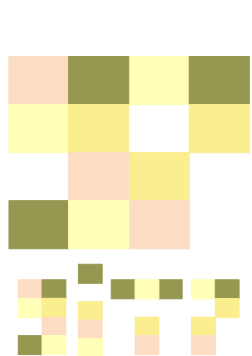


京を用いた連星磁場中性子星合体の数値 相対論シミュレーション

木内建太 (YITP)

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久徳浩太郎 (UWM), 関口雄一郎 (YITP), 柴田大
(YITP), 和田智秀 (筑波技術大)



YUKAWA INSTITUTE FOR
THEORETICAL PHYSICS



Motivation

1. Gravitational waves = ripples of the space-time

- ▶ Verification of GR
- ▶ The EOS of neutron star matter
- ▶ The central engine of SGRB
- ▶ ~10 events / yr for KAGRA

GW detectors



2. A possible site of the r-process synthesis

A significant amount of neutron star matter could be ejected from BNS mergers ($M_{\text{eje}} \approx 10^{-4}-10^{-2}M_{\odot}$, Hotokezaka et al. 13)

⇒ Nuclear synthesis in the ejecta (Lattimer & Schramm 76)

- ▶ Radio active decay of the r-process elements
- ▶ Electromagnetic counterpart = kilonova (Li-Paczynski 98, Kulkarni 05, Metzger et al. 10, Kasen et al. 13, Barnes-Kasen 13, Tanaka-Hotokezaka 13, Hotokezaka et al. 13, Takami-Nozawa-loka 14)
- ▶ NIR excess in afterglow of GRB130603B (Berger et al.13, Tanvir et al. 13)

A step toward physically reliable model of BNS mergers

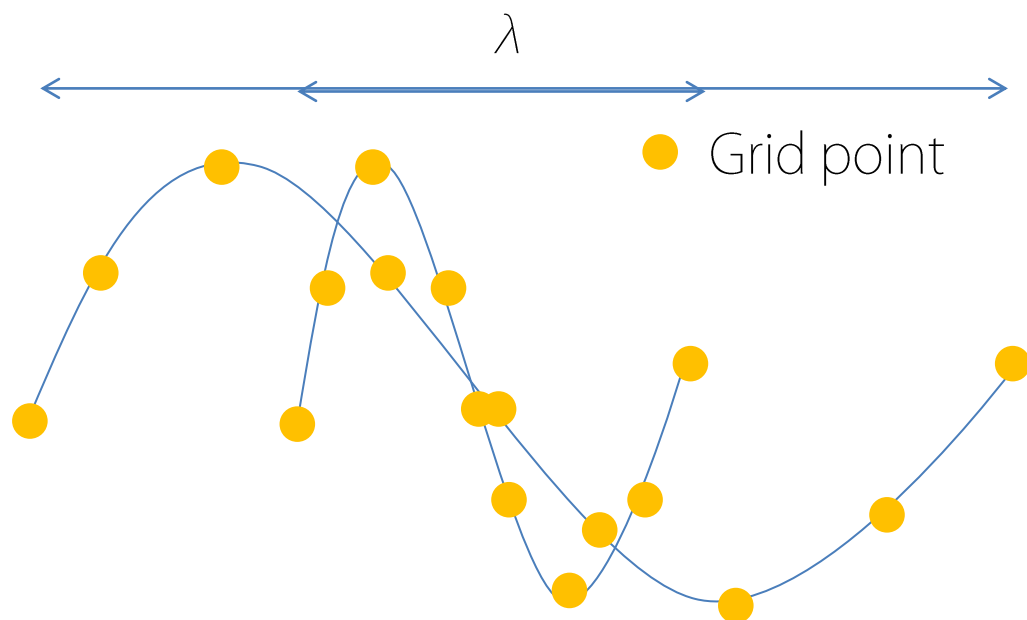
Kyoto NR group approaches from two directions;

- ▶ MHD (KK)
- ▶ Microphysics

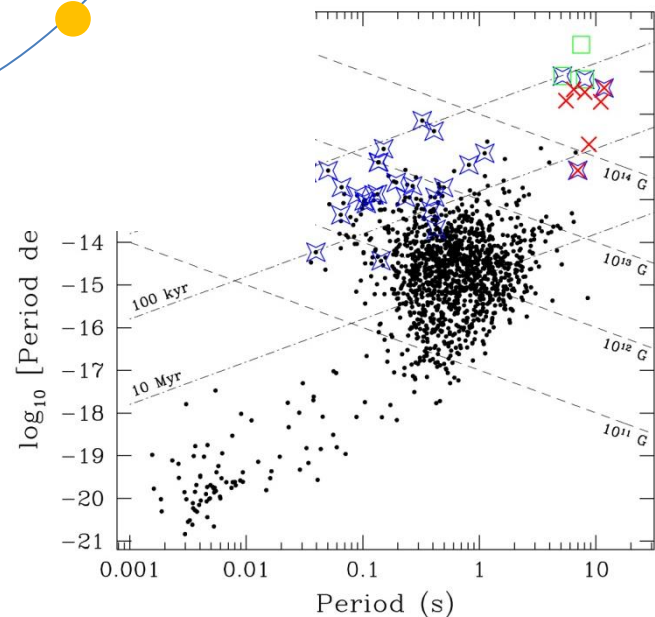
Are B-fields
▶ Observed

The MHD in
short-wavelength

⇒ Necessary
simulation which covers a large dynamical
range of $O(10)\text{km}-O(1,000)\text{km}$.



Diagram



Japanese supercomputer K @ AICS



▶ Total peak efficiency is 10.6 PFLOPS (663,552 cores)

This study is one of the main subject of the HPCI strategic program field 5.

Numerical Relativity simulation of magnetized BNS mergers

- ▶ High resolution $\Delta x=70\text{m}$ (16,384 cores on K)
- ▶ Medium resolution $\Delta x=110\text{m}$ (10,976 cores on K)
- ▶ Low resolution $\Delta x=150\text{m}$ (XC30, FX10 etc.)

c.f. Radii of NS $\sim 10\text{km}$, the highest resolution of the previous work is $\Delta x \approx 180\text{m}$ (Liu et al. 08, Giacomazzo et al. 11, Anderson et al. 08)

Nested grid \Rightarrow Finest box = 70km^3 , Coarser grid = 4480km^3 ($N \sim 10^9$), a long term simulation of about 100 ms

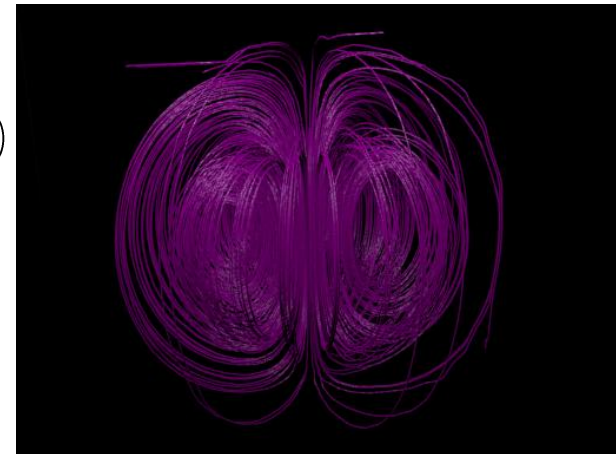
Fiducial model

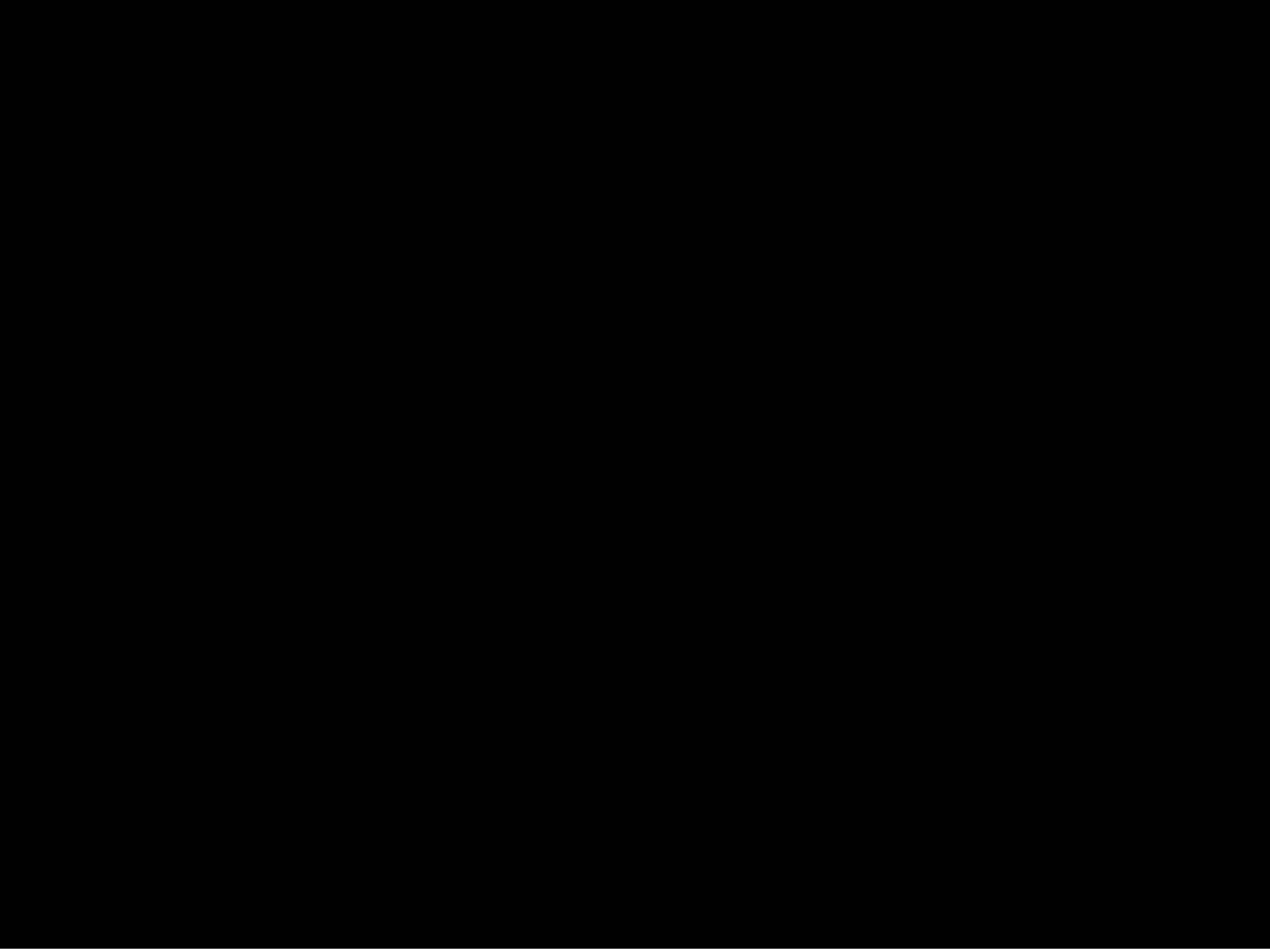
EOS : H4 (Gledenning and Moszkoski 91) ($M_{\text{max}} \approx 2.03M_{\odot}$)

Mass : 1.4-1.4 M_{\odot}

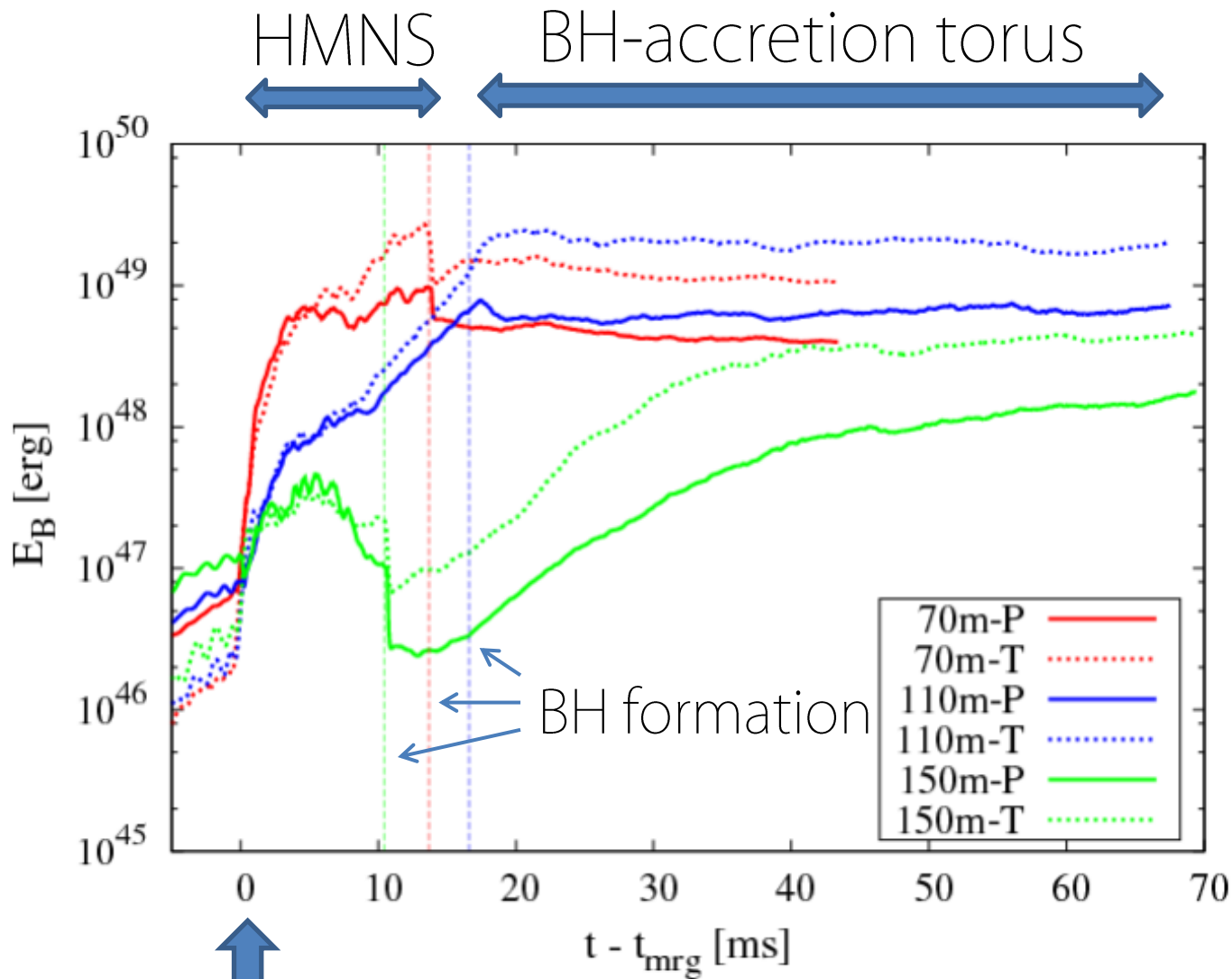
B-field : 10^{15}G

Magnetic field lines of NS





Evolution of the magnetic field energy

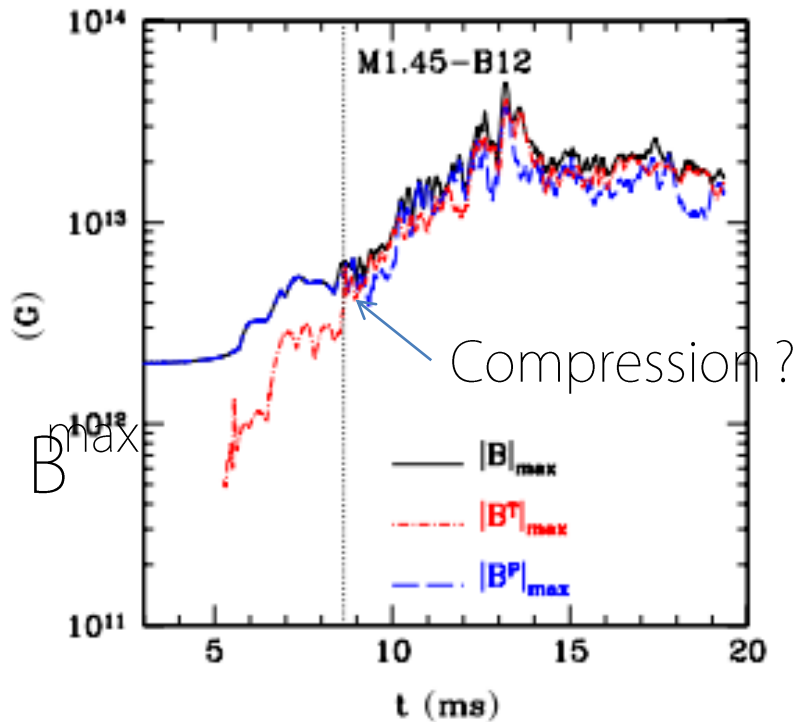


P = Poloidal comp.
T = Toroidal comp.

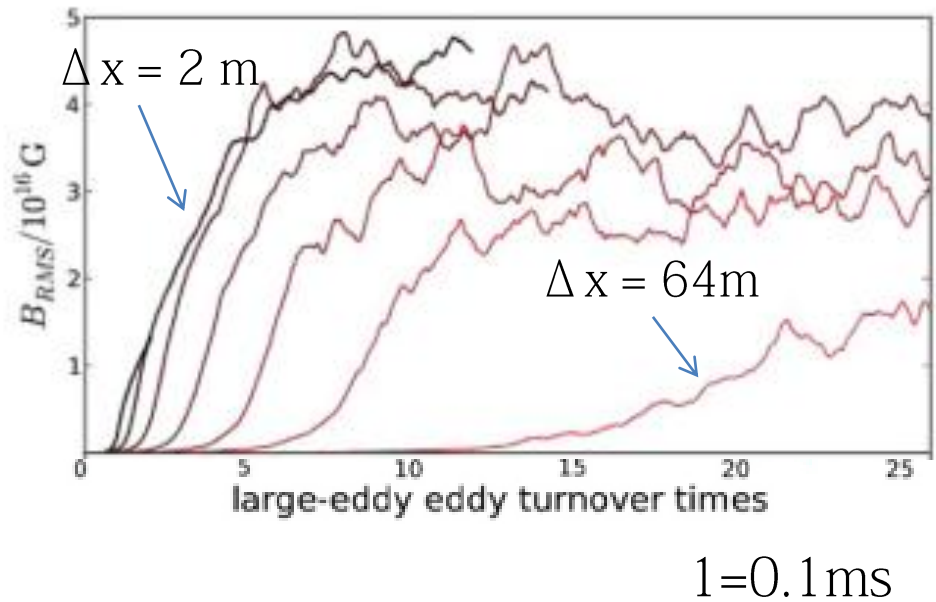
Amplification via KH vortices @ the merger (Rasio and Shapiro 99)

GRMHD by AEI (Giacomazzo et al. 11)

Local box simulation (Zrake and MacFadyen 13, Obergaulinger et al. 10)



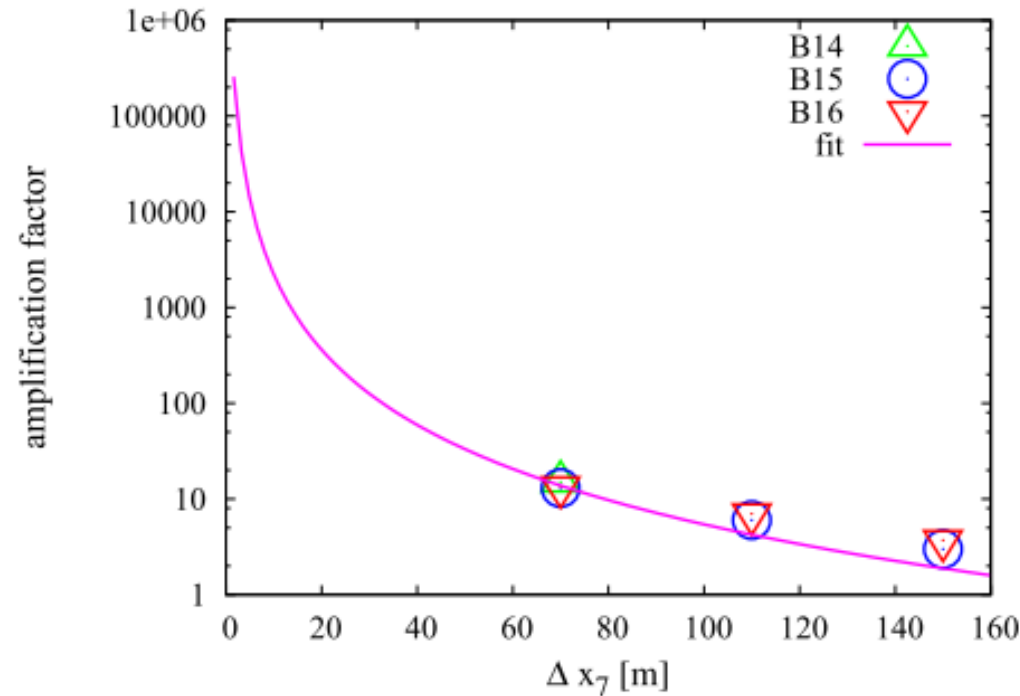
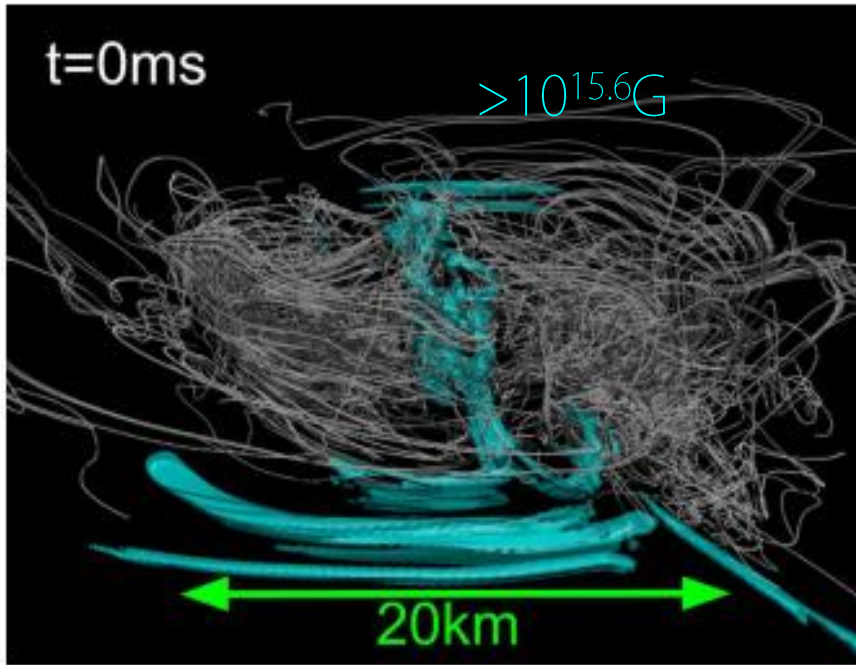
Time evolution of $\langle B \rangle$



Can really the KH vortices amplify the B-fields ?

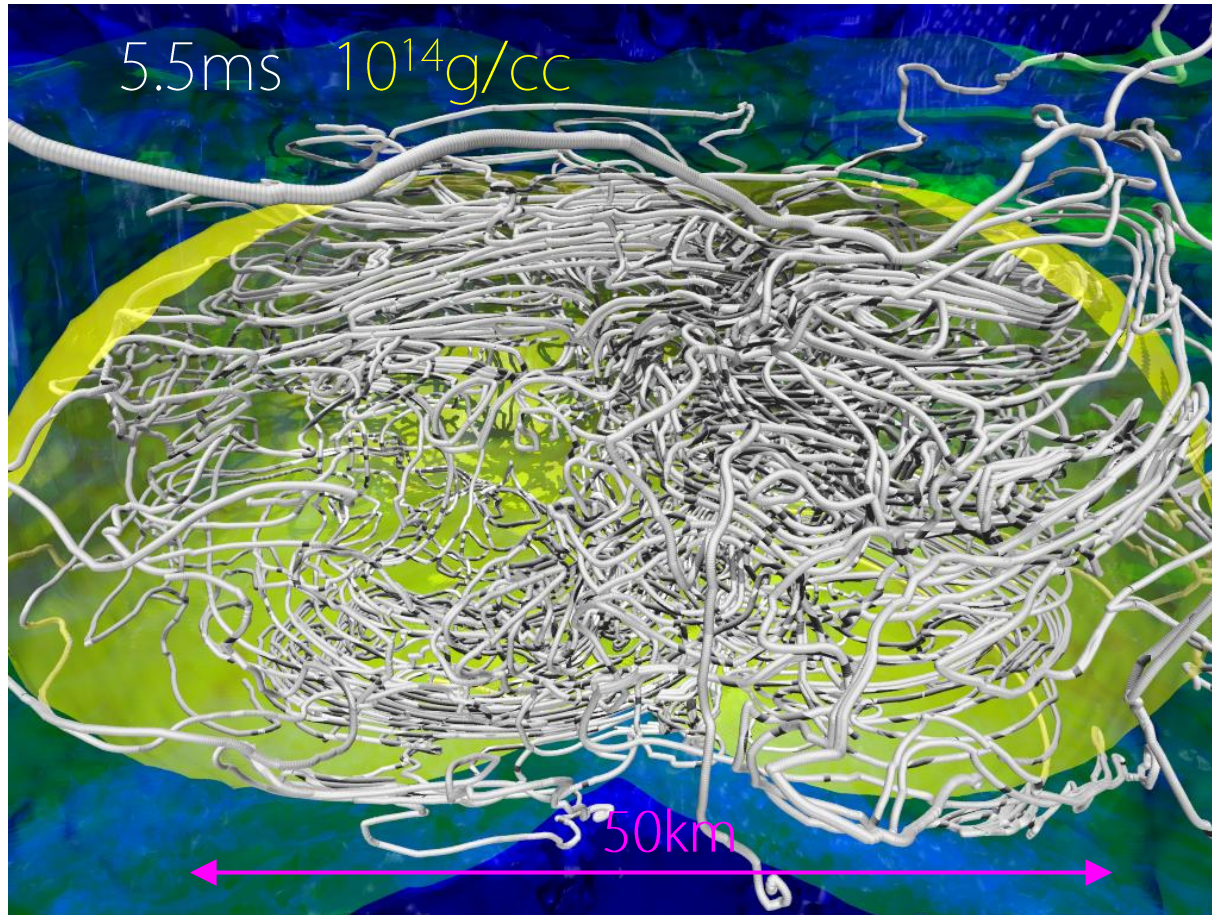
Yes !

Field lines and strength @ merger Amplification factor vs resolution



- ▶ The smaller Δx is, the higher growth rate is.
- ▶ The amplification factor does not depend on the initial magnetic field strength
- ▶ It is consistent with the amplification mechanism due to the KH instability. (Obergaulinger et al. 10, Zrake and MacFadyen 13)

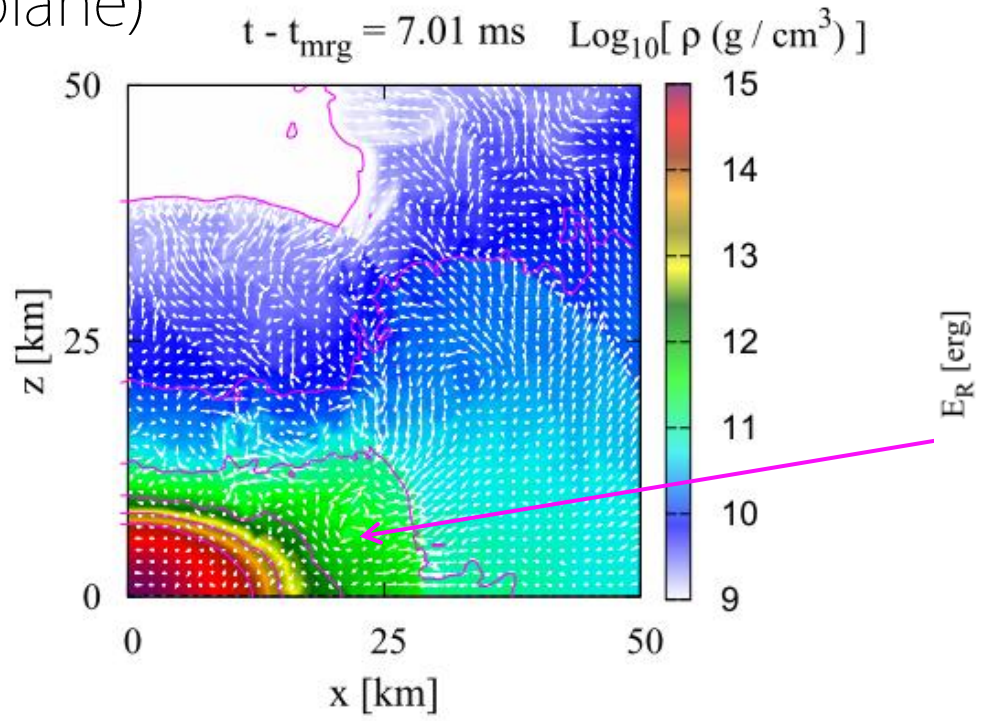
Field lines and density iso-contour inside HMNS



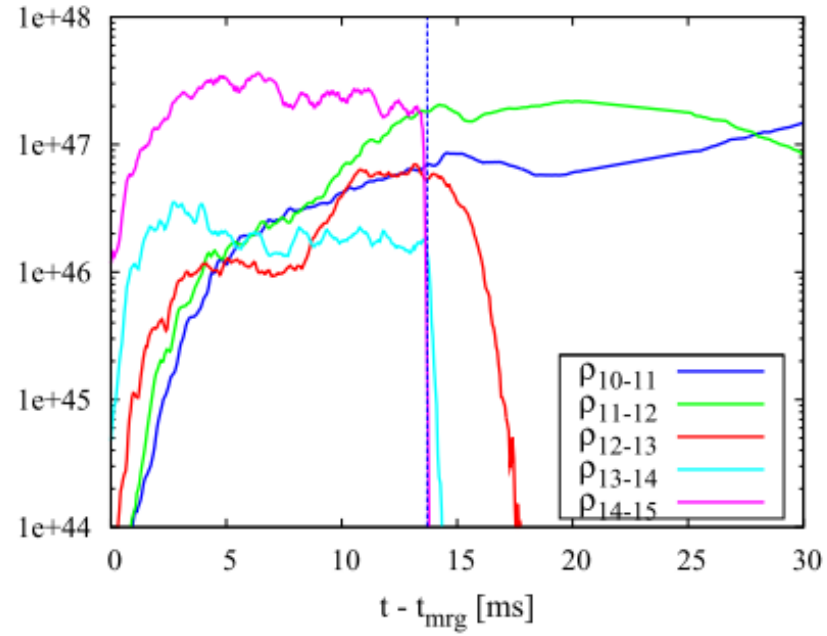
- ▶ Turbulent state inside HMNS
- ▶ HMNS is differentially rotating \Rightarrow Unstable against the Magneto Rotational Instability (Balbus-Hawley 92)
- ▶ Magnetic winding works as well

B-field amplification inside HMNS

Density contour of HMNS (Meridional plane)

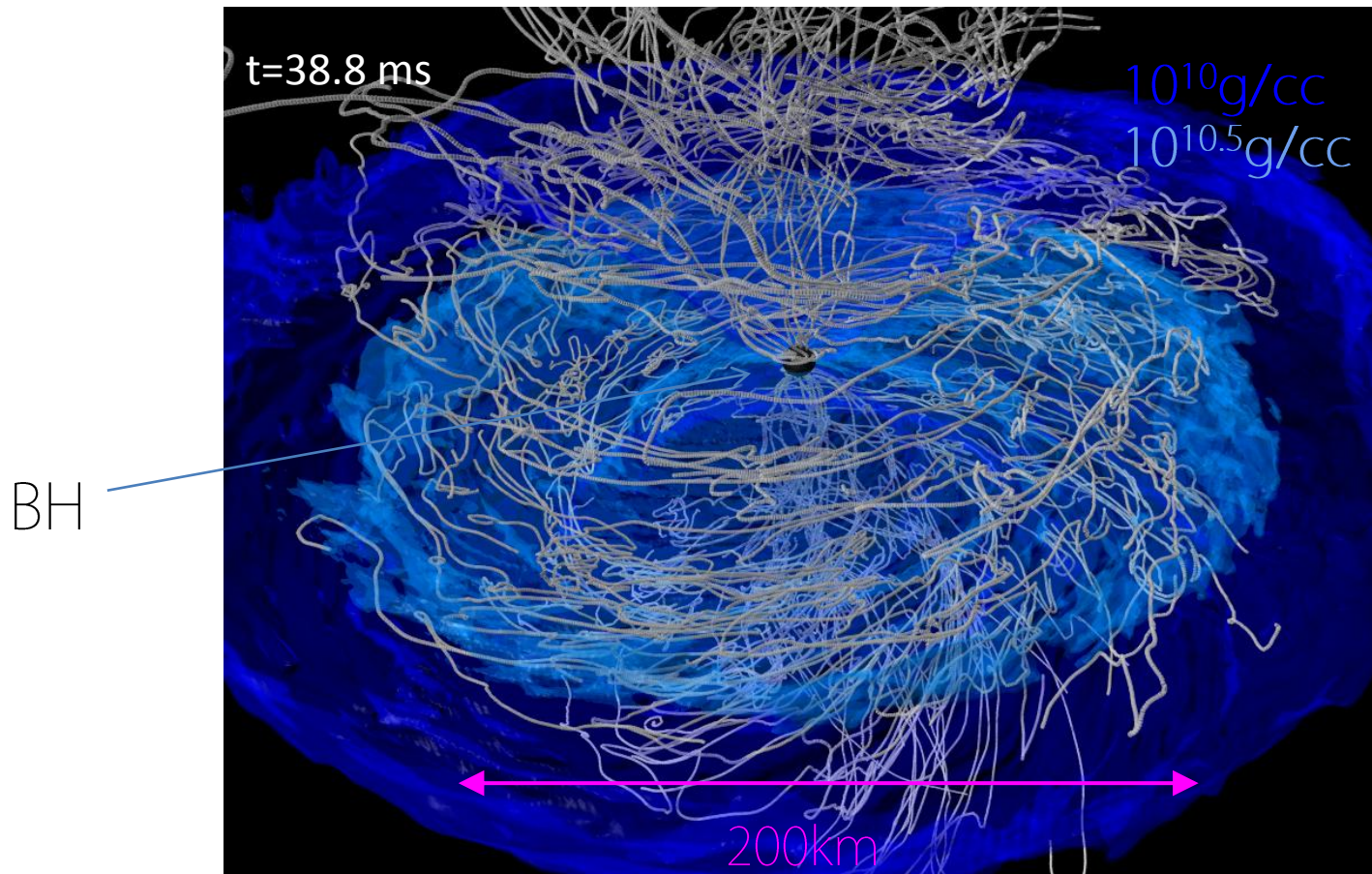


Magnetic field energy inside
 $10^{11} \text{ g/cc} \leq \rho \leq 10^{12} \text{ g/cc} \leq \rho$
 $\leq 10^{a+1} \text{ g/cc}$ $B = B_0 - B_1$ for high-
 res. run



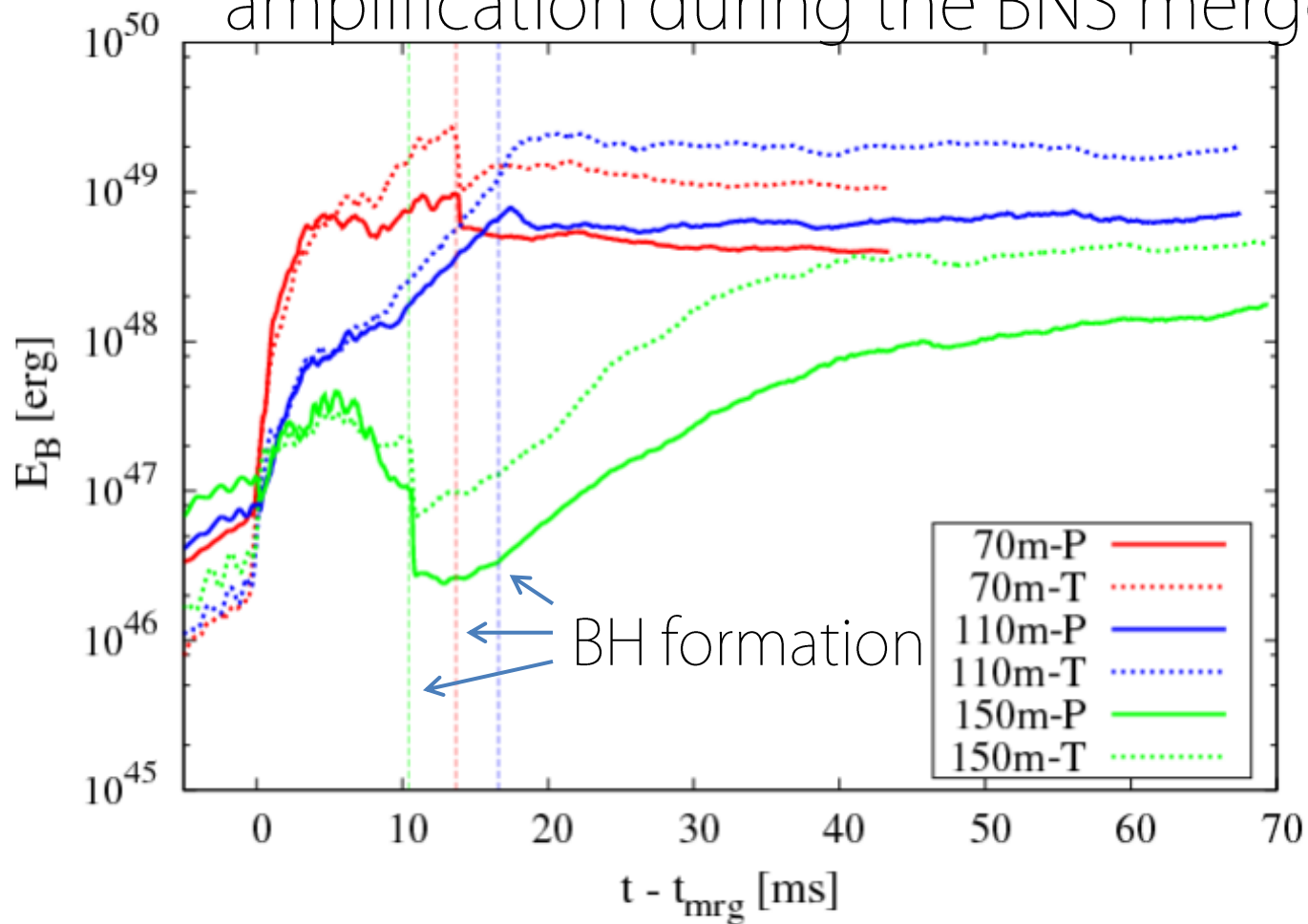
- ▶ $\lambda_{\text{MRI}} = B / (4 \pi \rho)^{1/2} 2 \pi / \Omega$
- ▶ The condition $\lambda_{\text{MRI}, \phi} / \Delta x \gtrsim 10$ is satisfied for the high and medium run, but not in low run. $B =$ Toroidal magnetic field
- ▶ Growth rate of B-fields for 8 - 14 ms $\approx 130\text{-}140\text{ Hz} \sim O(0.01) \Omega$
- ▶ B-field amplification is caused by the non-axisymmetric MRI (Balbus - Hawley 92)

Black hole—accretion torus



- ▶ We have not found a jet launch.
- ▶ Ram pressure due to the fall back motion $\sim 10^{28} \text{ dyn/cm}^2$ (Need 10^{14-15}G in the vicinity of the torus surface)
- ▶ Necessity of the poloidal motion to build a global poloidal field

Summary of the magnetic field amplification during the BNS merger



► KH instability at the merger and MRI inside the HMNS \Rightarrow Significant amplification of B-fields

► Low res. run cannot follow this picture \Rightarrow Amplification inside the BH-torus (picture drawn by the previous works)

Caveats

- ▶ Observation of the BNS ; $B_{\text{dip}} = 10^{12.2}\text{G}$
- ▶ We assume that B_{max} is 10^{15}G

Criticism ; The magnetic fields chosen correspond to the highest magnetic fields observed for some magnetars.

Therefore the present work is still a little academic.

Question ; What's the final value of the amplified magnetic fields ?

- ▶ We are not interested in the magnetar's merger.
- ▶ If you start a "realistic" value of the magnetic fields, say 10^{13}G , you need more grid resolution. Otherwise, such a simulation will be nonsense.

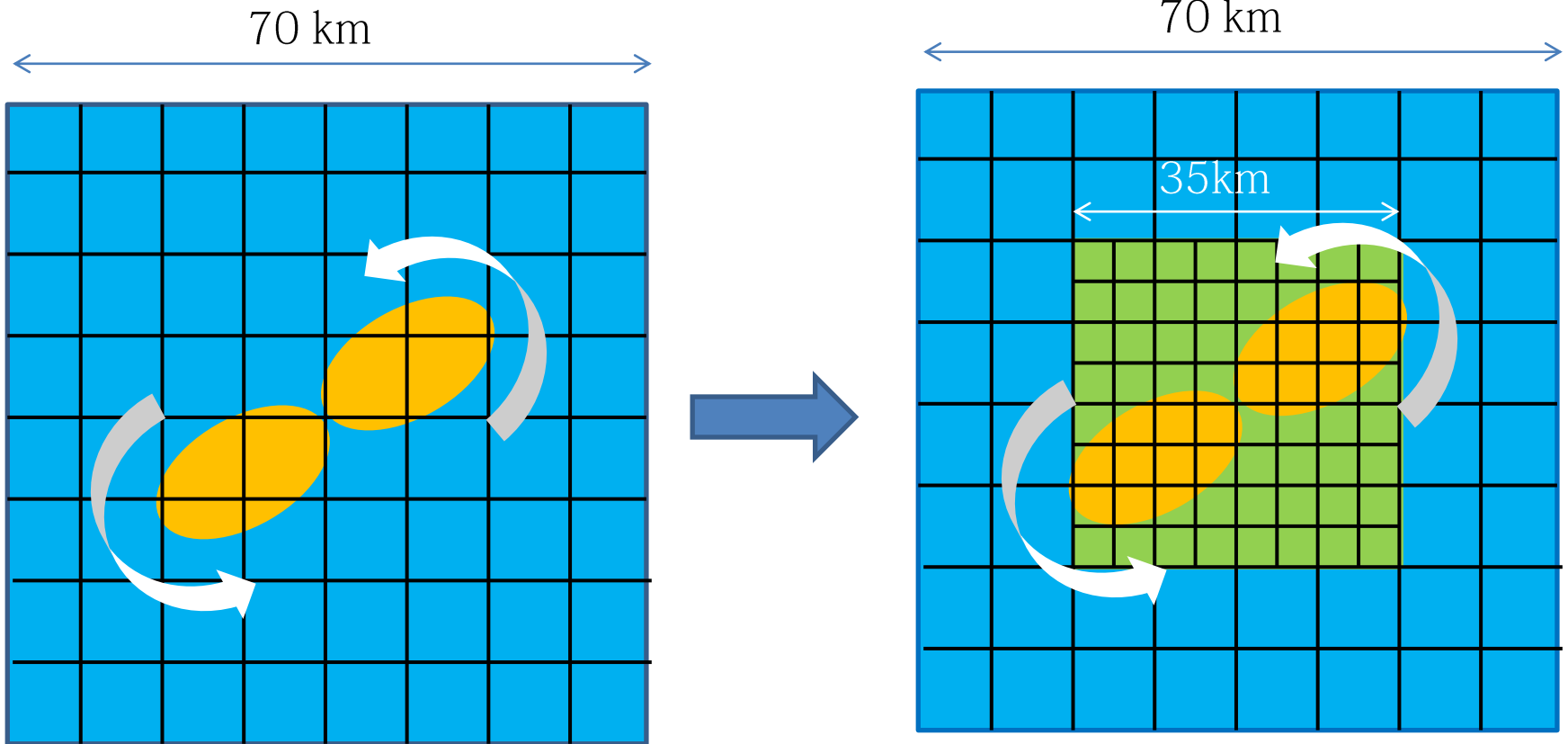
What's the "realistic" value of the amplified B-fields ?

We are doing higher resolution simulations with "realistic" value of the B-fields.

Bridge between global and local simulation

Idea : Just before the merger, we increase the FMR box. The simulation time is about 5 ms.

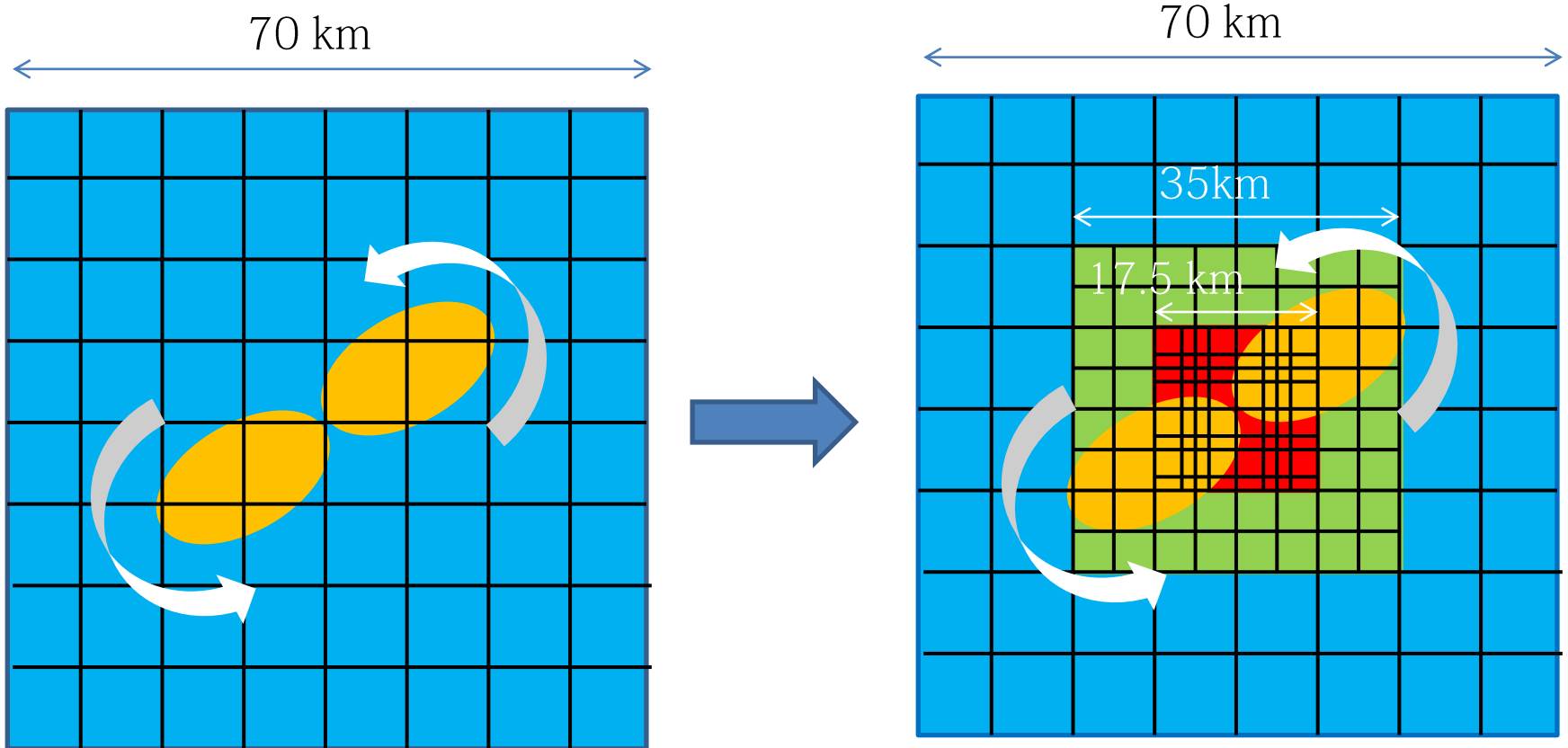
cf. The size of the shear-layer is $\sim 20\text{km}$.



Bridge between global and local simulation

Idea : Just before the merger, we increase the FMR box. The simulation time is about 5 ms.

cf. The size of the shear-layer is $\sim 20\text{km}$.



B-fields amplification via Kelvin-Helmholtz

Model

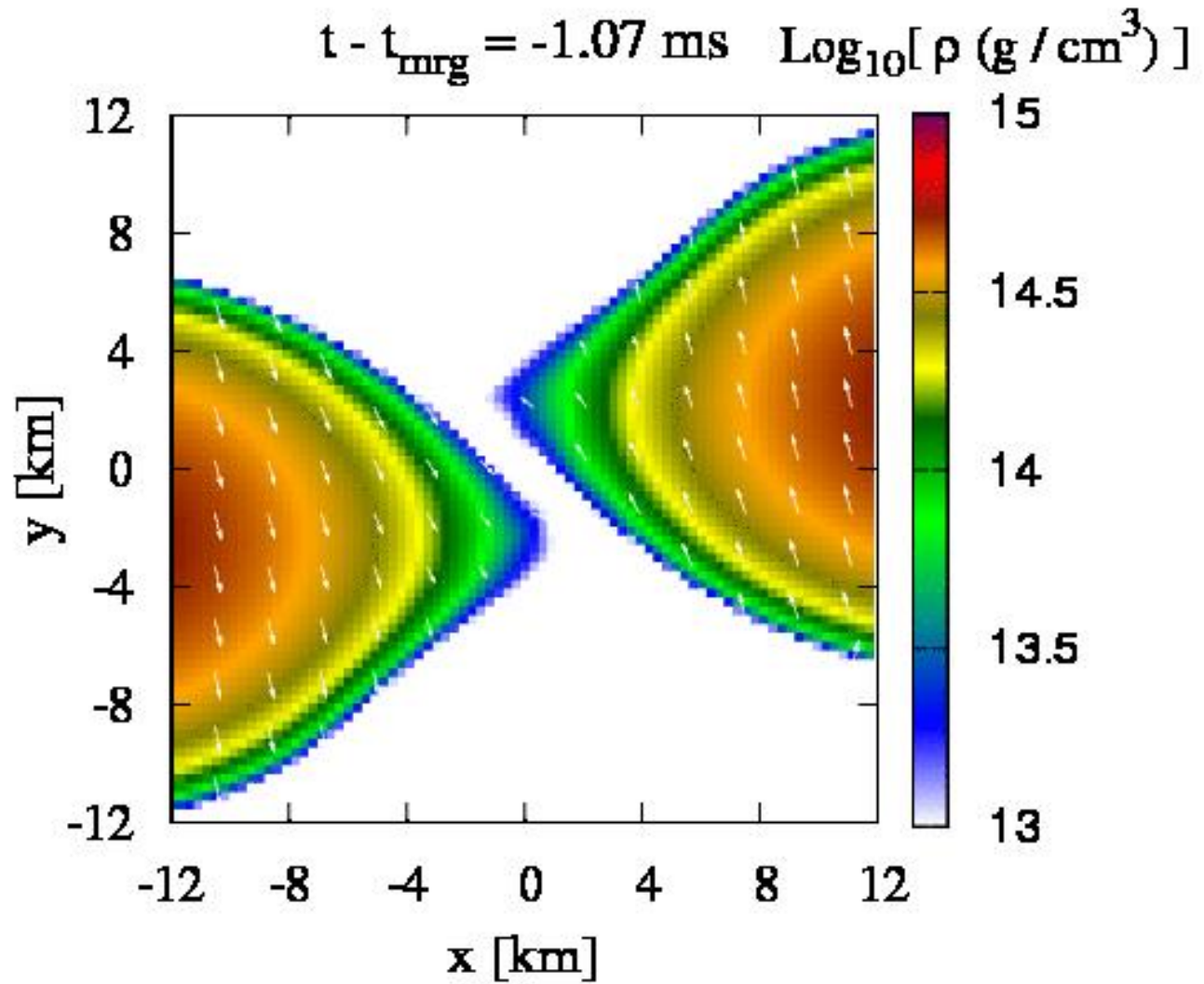
- ▶ 1.4-1.4 M_{\odot} and H4
- ▶ Start from a quasi equilibrium of a **non-magnetized** BNS and stop at $\alpha_{\min} \approx 0.638$.
- ▶ Add the B-fields by hand and increase refinement boxes. The “realistic value” of $B_{\max} \approx 10^{13}\text{G}$.
- ▶ 9 models
 - (ia) $\Delta x = 150\text{m}$; no increase the FMR box
 - (ib) $\Delta x = 150\text{m} \Rightarrow 75\text{m}$; one FMR box is added
 - (ic) $\Delta x = 150\text{m} \Rightarrow 75\text{m} \Rightarrow 37.5\text{m}$; two FMR boxes are added

 - (iia) $\Delta x = 110\text{m}$; no increase the FMR box
 - (iib) $\Delta x = 110\text{m} \Rightarrow 55\text{m}$; one FMR box is added
 - (iic) $\Delta x = 110\text{m} \Rightarrow 55\text{m} \Rightarrow 27.5\text{m}$; two FMR boxes are added

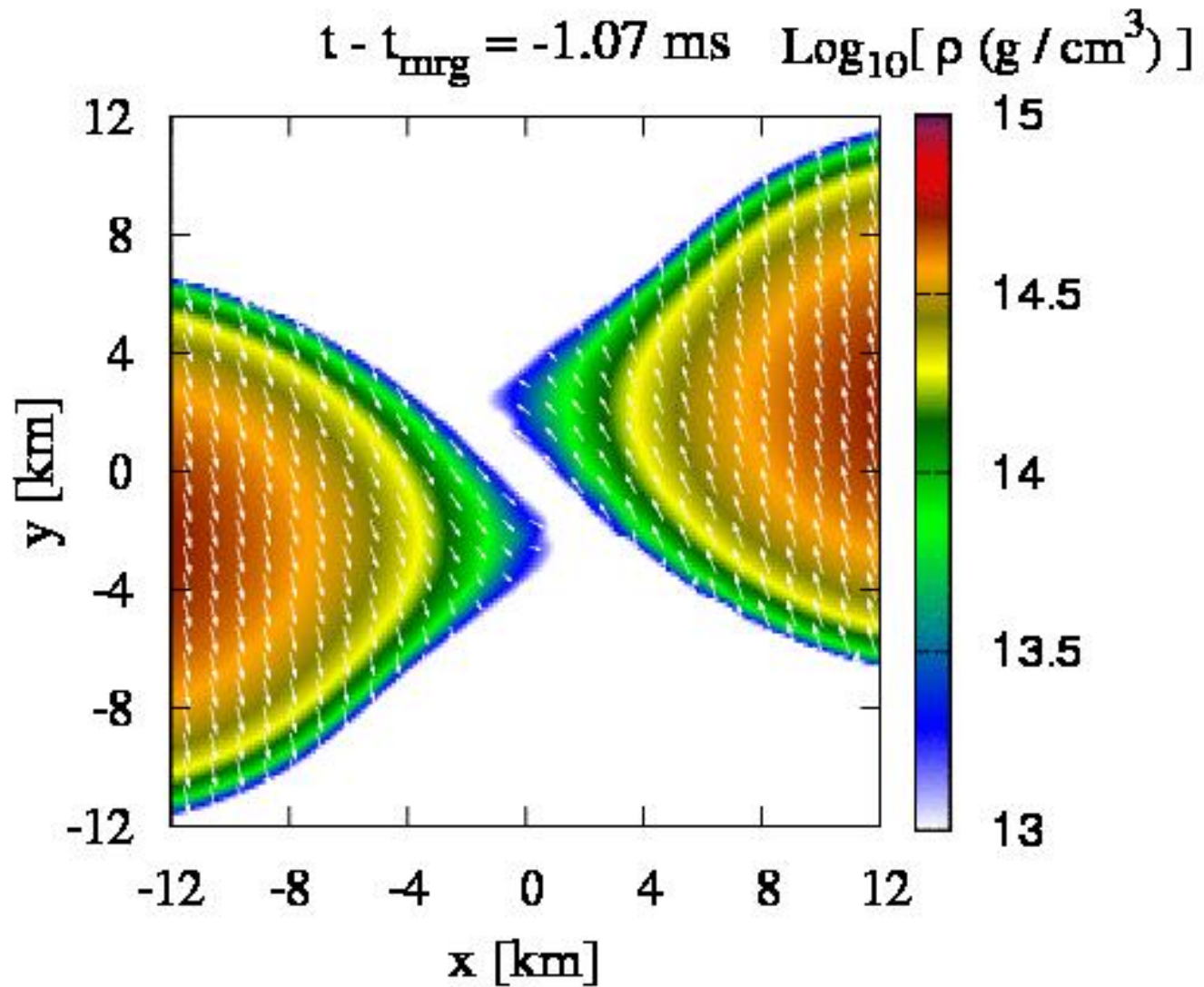
 - (iiia) $\Delta x = 70\text{m}$; no increase the FMR box
 - (iiib) $\Delta x = 70\text{m} \Rightarrow 35\text{m}$; one FMR box is added
 - (iiic) $\Delta x = 70\text{m} \Rightarrow 35\text{m} \Rightarrow 17.5\text{m}$; two FMR boxes are added

In all the models, the finest box size before the merger is about 70 km.

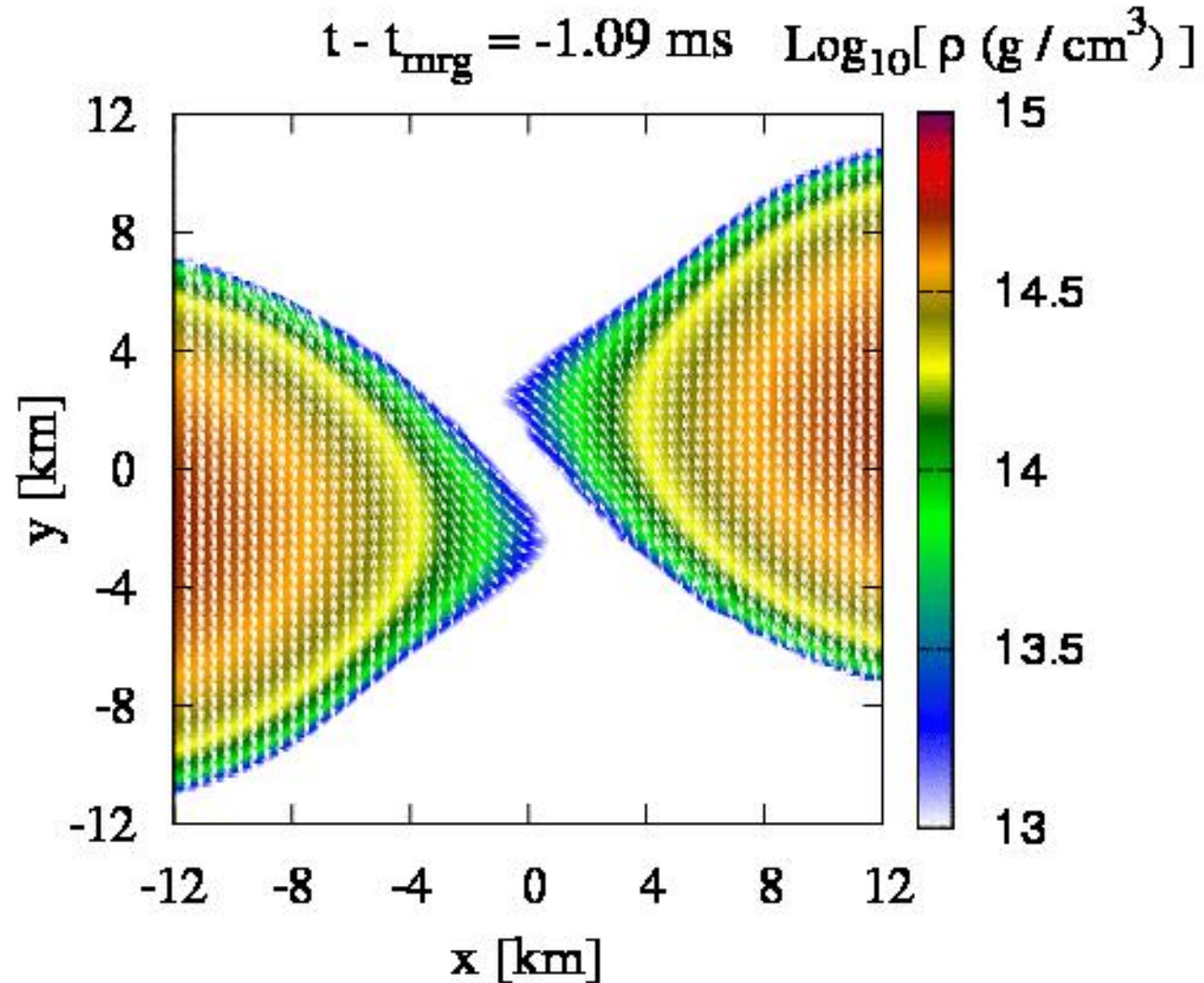
Density and vel. field on the orbital plane ($\Delta x=150\text{m}$)



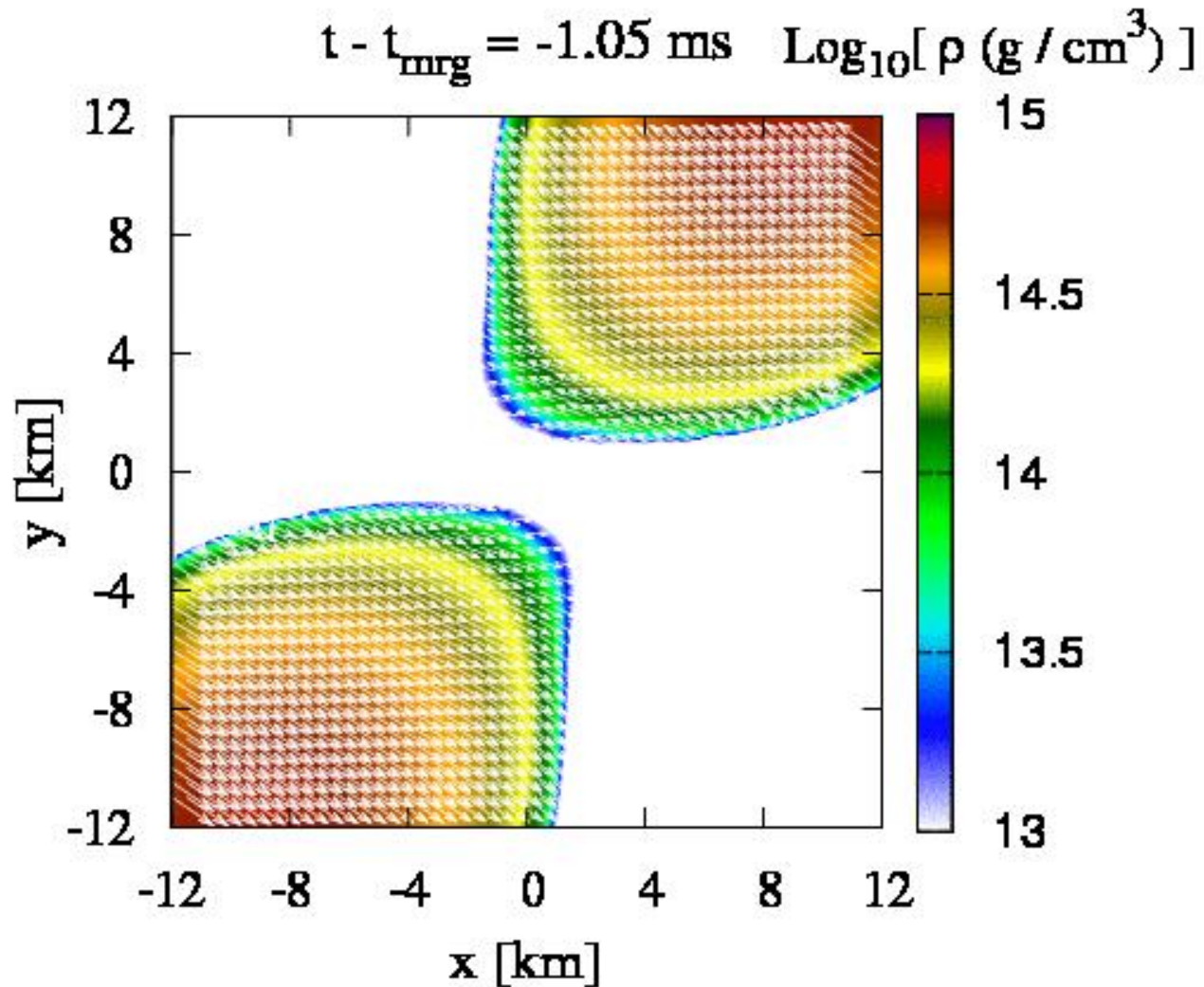
Density and vel. field on the orbital plane
($\Delta x=150\text{m}\rightarrow 75\text{m}$)



Density and vel. field on the orbital plane
($\Delta x = 150\text{m} \rightarrow 75\text{m} \rightarrow 37.5\text{m}$)

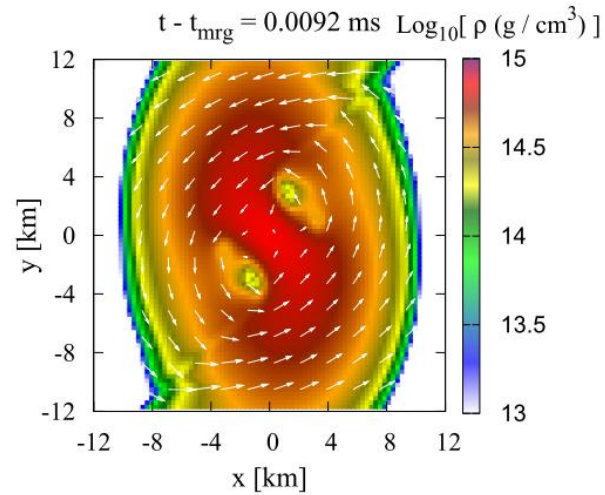


Density and vel. field on the orbital plane
($\Delta x=70\text{m}\rightarrow 35\text{m}\rightarrow 17.5\text{m}$)

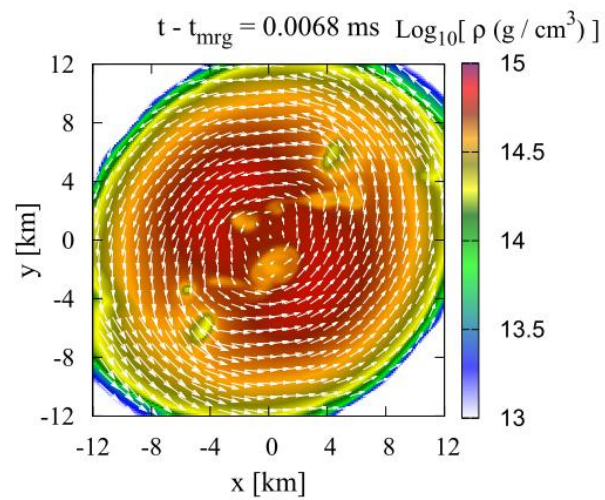


Density and vel. field on the orbital plane

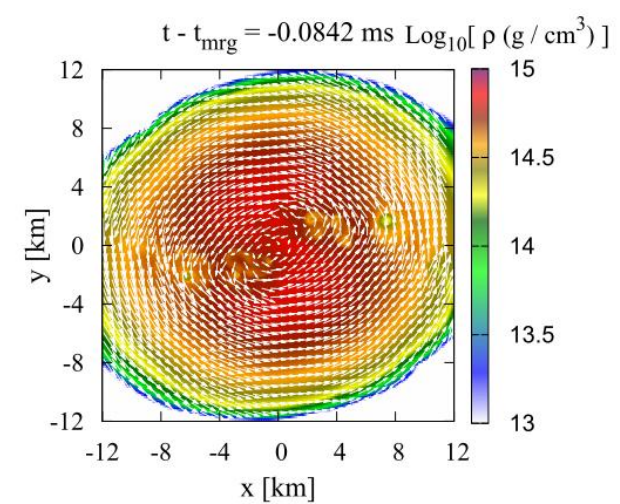
($\Delta x = 150\text{m}$)



($\Delta x = 150\text{m} \rightarrow 75\text{m}$)



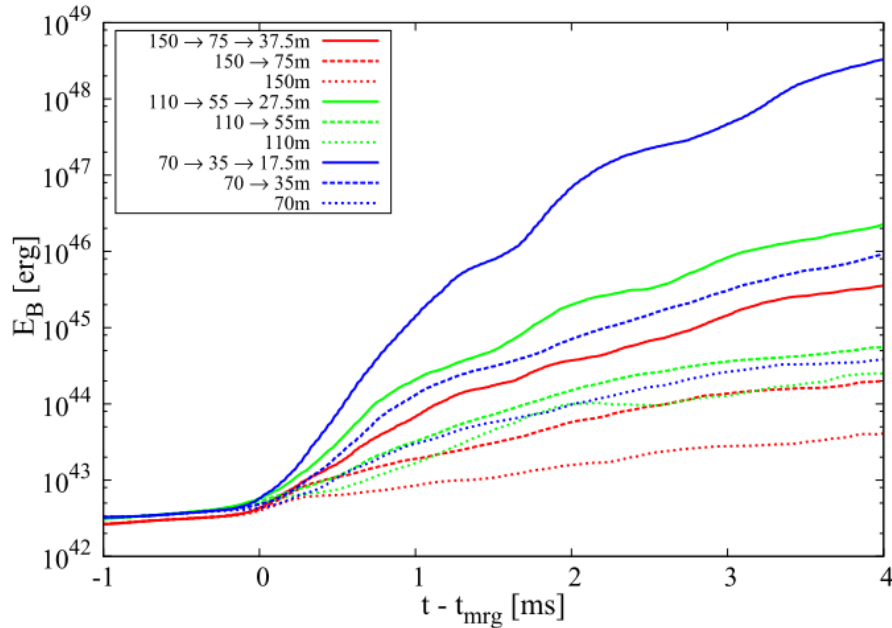
($\Delta x = 150\text{m} \rightarrow 75\text{m} \rightarrow 37.5\text{m}$)



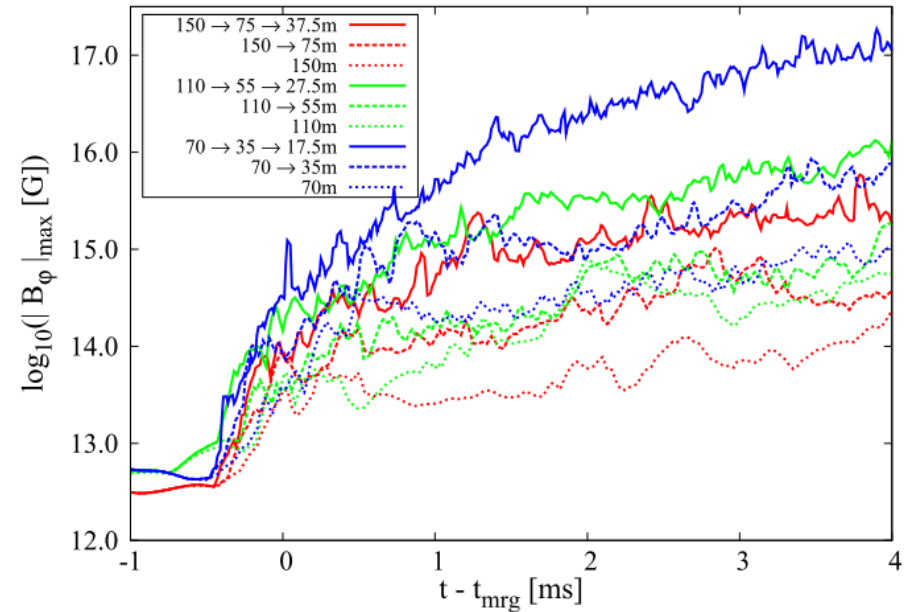
→ Real

Result (Preliminary)

Magnetic field energy evolution



Maximum field evolution



- ▶ Still, the amplification is determined by the resolution.
- ▶ Maximum field is almost virial value, which is comparable to the kinetic energy; i.e., $\sim 10^{17}G$.
- ▶ The magnetic field energy is amplified 10^6 times at least. ; The averaged value of the B-fields is amplified by 10^3 times.

Question ?

- ▶ Angular momentum transport by Reynolds / Maxwell stress ?
- ▶ What happens if the B-fields are dissipated ?

Summary

We have performed a highest resolution simulation of magnetized binary neutron star merger simulation in the framework of Numerical Relativity.

- ▶ Kelvin-Helmholtz instabilities
 - ▶ Non-axisymmetric instabilities
- are key ingredients

The accretion torus
⇒ Qualitatively correct

Caveats

If you start more massive
you need more computing power
be nonsense.

- ▶ Necessity to launch an outflow to build a global poloidal magnetic field.



of massive neutron star

at its birth.
previous works

magnetic fields, say 10^{11} G,
such a simulation will