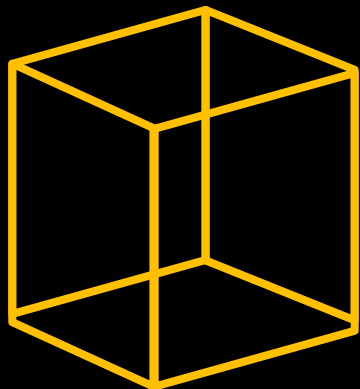
NEXT YEAR'S TALK
Stay Tuned !!



TODAY'S TALK



$0.121 \text{ fm} \times 32 = 3.9 \text{ fm}$
 $m_\pi = 350\text{-}1200 \text{ MeV}$



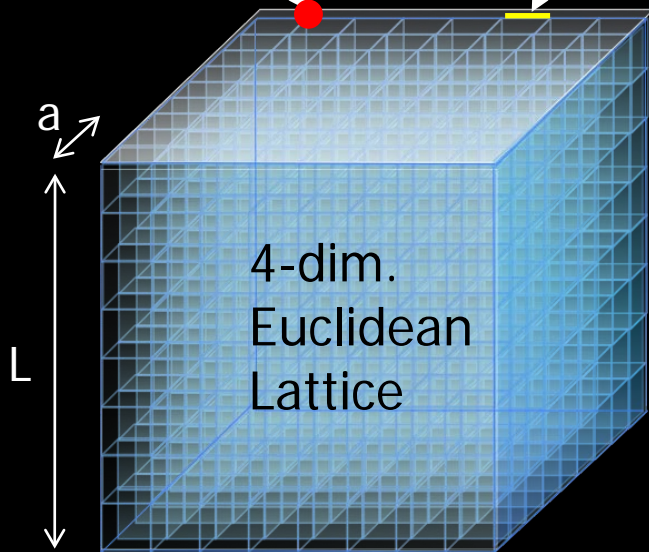
$0.084 \text{ fm} \times 96 = 8.1 \text{ fm}$
 $M_\pi \sim 150 \text{ MeV}$

格子QCD

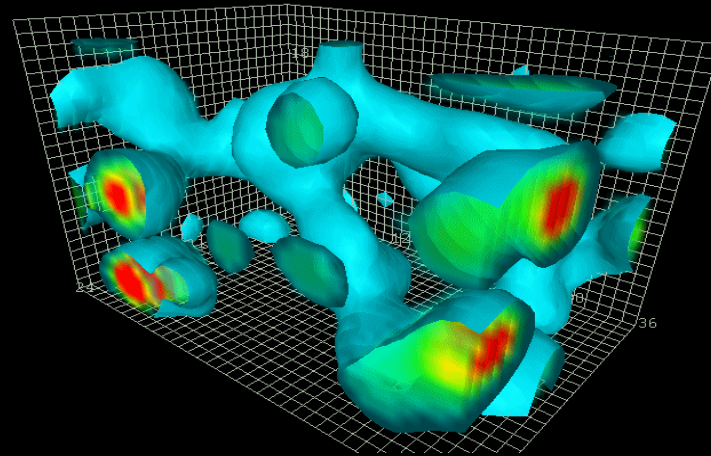


K. Wilson
(1936-2013)

quarks q on the sites
gluons $U_\mu = \exp(iagA_\mu)$ on the links



$$Z = \int [dU][dq d\bar{q}] \exp \left[- \int d\tau d^3x \mathcal{L}_E \right]$$

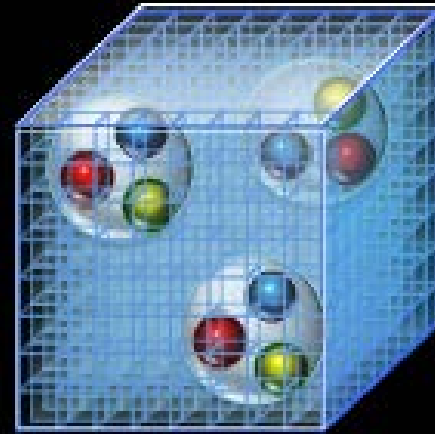
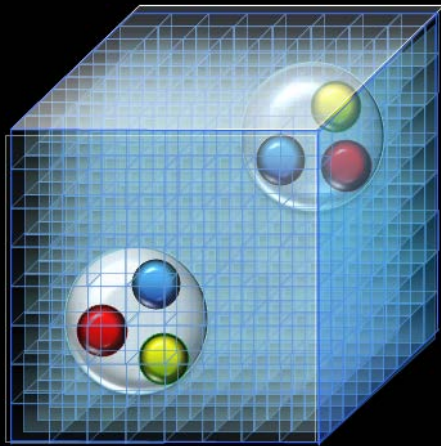


- well defined statistical system (finite a and L)
- gauge invariant
- fully non-perturbative



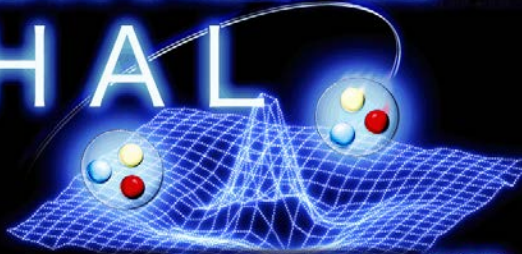
Numerical simulations

Baryon Forces from LQCD



Hadrons to Atomic nuclei

HAL



from Lattice QCD

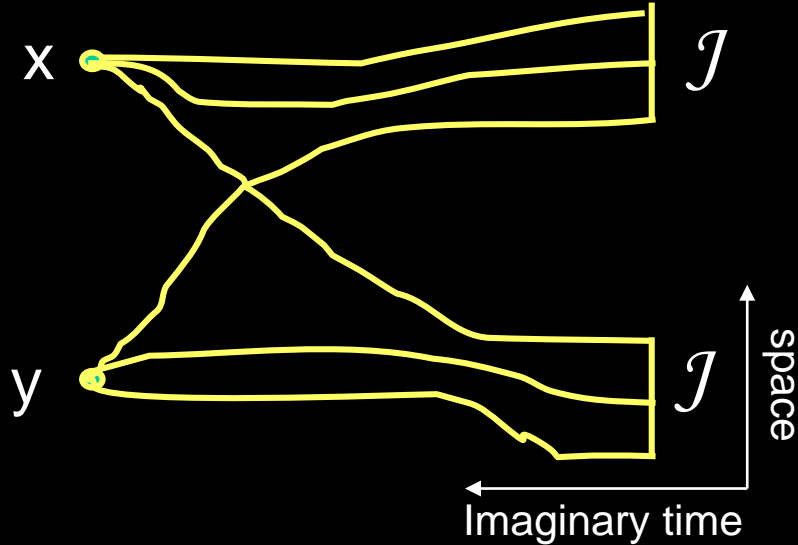
Univ. Tsukuba
Univ. Tokyo
RIKEN
Nihon Univ.
YITP (Kyoto)
RCNP (Osaka)
Birjand

T. Miyamoto, H. Nemura, K. Sasaki, M. Yamada
B. Charron
T. Doi, T. Hatsuda, Y. Ikeda, V. Krejcirik
T. Inoue
S. Aoki, T. Iritani
N. Ishii, K. Murano
F. Etminan

Review: "Lattice QCD Approach to Nuclear Physics"

HAL QCD Collaboration, Prog. Theor. Exp. Phys. 2012 (2012) 01A105

Hadronic correlations in LQCD



$$\begin{aligned} & \langle N_1(\mathbf{x}, t) N_2(\mathbf{y}, t) \mathcal{J}_1^\dagger(0) \mathcal{J}_2^\dagger(0) \rangle \\ &= \sum_n \langle 0 | N_1(\mathbf{x}) N_2(\mathbf{y}) | n \rangle a_n e^{-E_n t} \\ & \xrightarrow{t > t^*} \phi(\mathbf{r}, t) = \sum_{n < n^*} b_n \phi_n(\mathbf{r}) e^{-E_n t} \end{aligned}$$

Finite Volume Method :

$E_0(L) \rightarrow$ phase shift

Luescher, Nucl. Phys. B354 (1991) 531

HAL QCD Method

$\phi(\mathbf{r}, t) \rightarrow$ kernel \rightarrow phase shift

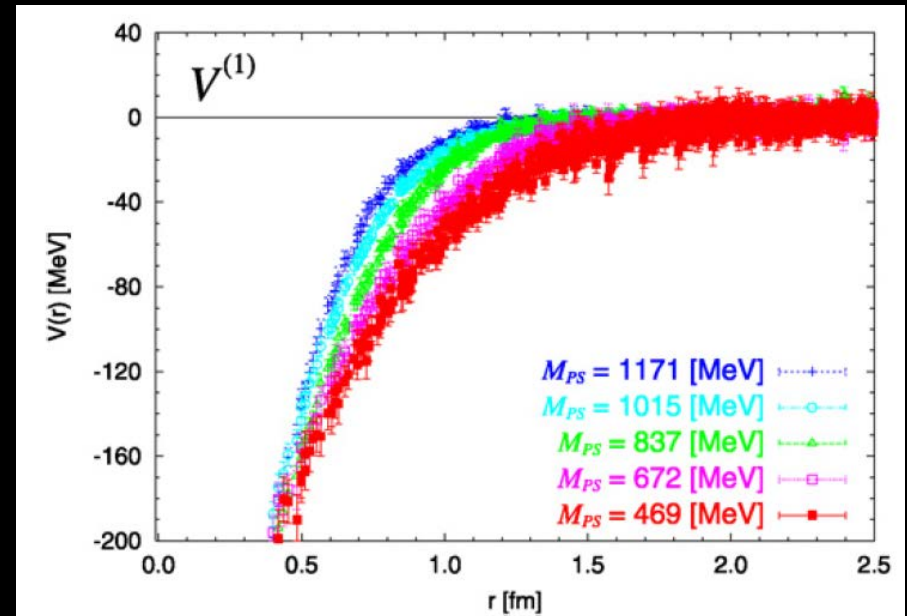
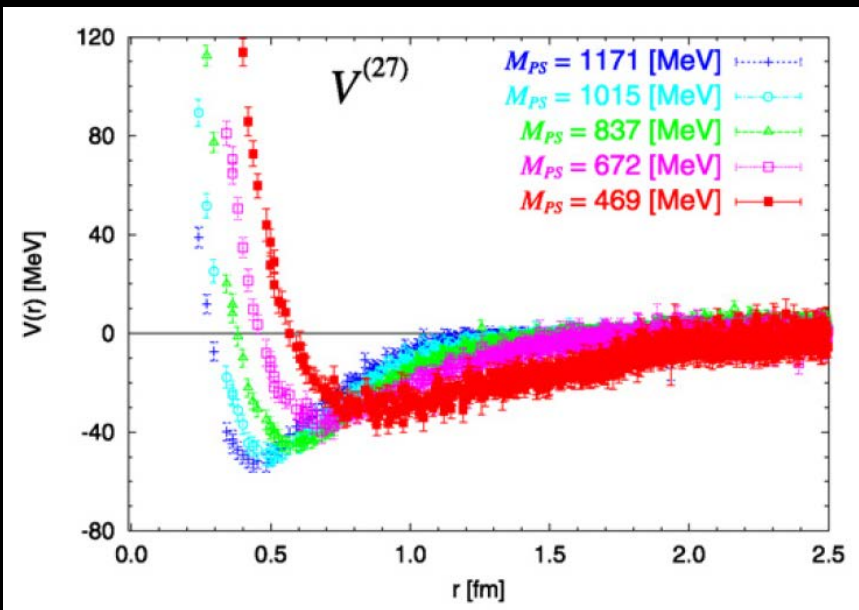
Ishii, Aoki & Hatsuda, PRL 99 (2007) 022001
 Comp. Sci. Dis. 1 (2009) 015009
 HAL QCD Coll., PLB 712 (2012) 437

BB Forces in 3-flavor QCD

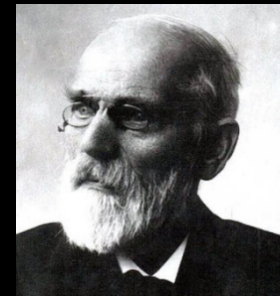
HAL QCD Coll.
Phys. Rev. Lett. 106 (2011) 162002
Nucl. Phys. A881 (2012) 28

PP (uud-uud) channel
(partial) Pauli blocking

H (uds-uds) channel
No Pauli blocking



Pauli and van der Waarls
at work !



BB Forces in 3-flavor QCD

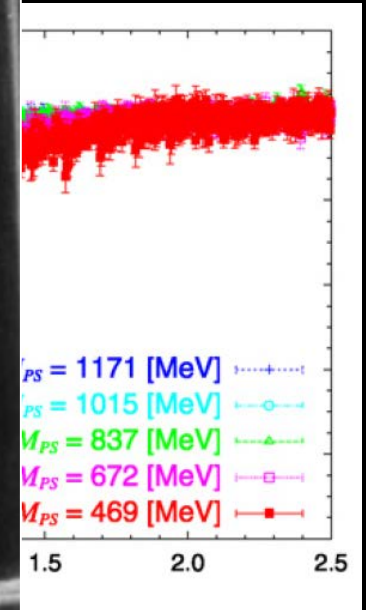
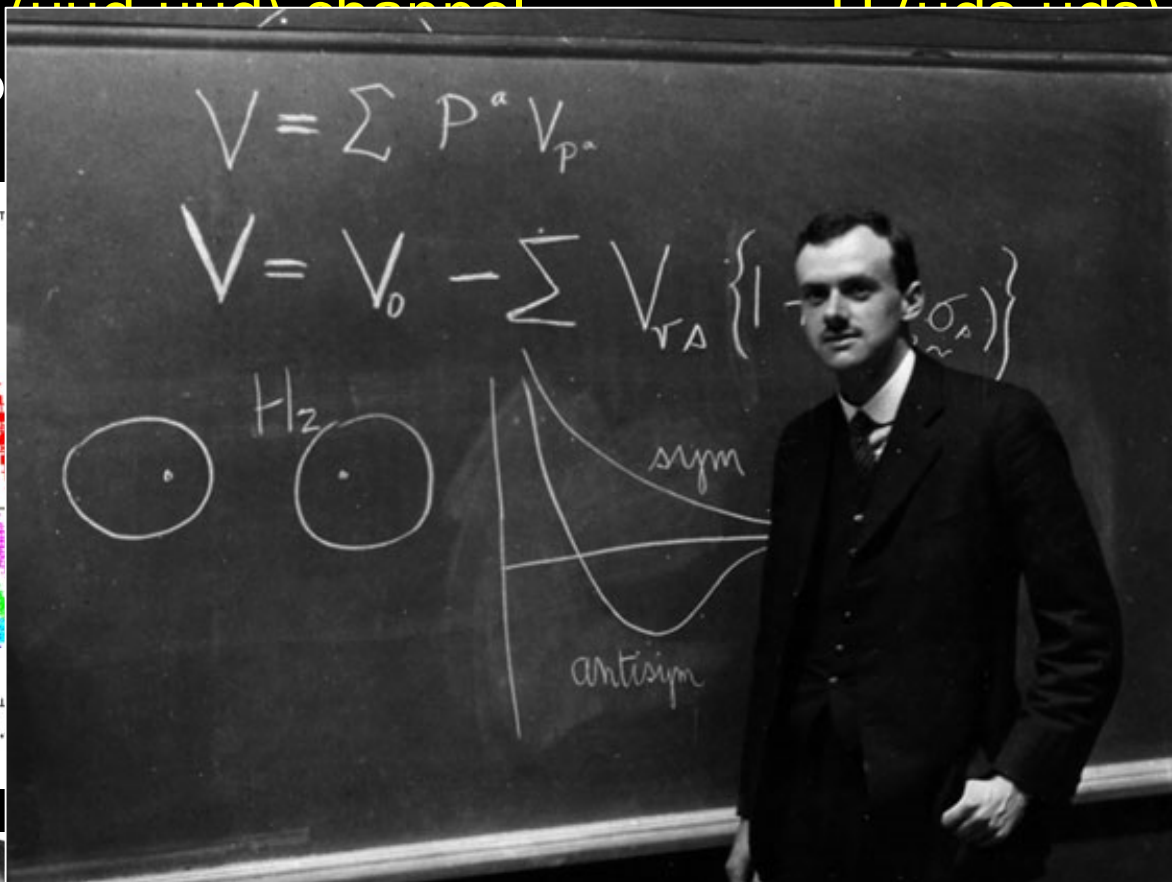
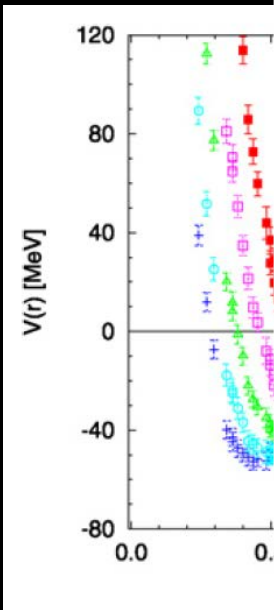
HAL QCD Coll.
Phys. Rev. Lett. 106 (2011) 162002
Nucl. Phys. A881 (2012) 28

PP (qud qud) channel

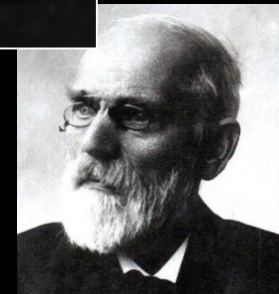
HH (uds uds) channel

(p)

locking



Pauli and van der Waarls
at work !

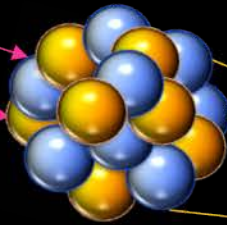


Nuclear Matter, Neutron Matter & Finite Nuclei from LQCD + BHF

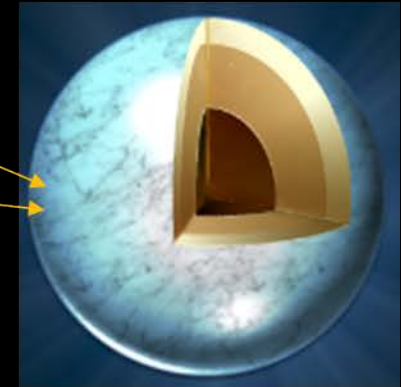
nucleon ~ 1 [fm]



nucleus ~ 10 [fm]



Neutron star ~ 10 [km]

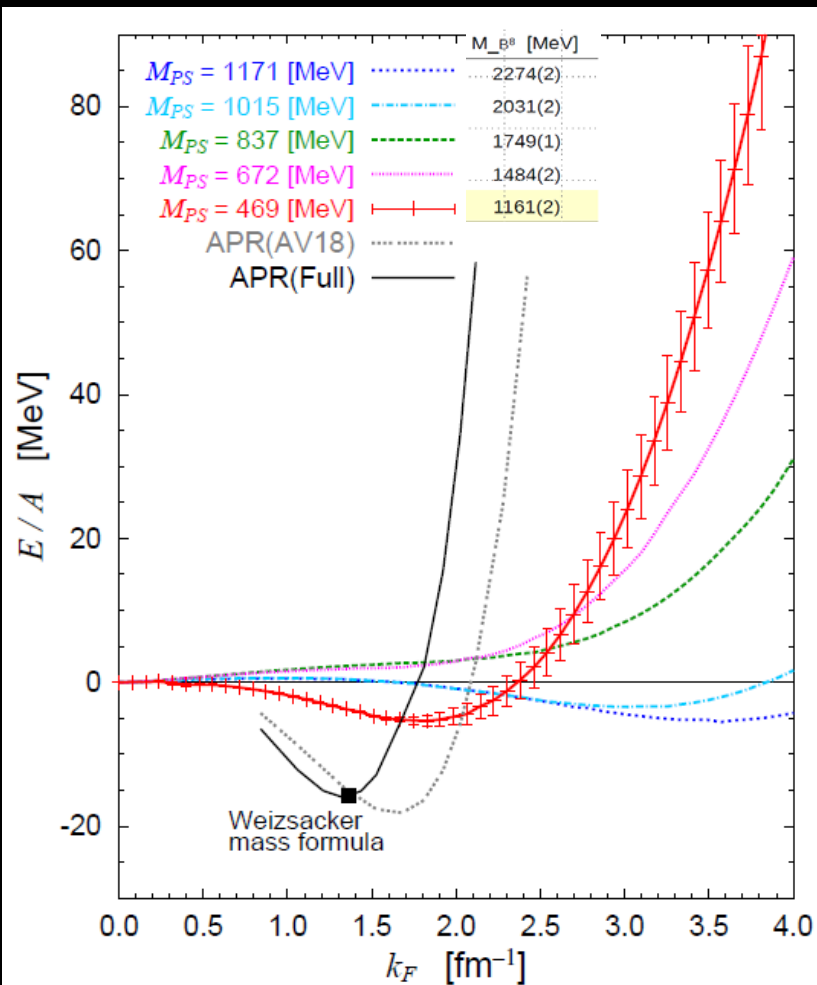


Nuclear EOS from Lattice NN force + BHF calculation

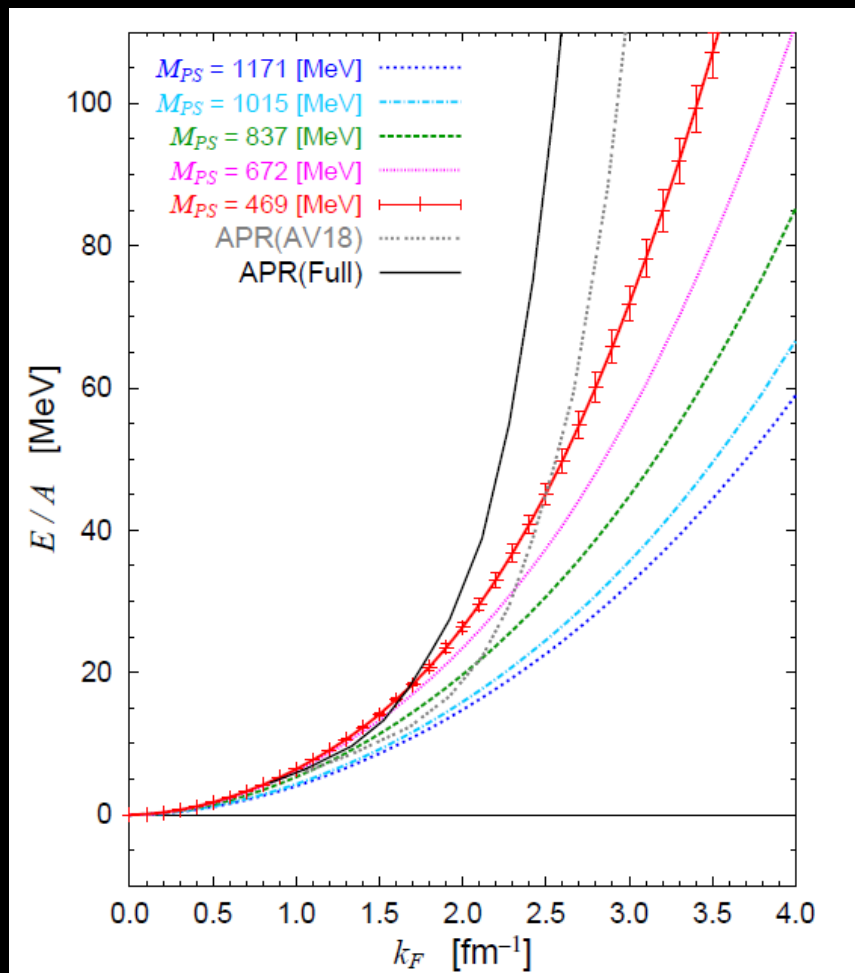
(NN force: 1S_0 , 3S_1 , 3D_1 channels only)

HAL QCD Coll., Phys. Rev. Lett. 111 (2013) 112503

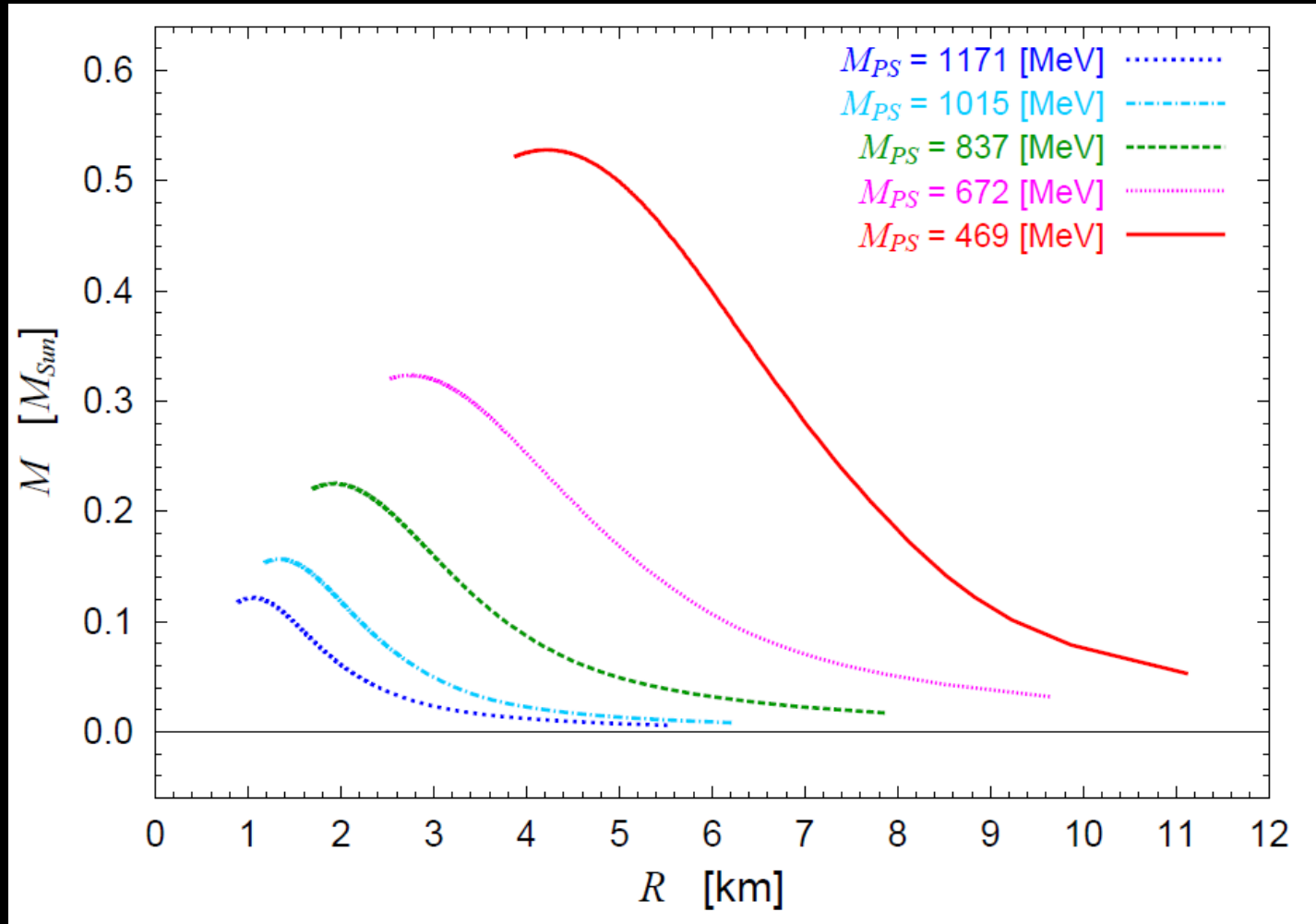
Nuclear Matter



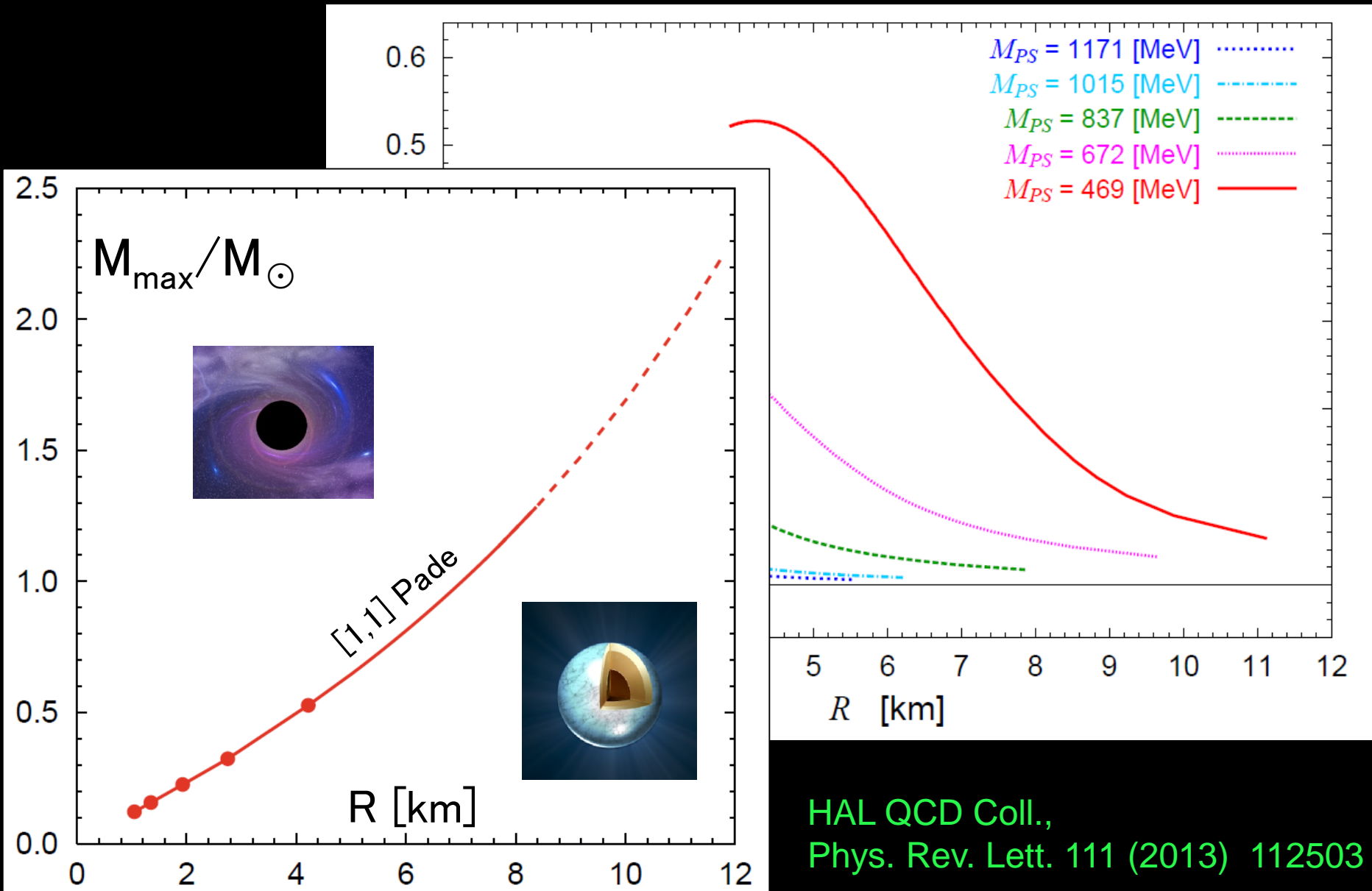
Neutron Matter



Neutron Star from “Lattice EOS”



Neutron Star from "Lattice EOS"



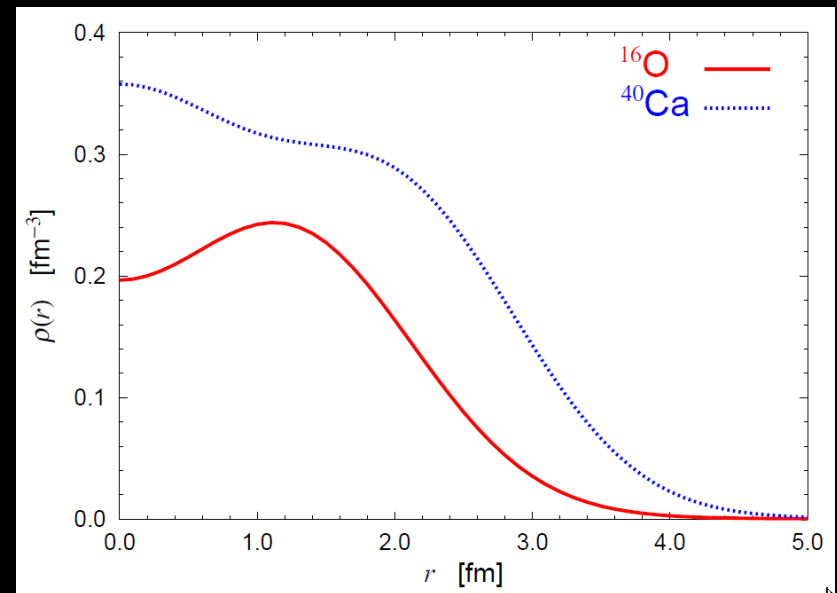
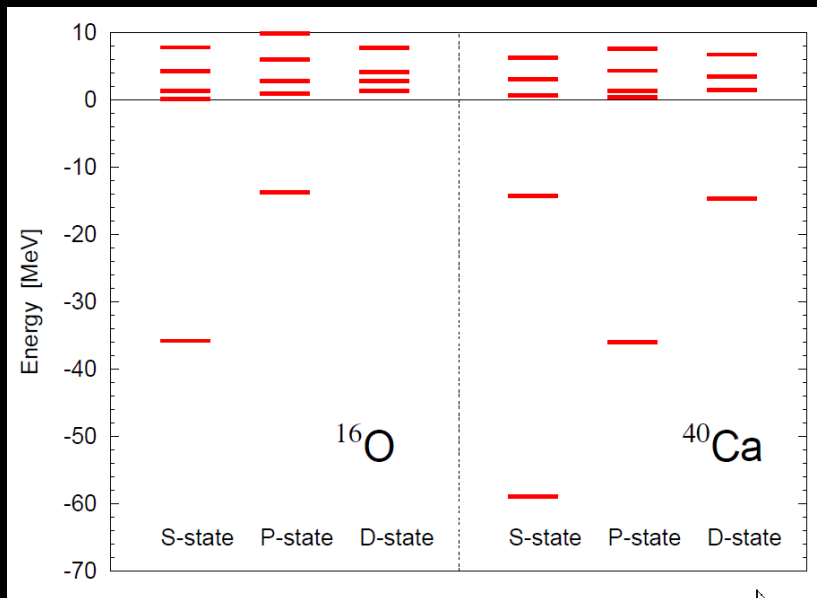
HAL QCD Coll.,
Phys. Rev. Lett. 111 (2013) 112503

Finite Nuclei from Lattice NN force + BHF calculation

(NN force: 1S_0 , 3S_1 , 3D_1 channels only)

Inoue et al. [HAL QCD Coll.], arXive 1408.4892

Bound nuclei start to appear from $m_\pi = 470$ MeV

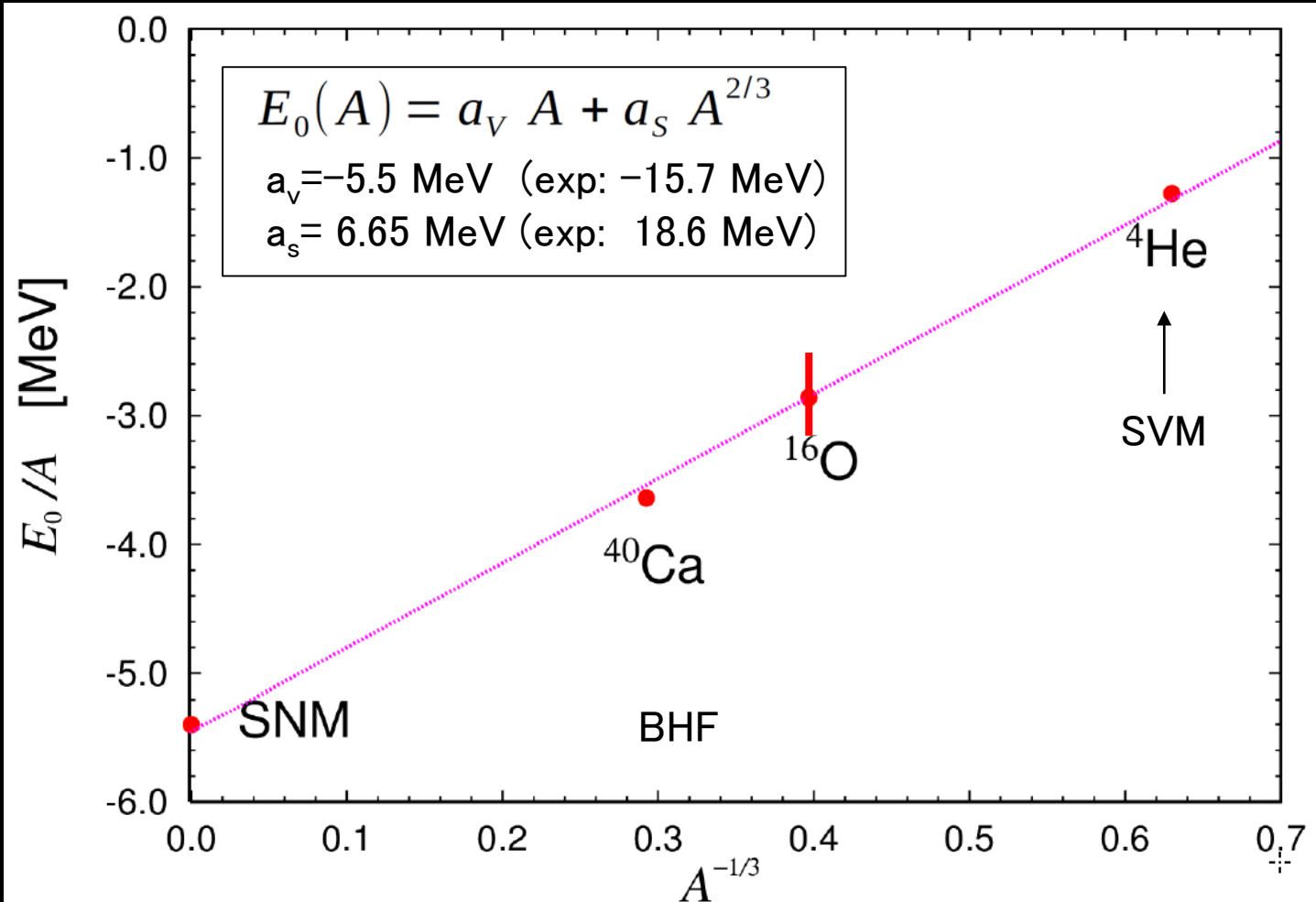


	Single particle level				Total energy		Radius
	$1S$	$1P$	$2S$	$1D$	E_0	E_0/A	$\sqrt{\langle r^2 \rangle}$
^{16}O	-35.8	-13.8			-34.7	-2.17	2.35
^{40}Ca	-59.0	-36.0	-14.7	-14.3	-112.7	-2.82	2.78

Nuclear Binding Energy from Lattice NN Force

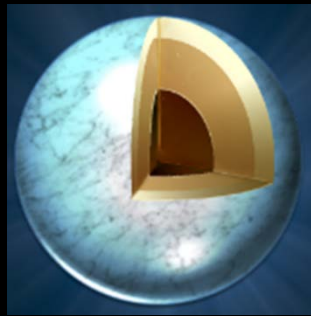
Inoue et al. [HAL QCD Coll.], arXiv 1408.4892

Bethe-Weizacker behavior at $m_\pi = 470$ MeV

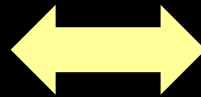


冷却原子を用いた 中性子星の実験室シミュレーション？

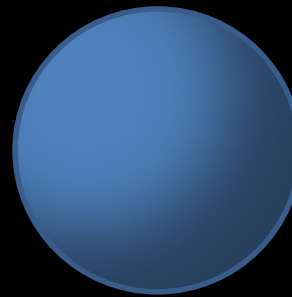
重力



~10km



MOT

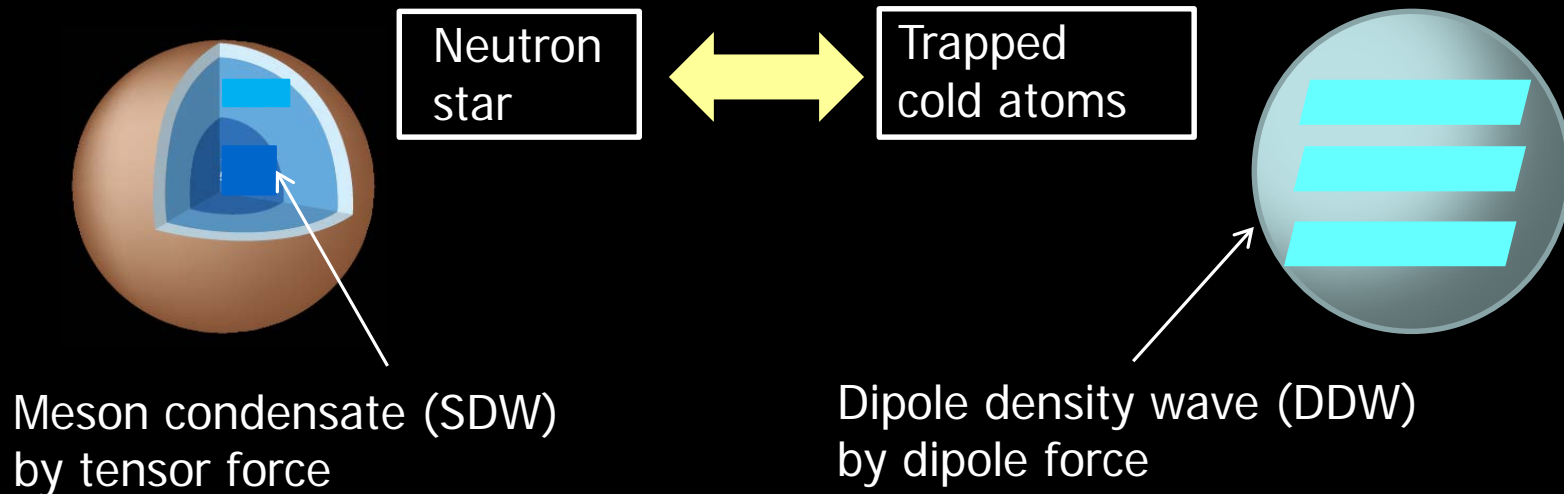


~1 mm

- ハドロン相とクォーク相のクロスオーバー
⇔ 冷却 ボース原子-冷却フェルミ原子混合気体
Maeda, Baym & Hatsuda, Phys. Rev. Lett. 103 (2009) 085301
- π 中間子凝縮 ⇔ 冷却双極子原子(分子)気体
Maeda, Baym & Hatsuda, Phys. Rev. A 87 (2013) 021604(R)

meson-condensation in ultracold dipolar atoms

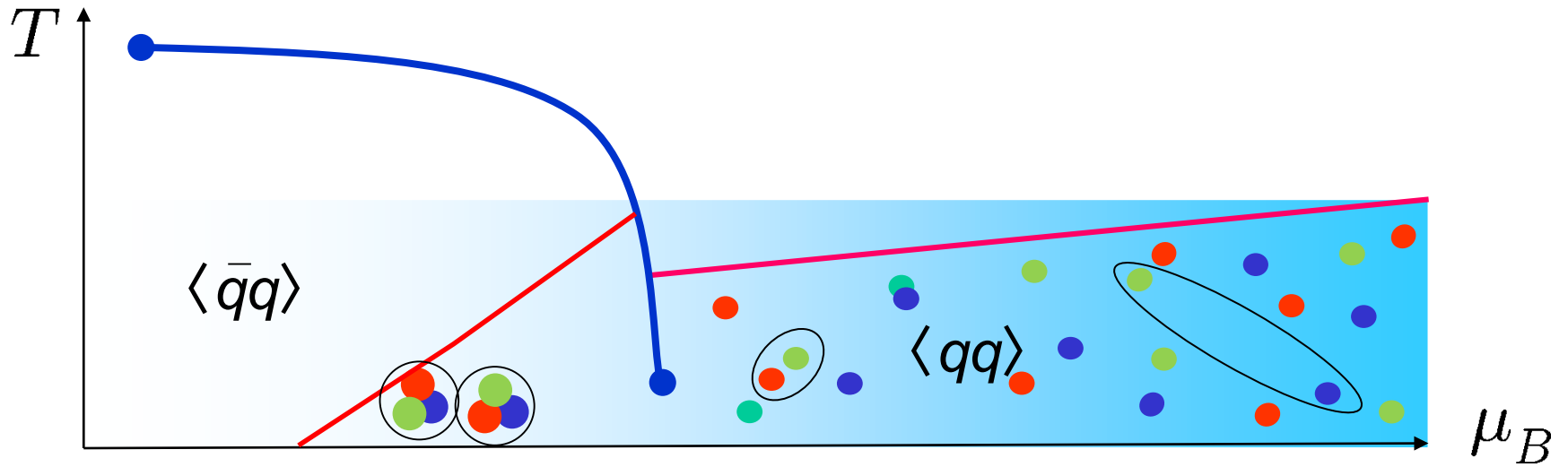
Maeda, Baym, Hatsuda (2012)



$$U_{dd} = -\frac{3(\vec{\mu}_1 \cdot \hat{r})(\vec{\mu}_2 \cdot \hat{r}) - \vec{\mu}_1 \cdot \vec{\mu}_2}{r^3} - \frac{8\pi}{3} \vec{\mu}_1 \cdot \vec{\mu}_2 \delta(\vec{r})$$

neutron matter	atomic dipolars
neutron stars	atomic gases(e.g. ^{163}Dy , ^{161}Dy)
neutrons	fermionic dipolars
spin	pseudo-spin (hyperfine states)
neutral vector meson (ρ^0)	photon
tensor-force potential	dipole-dipole interaction potential
meson condensation	spin/density wave

Hadron-Quark Phase Transition and the role of "Diquarks"



Nuclear superfluid



Fermion+Diquark



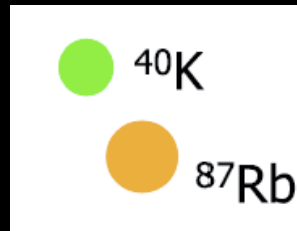
Diquark superfluid



Induced superfluid



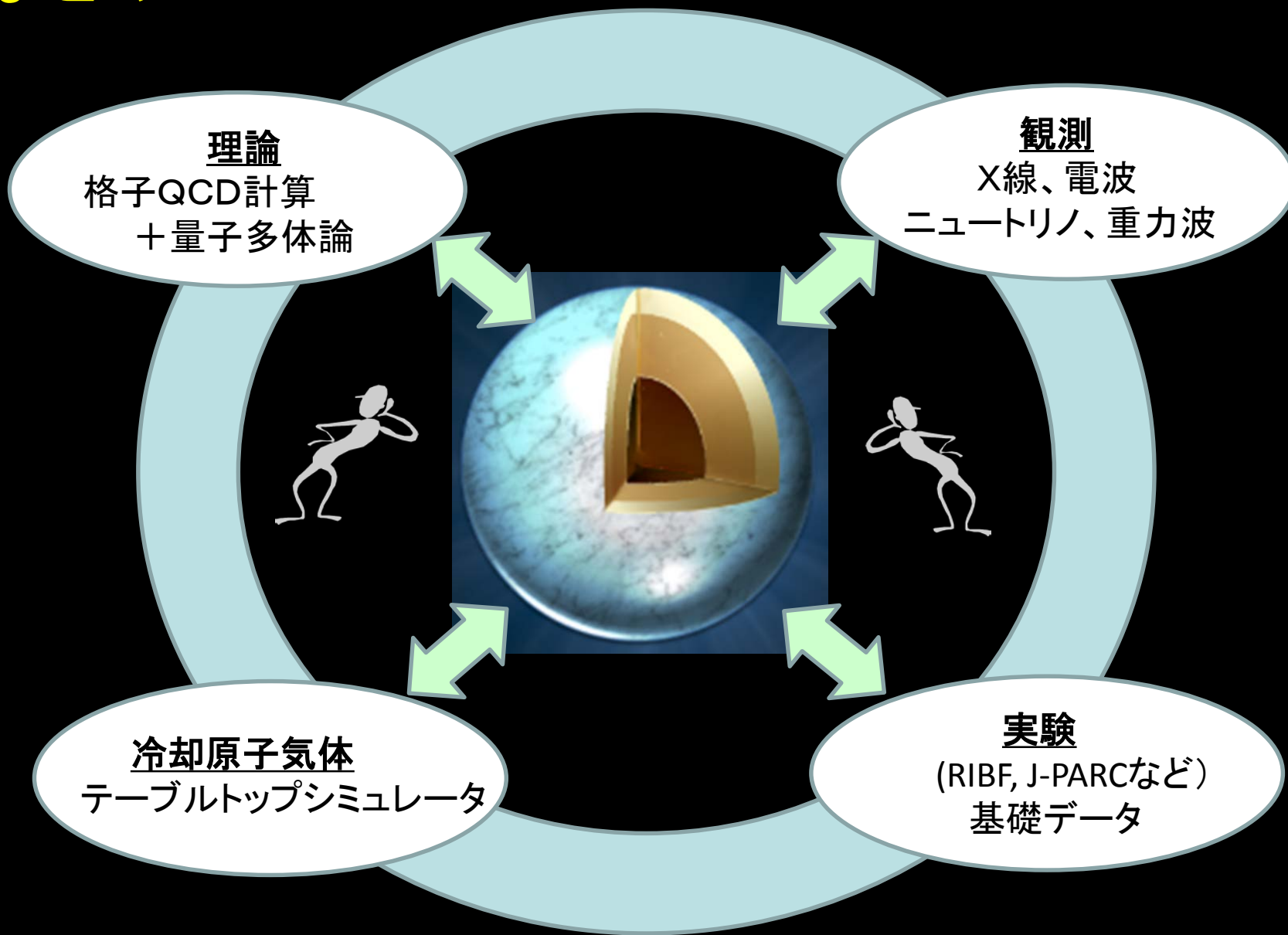
Fermi-Bose mixture



$$a_{NN}^{\text{Born}} = -\frac{m_N}{2m_R} a_{bf}$$

Maeda, Baym & Hatsuda,
Phys. Rev. Lett. 103 ('09)

まとめ



Present un-physical point simulation
for single and multi-baryons

On-going physical point simulation
for single and multi-baryons in K

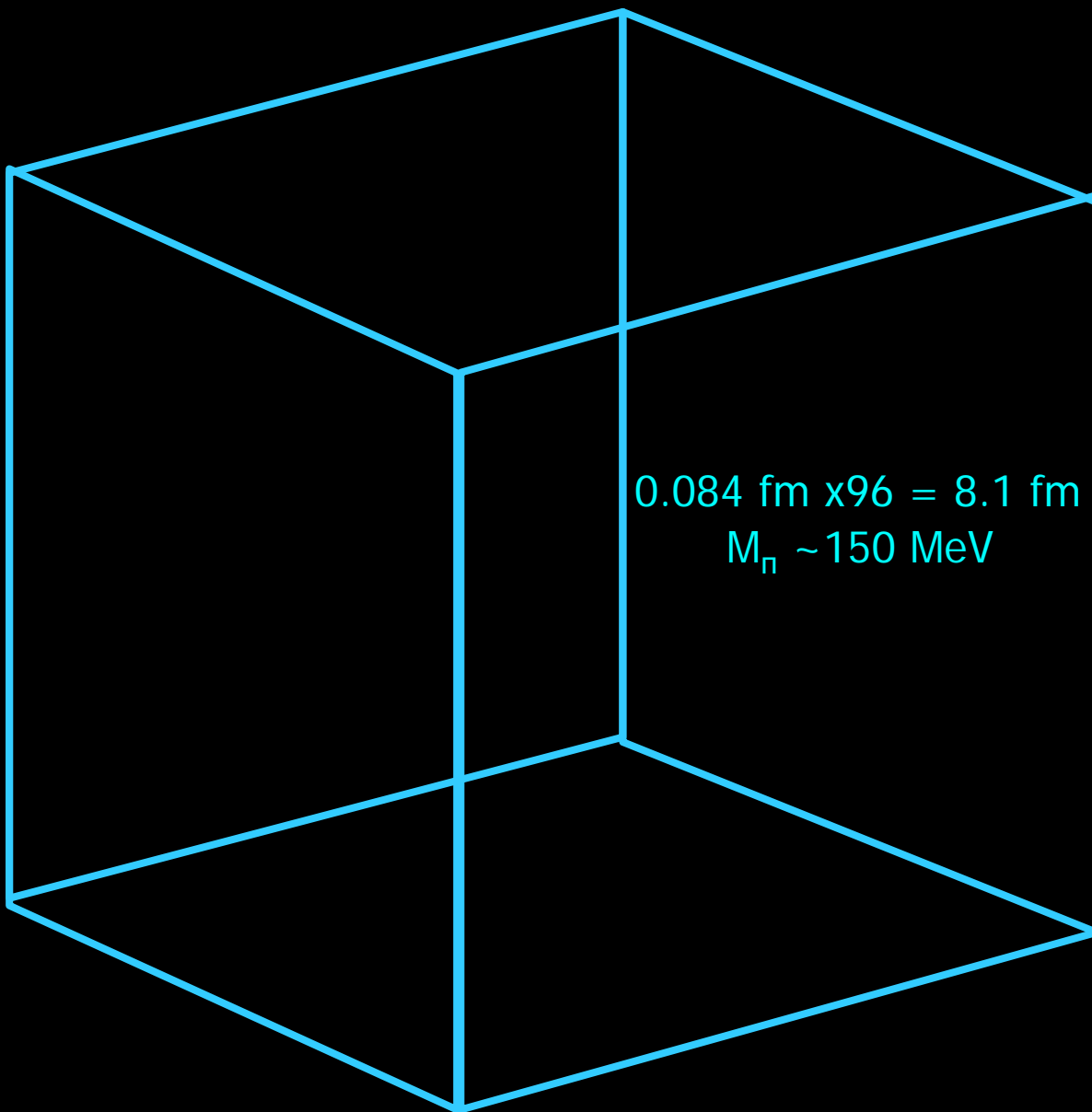
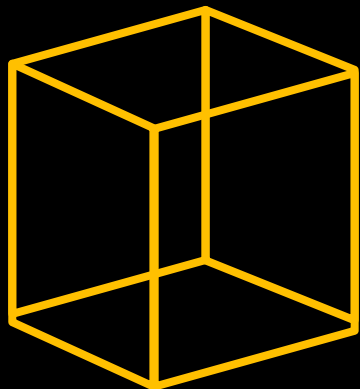
NEXT YEAR'S TALK
Stay Tuned !!



TODAY'S TALK



$0.121 \text{ fm} \times 32 = 3.9 \text{ fm}$
 $m_\pi = 350\text{-}1200 \text{ MeV}$



$0.084 \text{ fm} \times 96 = 8.1 \text{ fm}$
 $M_\pi \sim 150 \text{ MeV}$

END